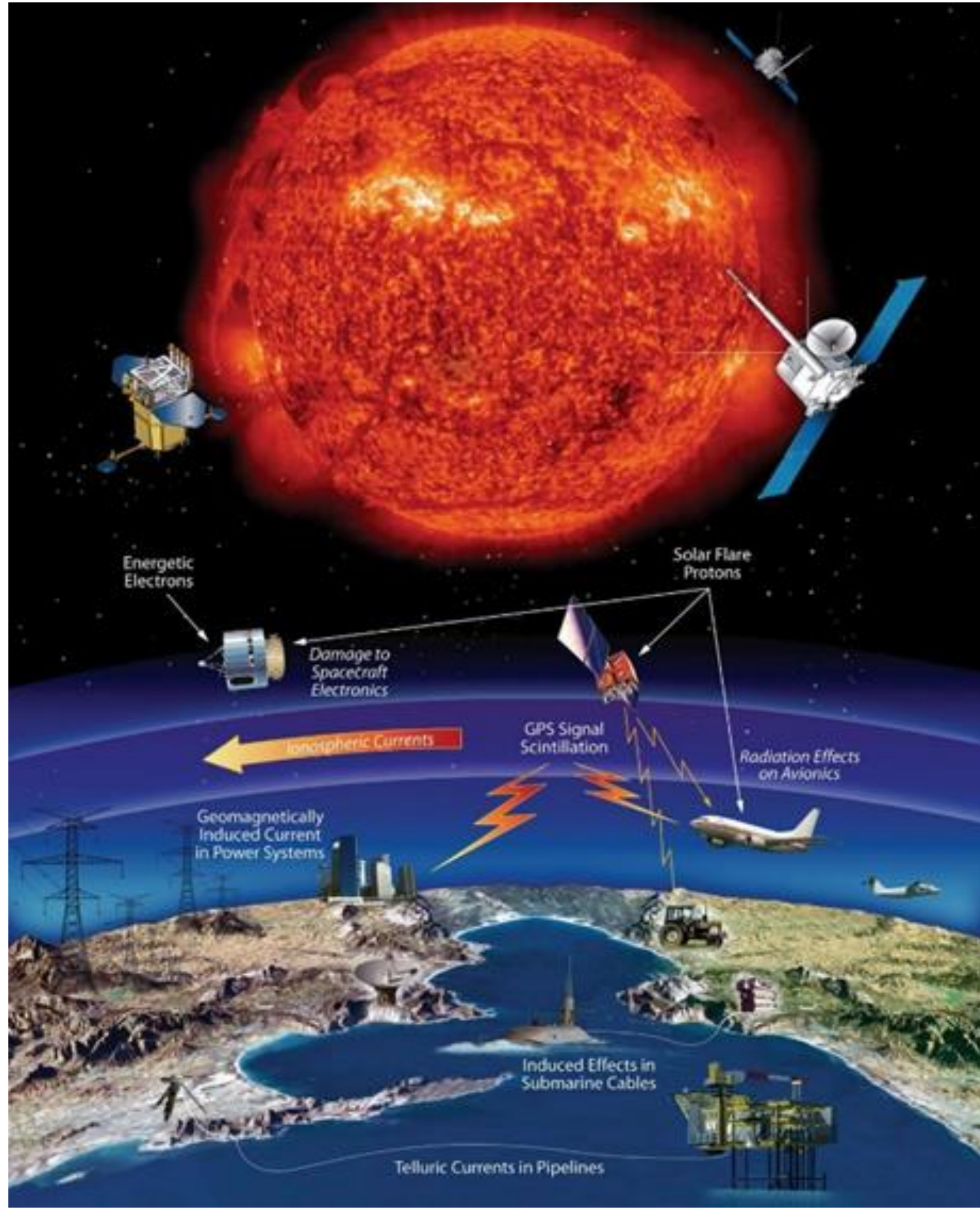


# Sequential Calibration and Data Assimilation for predicting atmospheric variability

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## Introduction



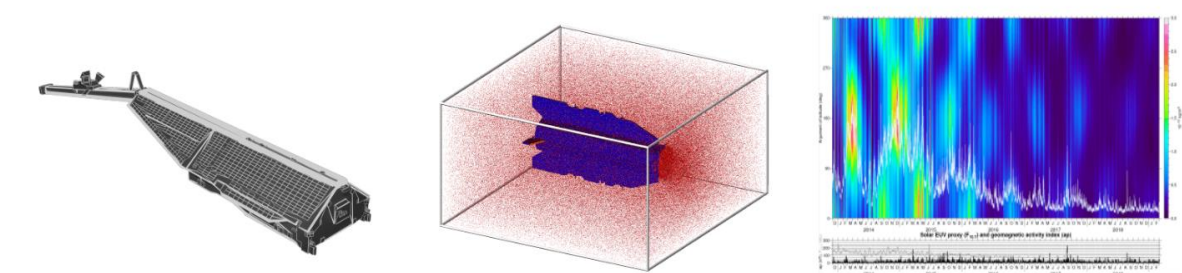
Source: <https://geomag.bgs.ac.uk/>

**Mind the gap in atmosphere!**  
Promoting TEC/Ne and Thermosphere  
Neutral Density as Essential Geodetic  
Variables through the GGOS and IAG  
Spatial / Temporal resolution?  
Coverage? Latency?

