

# Momentum Transfer Events and Other Disturbances in LRI Data

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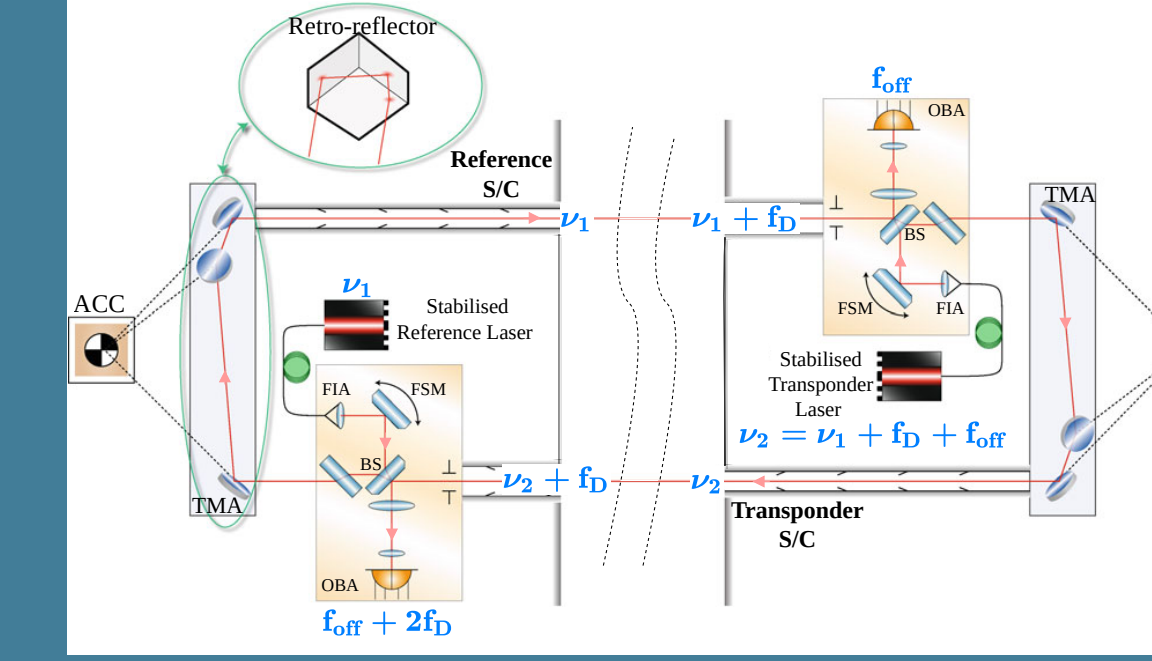
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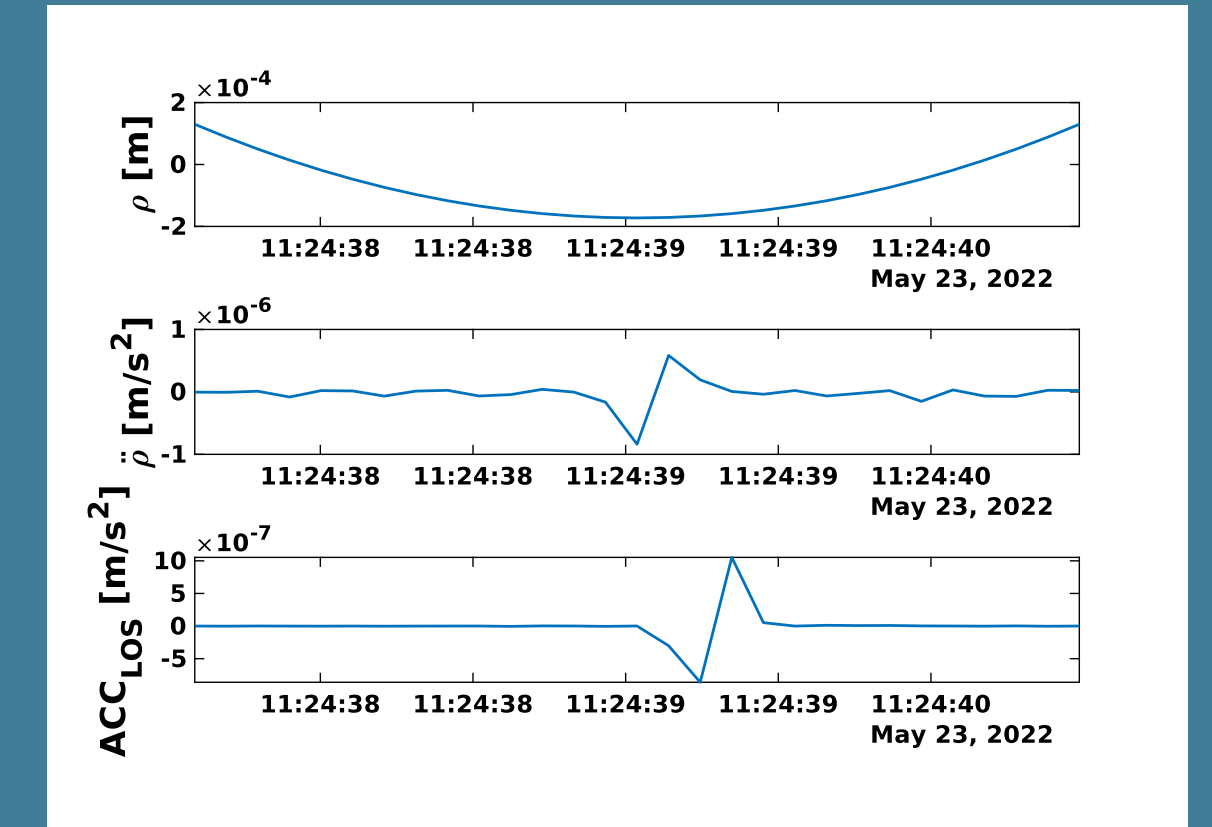
## Introduction

Launched in May 2018, GRACE-FO twin satellite mission hosts the technology demonstrator instrument Laser Ranging Interferometer (LRI) to precisely measure the inter-satellite range variations between the two spacecraft, GF1 and GF2. For the past five years, the LRI has resolved this range within a billionth of a meter. The Earth's gravitational pull acts differently on the two spacecraft and thus changes their separation from a reference distance of 220 km. These distance variations can be used for mapping the Earth's gravity field.



Courtesy: Sheard et al., 2012

Working Principle of LRI: The spacecraft (S/C) are in Reference or Transponder role. The Reference LRI transmits a near-infrared laser beam ( $\nu_1$ ) from the stabilised laser towards the Transponder S/C along the LOS. The received beam at the Transponder is Doppler shifted due to the relative velocity of the spacecraft. The frequency ( $\nu_2$ ) of the Transponder laser is matched to the received frequency with an offset ( $f_{off}$ ) of 10 MHz. This beam is transmitted back to the Reference S/C and undergoes another Doppler Shift. The transmitted and received beams at the Reference S/C interfere to produce a beat note containing the Doppler frequency ( $f_D$ ) from which the range ( $\rho$ ) can eventually be derived<sup>[1]</sup>.



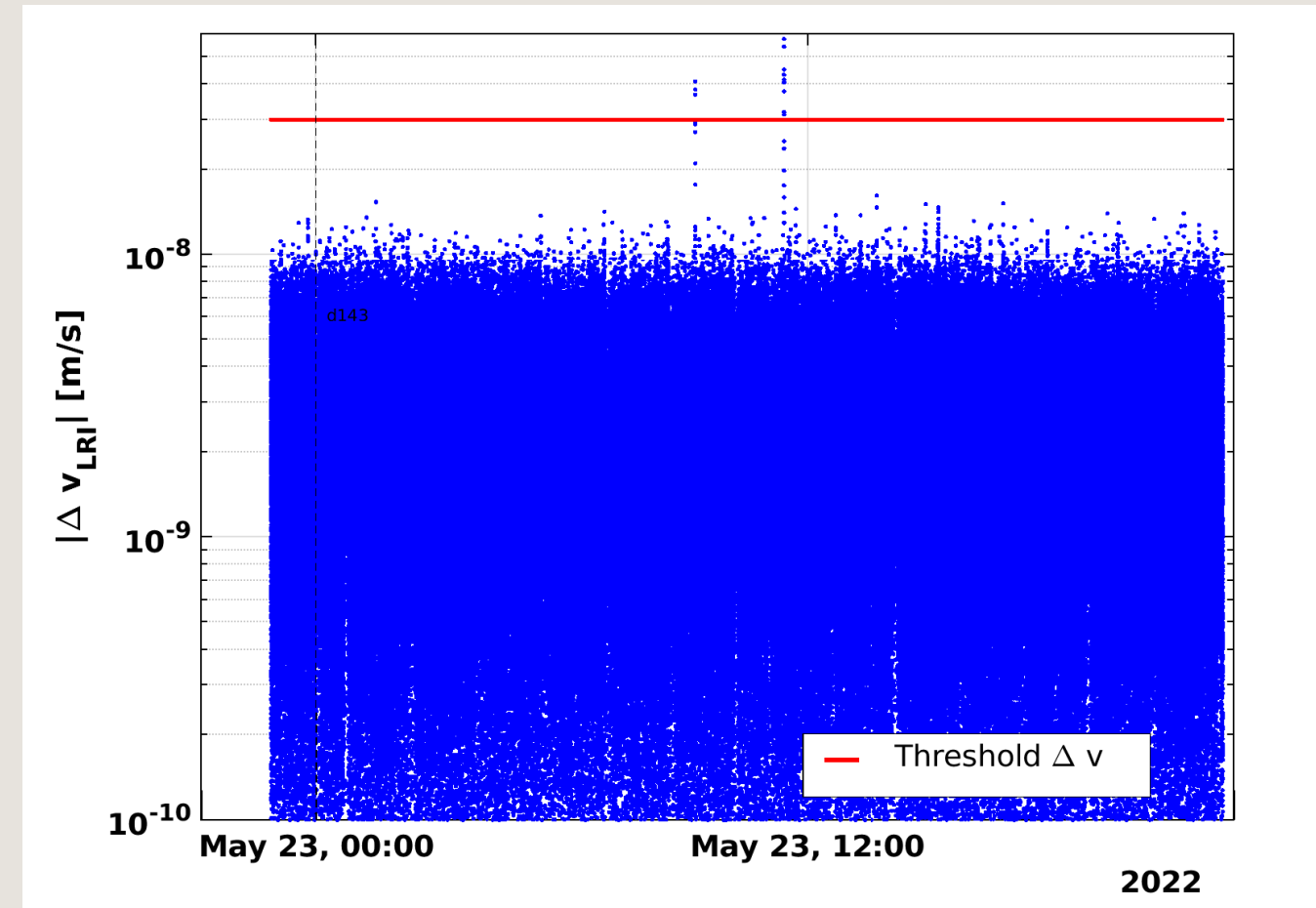
Both LRI and the ACCs measure momentum transfer, and their data is used for the following analysis. The plot shows the respective detrended data in GF1 (Reference) for a typical MTE. mode

We, at the AEI, analyse the LRI data to find disturbances like phase jumps<sup>[2]</sup> and Single Events Effects (SEU)<sup>[3]</sup>, and remove them to obtain low noise range measurements. Momentum Transfer Events (MTEs), as the one on the right, are also a non-gravitational disturbance, but they are not removed from the data because they are true changes in range.

## Detection of MTEs

1. Firstly, the range  $\rho$  is calculated from the ranging phase  $\phi_{LRI}$ . From this range, the spacecraft momentum change  $\Delta v_{LRI}$  is determined. This is done using a unique detrending method<sup>[4]</sup> that removes the background signal and isolates impulse like events to provide an accurate estimate of the  $\Delta v_{LRI}$ . Stretches of the  $\Delta v_{LRI}$  above a certain threshold are considered an MTE candidate.