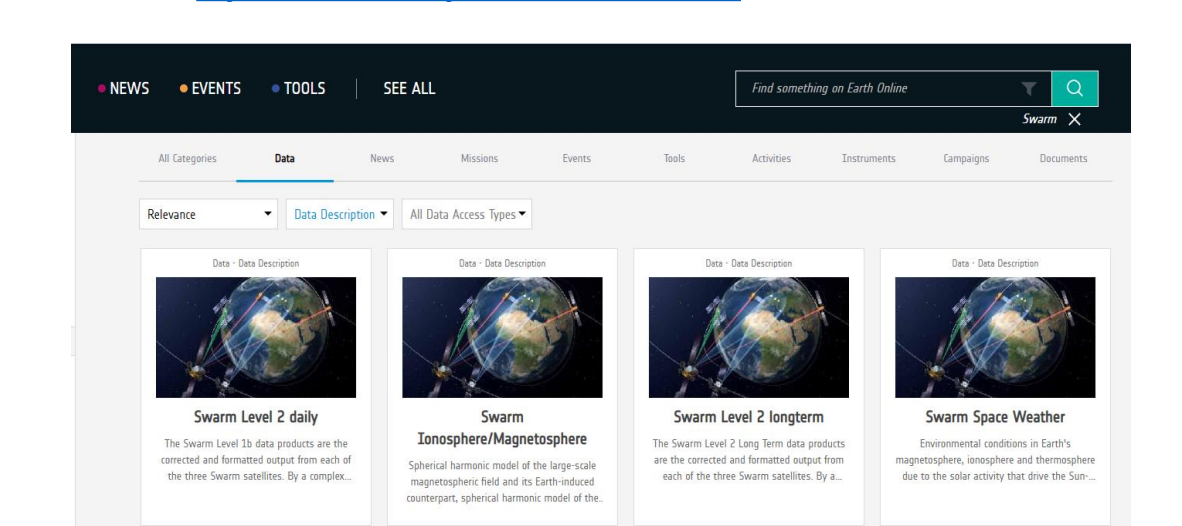
## Data & Model

Space-borne Thermosphere Neutral  
Density (TND)  
Total Electron Content and Density  
NRLMSISE-00  
IRI  
TIE-GCM

All freely available on our FTP server. You might need a FTP client to open the link (user anonymous, any password is accepted).



High-fidelity geometry models for the CHAMP, GRACE, GOCE and Swarm satellites are freely available under Creative Commons License (CC BY-NC-SA).  
<ftp://thermosphere.tudelft.nl/>