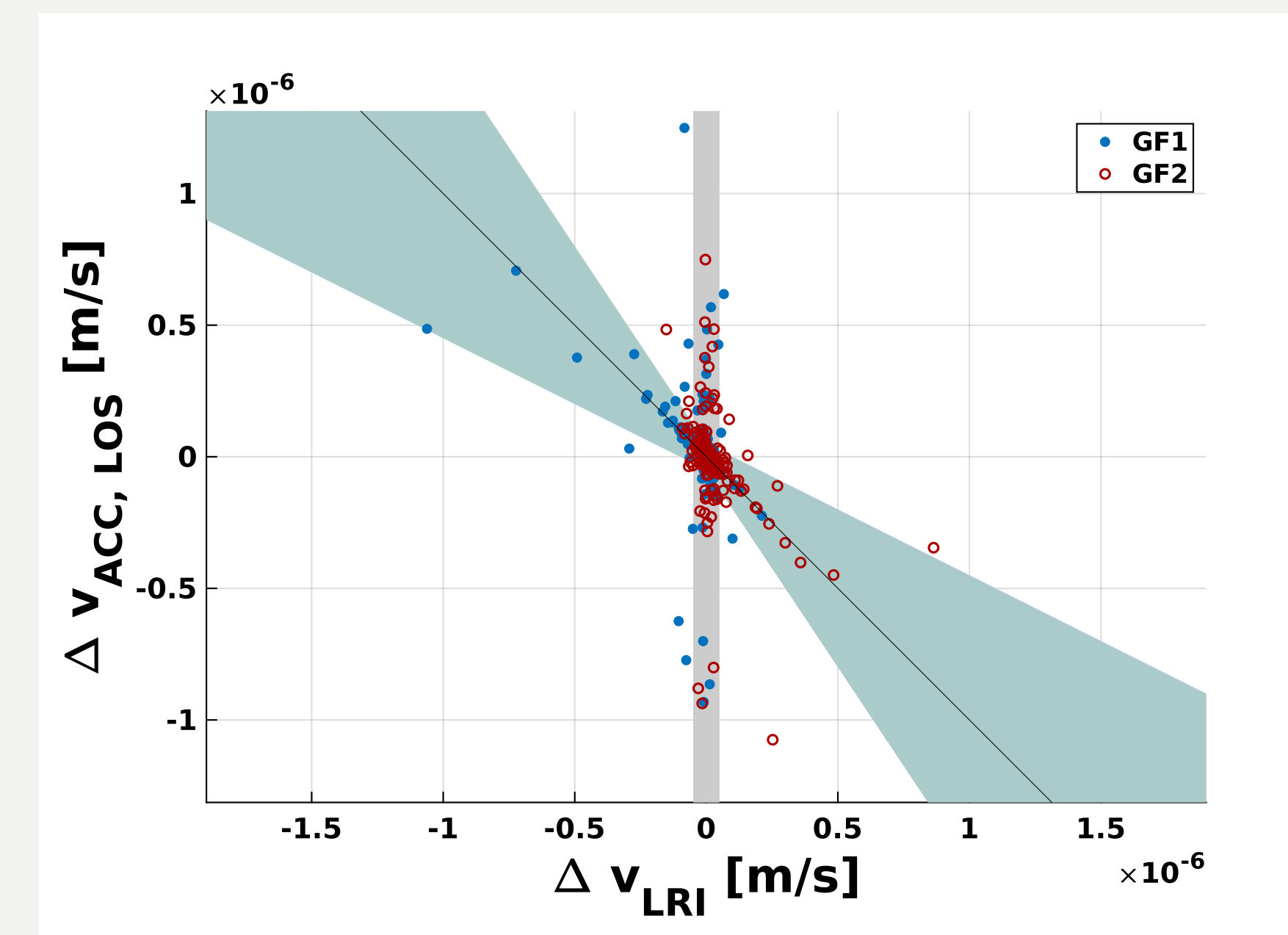
2. The ACC measures accelerations along 3 axes. The ACC time-series along the axis which is roughly aligned with the line-of-sight (LOS) axis of the LRI, is correlated with the LRI range acceleration  $\ddot{\rho}$  for each MTE candidate.



3. MTE candidates where the cross-correlation between ACC and LRI accelerations is larger than 0.1 are marked as MTE.

4. Since MTEs are only detected in the LRI Reference S/C data, the ACC data is used to identify the S/C on which they have occurred. The cross-correlation is computed with ACC data from both S/C. This helps define on which satellite the MTE occurred.