<https://swarm-diss.esa.int/>



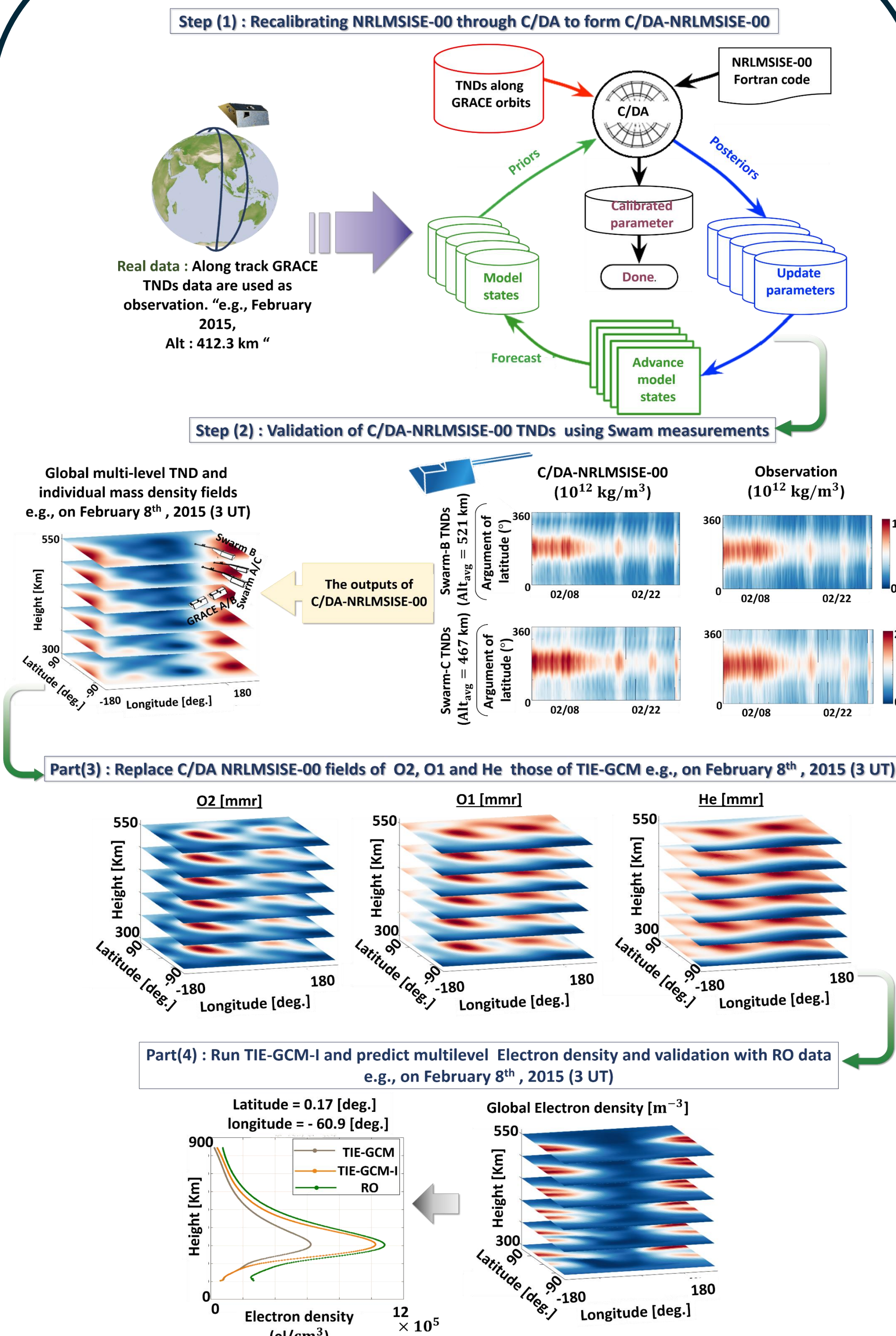
Vielberg, Kristin; Lück, Christina; Corbin, Armin; Forootan, Ehsan; Löcherer, Anno; Kusche, Jürgen (2021): and Swarm. PANGAEA, <https://doi.org/10.1594/PANGAEA.931347>

$$N_e(\lambda, \varphi, h) = \sum_{k=1}^K \sum_{n=1}^N d_{n,k} g_n(\lambda, \varphi, h) Z_k$$

$N_e$  is the 3-D electron density,  
 $g_n$  represents Slepian base functions  
 $Z_k$  contains height-dependent functions  
 $d_{n,k}$  unknown coefficients to be estimated

Farzaneh and Forootan, 2018, Reconstructing regional ionospheric electron density: a combined spherical Slepian function and empirical orthogonal function approach. *Surveys in Geophysics*, doi:10.1007/s10712-017-9446-y  
Farzaneh and Forootan, 2020, A least squares solution to regionalized VTEC estimates for positioning applications. *Remote Sensing*, doi:10.3390/rs12213545

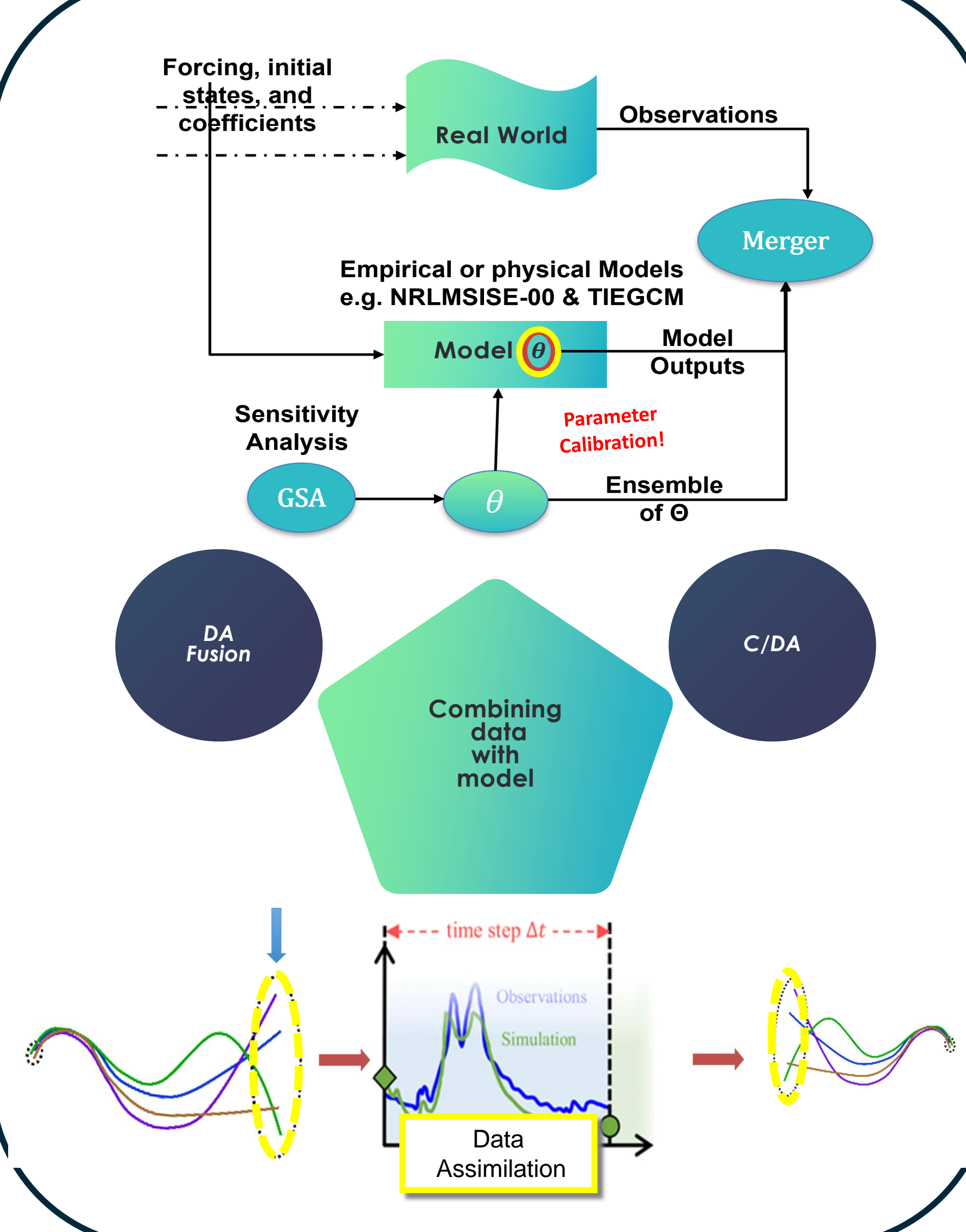