## Results of Detection



### Observations:

1. Number of MTEs detected in GF1 are 140 and in GF2 are 152 for the period between launch of GRACE-FO to July 2023.

2. The  $\Delta v$  estimate of LRI and ACC is either:

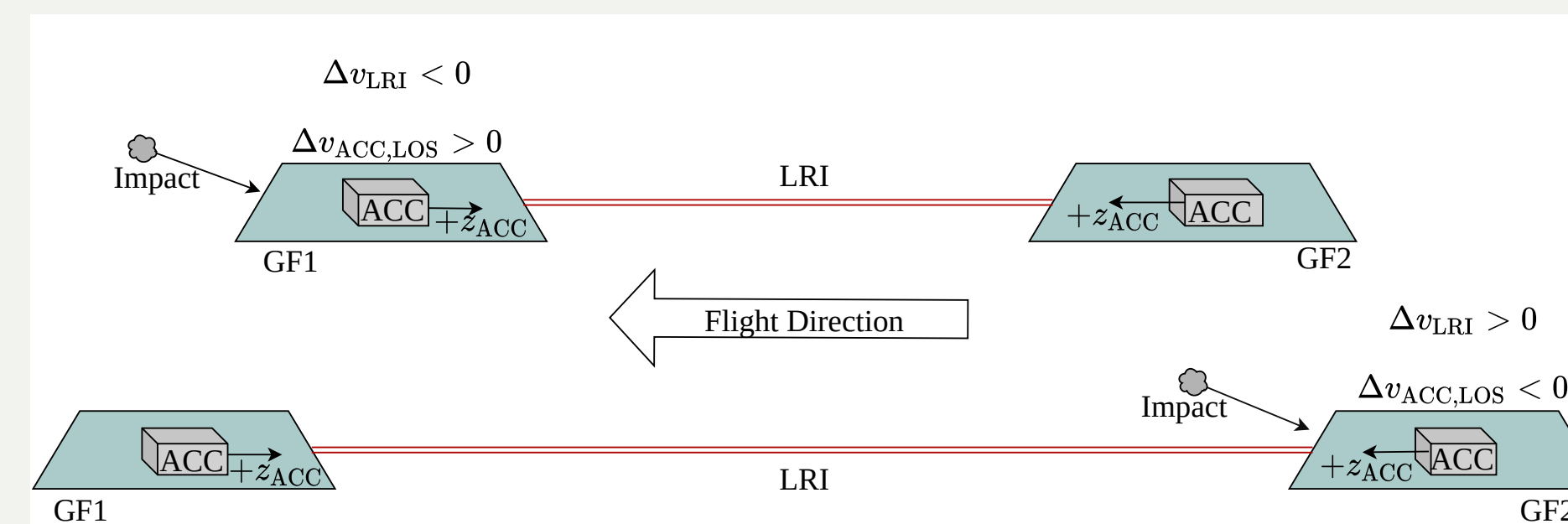
- A well correlated
- B high  $\Delta v_{ACC, LOS}$

3. Correlation plot between  $\Delta v_{ACC, LOS}$  and  $\Delta v_{LRI}$ , show that GF1 and GF2 events occupy different areas along the correlation line. Explained below.

Debris and meteoroids predominantly impact both spacecraft from the direction of flight:

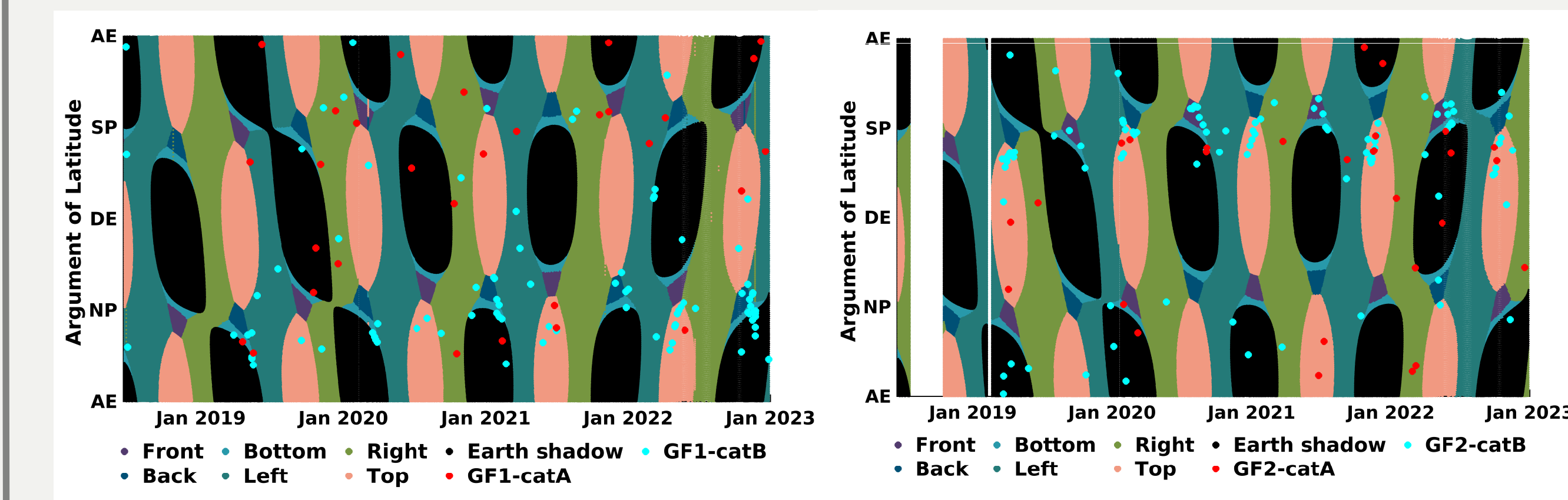
- Impacts on GF1 decrease the intersatellite distance and those on GF2 increase the distance, thereby producing a negative and positive  $\Delta v_{LRI}$ , respectively.

- The SRF +z axis for the ACC is the LOS direction, so impacts on GF1 are along this direction and those on GF2 are against.

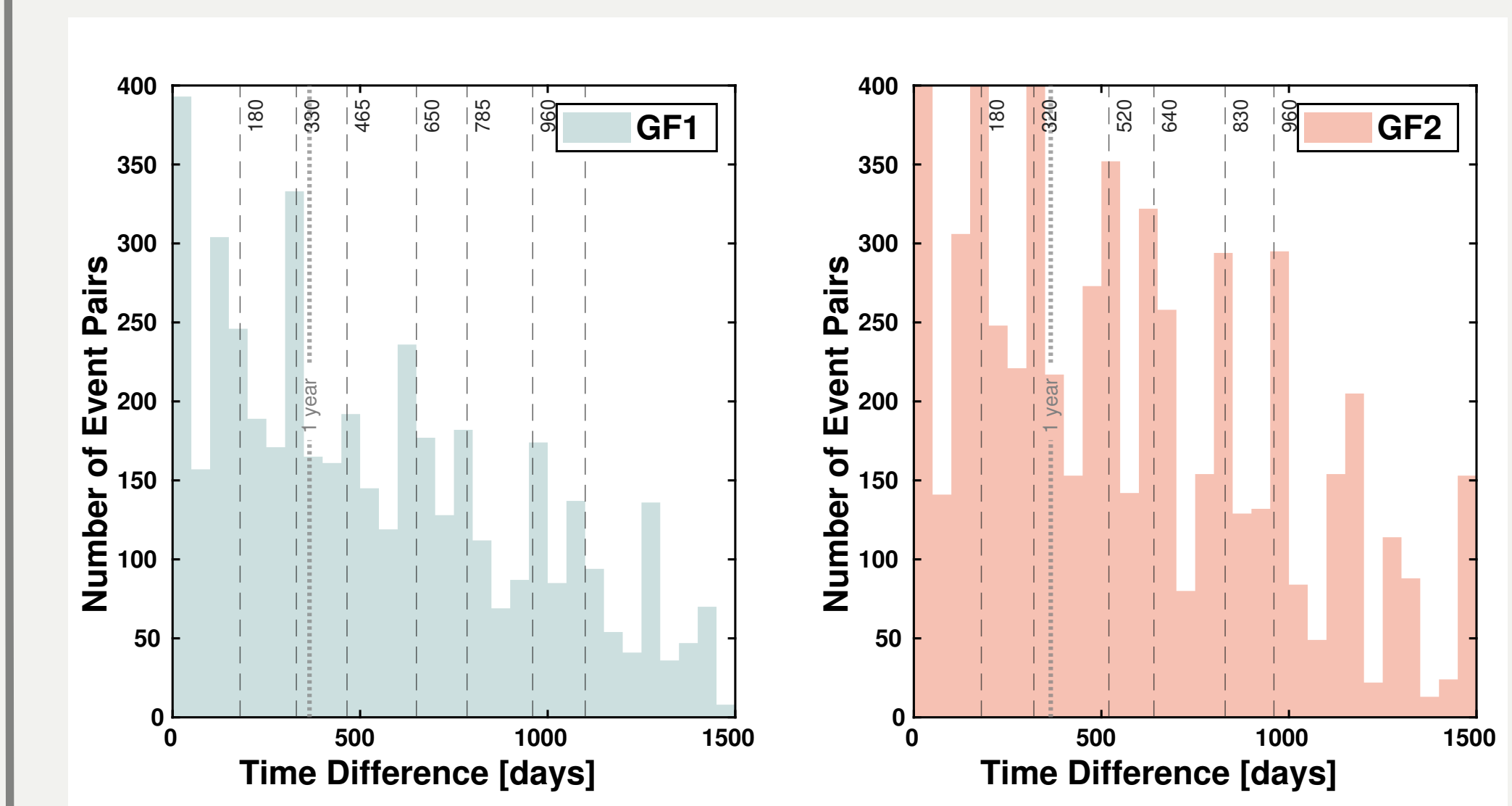


## Argument of Latitude and Periodicity

Events from the two categories over the argument of latitude and time, alongside the different surfaces of the S/C illuminated by the sun:



Events from category A are randomly distributed over the argument of latitude and time, however, those of category B appear in clusters when the surface illumination changes. The periodicity of category B shows its relationship with the beta-angle of the sun.