## Method



## Setup of C/DA

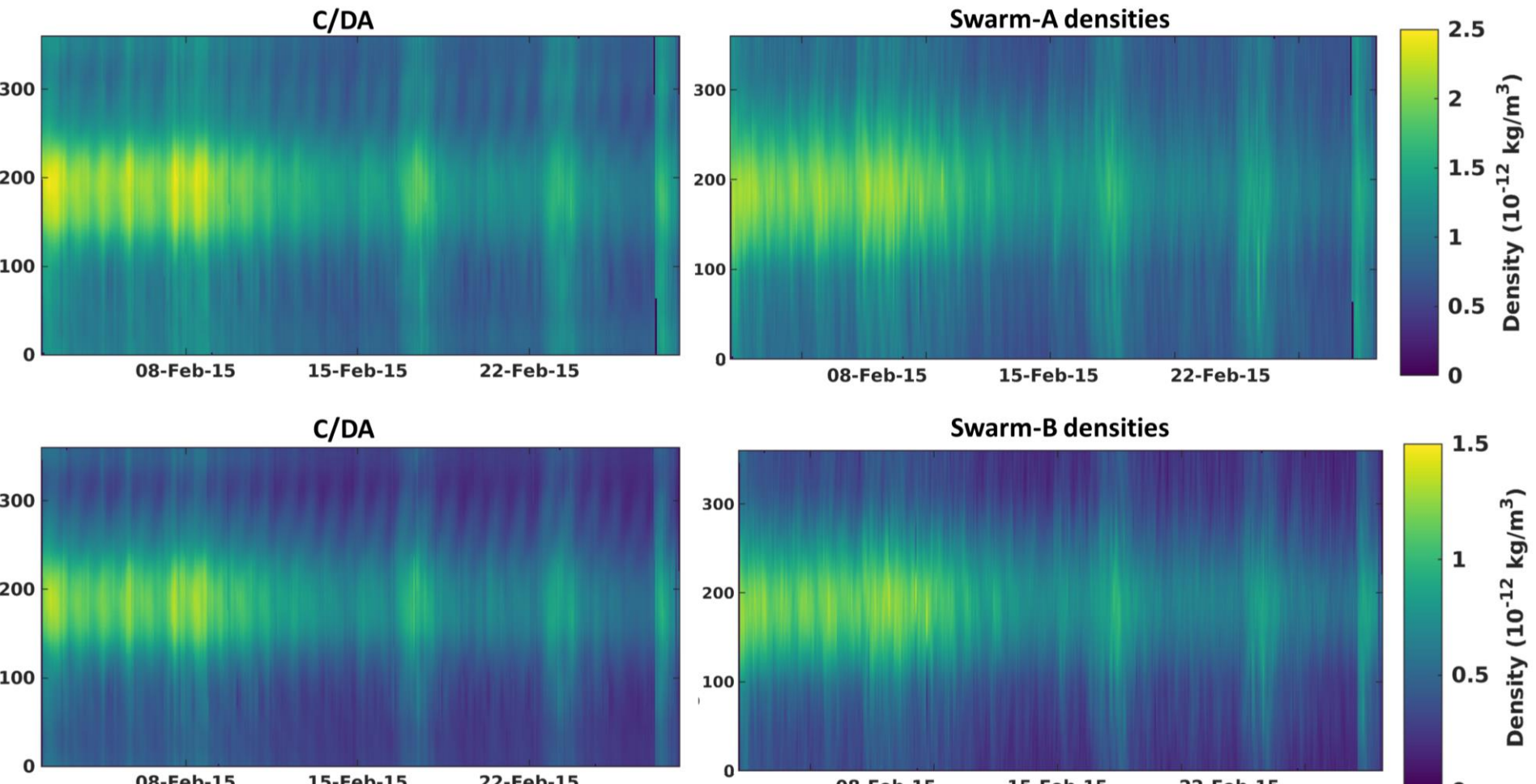
- Method: Ensemble Kalman Filter (EnKF).
- The ensemble size 30-90
- The assimilation window size is 0.5 - 3 hours.
- Experiment Dates: difference atmospheric activity
- Assimilated observations: CHAMP, GRACE, Swarm A-B-C TNDs, GNSS TEC, etc.
- Validations: Radio occultation, In-situ GNSS, positioning applications, etc.

## CDA

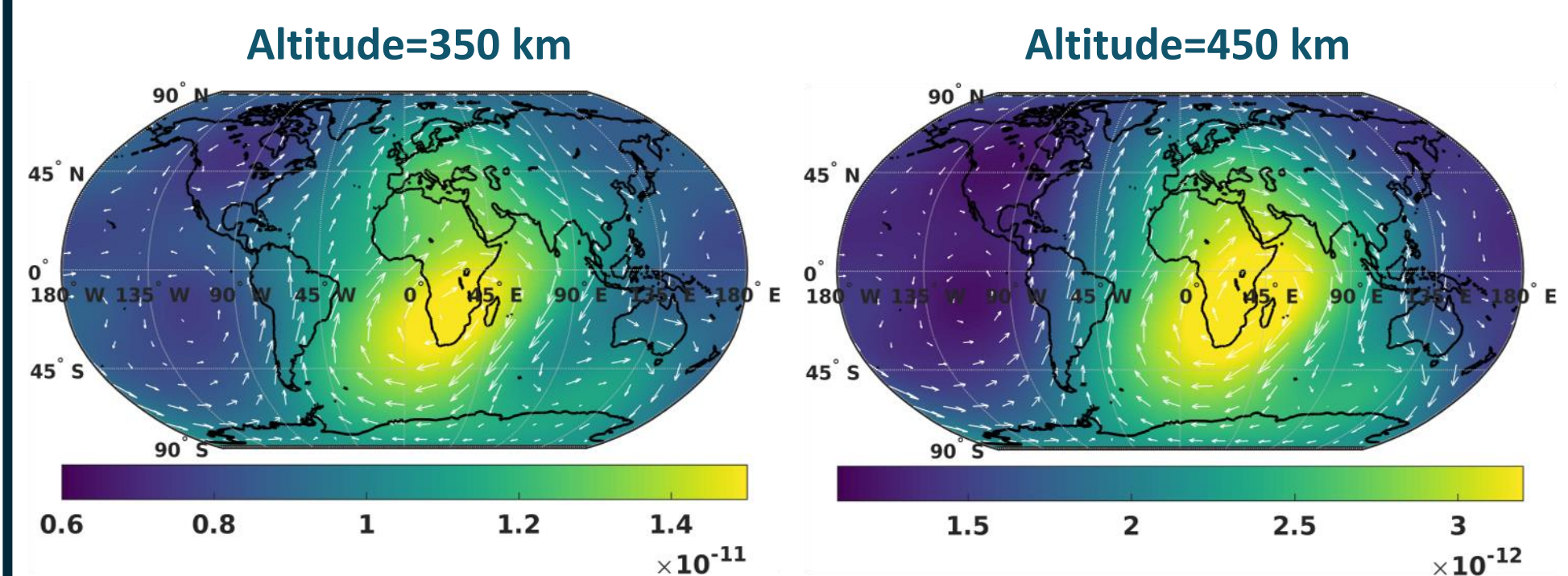


## Results

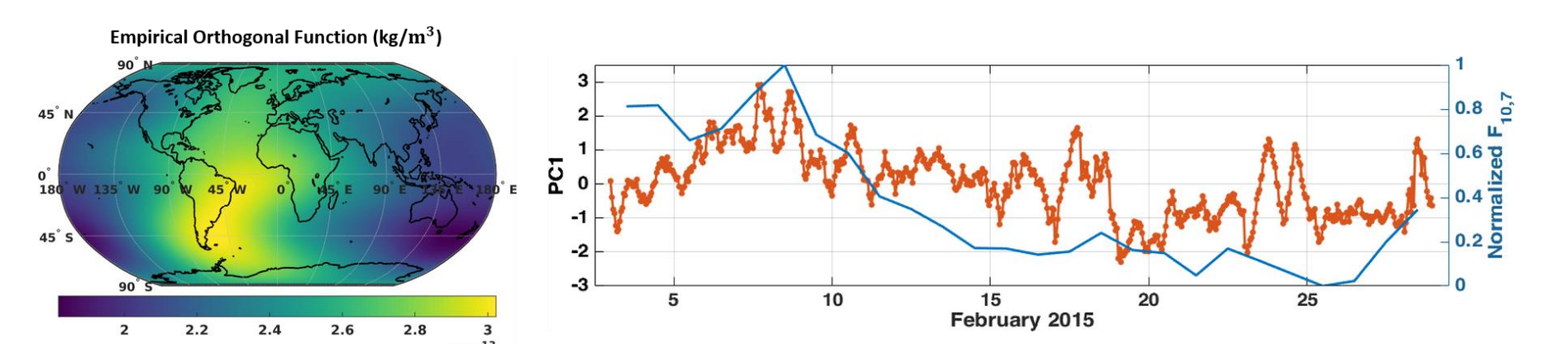
**Forecasting of C/DA-NRLMSISE-00 TNDs along the Daily Tracks Swarm:** Higher spatial correlation of 98.25, 97.53, and 98.25% are found between the TNDs from C/DA-NRLMSISE-00 and observed values along Swarm-A, Swarm-B, and Swarm-C orbits.