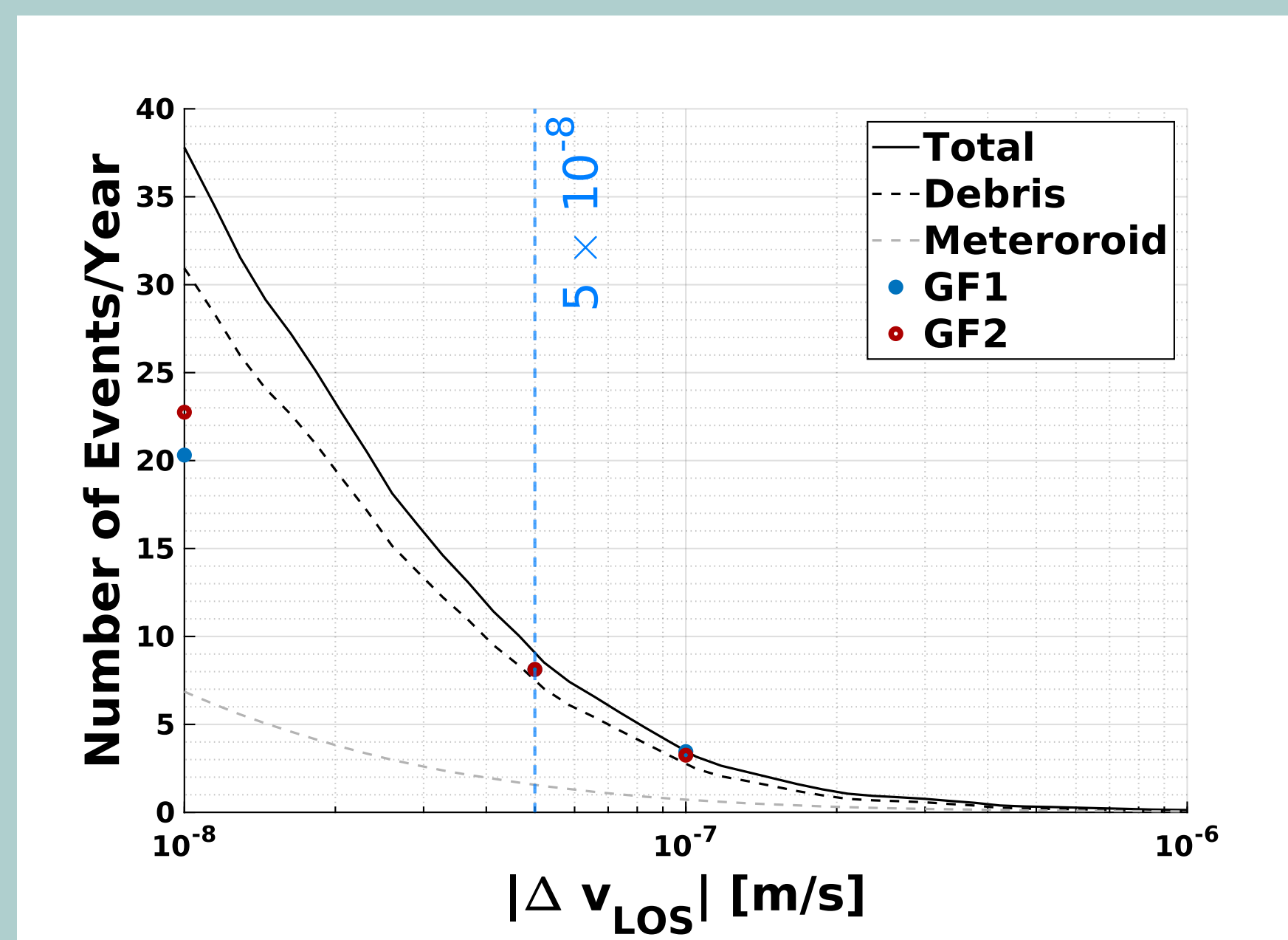
Plot to the left is a histogram of pair-wise time separation between all events.

1. The beta angle repeats every 160 days.

2. Clusters in GF2 are when the beta angle is at 0.

## Simulating MTEs annual rate using ESA MASTER v8.0.3

The software simulates the 3D impact flux of orbital debris and meteoroids on the S/C based on the GRACE-FO's orbit and S/C dimensions. The cumulative histogram shows simulated and observed distribution of events per year for the observed  $\Delta v_{LOS}$  range.



1. For both S/C, the observation adequately matches the simulation for total number of events annually, for  $|\Delta v_{LOS}|$  above  $5 \times 10^{-8}$  m/s.

2. The observation values fall below the model for smaller  $|\Delta v_{LOS}|$ , because such small events can not be properly detected in the noise.

## Conclusion

- Successful detection of 292 MTEs using the LRI data in the five years of its operation.
- The events can be categorised depending on the correlation: The category with high  $\Delta v_{ACC, LOS}$  shows grouping around the argument of latitude where the S/C enters or exits sun shadow. The periodicity of these events can be correlated with the beta-angle of the sun.
- Simulation of MTEs rates using the ESA MASTER software matches observation in the number of events annually for  $|\Delta v_{LRI}| \geq 5 \times 10^{-8}$  m/s.
- As MTEs are actual changes in momentum, these events are not removed from LRI data.

## References

- [1] Sheard, B. S. et al., "Intersatellite laser ranging instrument for the GRACE follow-on mission". *Journal of Geodesy* 2012
- [2] Alkha, Klaus et al., "In-Orbit Performance of the GRACE Follow-on Laser Ranging Interferometer". *Physical Review Letters* 2019
- [3] Misfeldt, Malte; Bekal, Pallavi et al., "Disturbances from single event upsets in the GRACE follow-on laser ranging interferometer". *Advances in Space Research* 2023
- [4] Bähre, Simon J., "Modelling and Removal of Thruster Signatures in GRACE Follow-On Laser Ranging Interferometer Data". *Bachelor Thesis* 2023