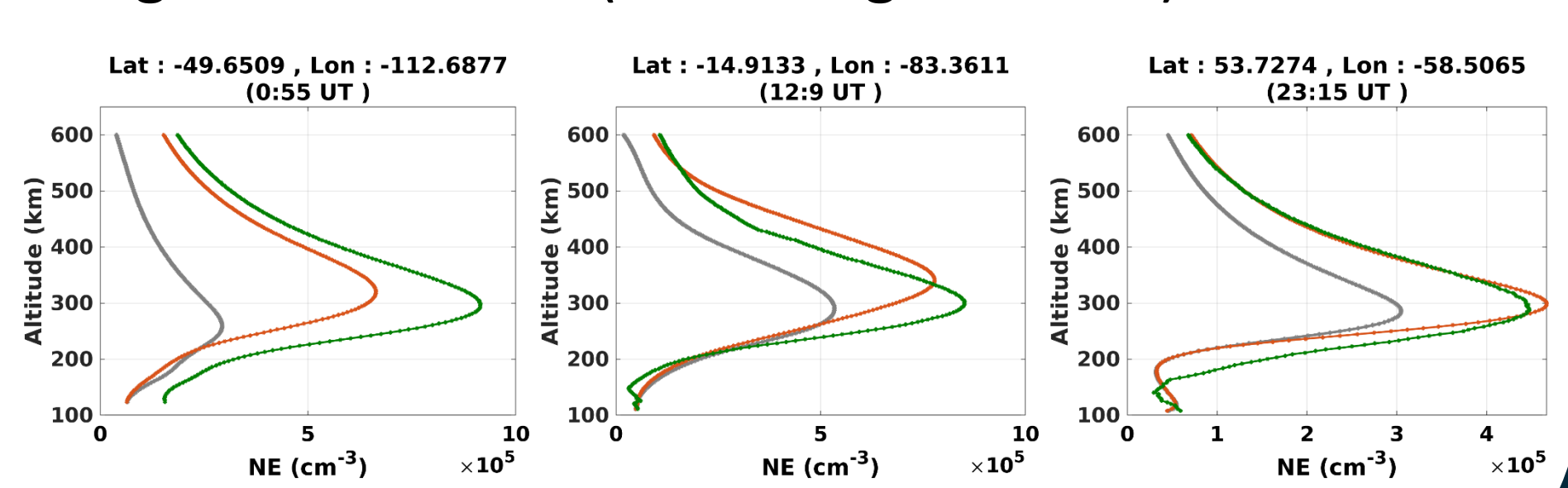
**Multi-level Variations of the global TND:** C/DA NRLMSISE-00 can be used to simulate neutral mass densities in other altitudes and locations.



**Spatial and Temporal Impacts of C/DA through the PCA:** The Principal Component Analysis (PCA) method is applied on the hourly differences between the original and C/DA model during February 2015. PC1 is found to be correlated with the solar activity index with the correlation coefficient of 50.04%.



**Forecasting Ionospheric Parameters:** The TIE-GCM-I reduces the RMSE between the electron density forecasts and RO observations within the range of 0.2-90.6% (on average 30.92%).



## Reference

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