

1 **Constraining Regional Hydrological Sensitivity over Tropical Oceans**

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12
13 **Abstract**

14 Regional hydrological sensitivity (i.e., precipitation change per degree local surface warming)
15 contributes substantially to the uncertainty in future precipitation projections over tropical oceans.

16 By applying a 2-mode model that dissects precipitation changes from sea surface temperature (SST)

17 changes and those from SST gradient changes, we find that the relationship between relative

18 precipitation (i.e., precipitation divided by the basin mean precipitation) and relative SST (i.e.,

19 SST minus the tropical mean SST) and that between relative precipitation and SST gradient remain

20 virtually constant during climate change. This means that regional hydrological sensitivity can be

21 constrained by the present-day SST-precipitation relationship. We report that climate models

22 systematically underestimate precipitation sensitivity to local relative SST changes. However, such

23 a bias has limited impact on tropical precipitation changes, which are primarily associated with

24 SST gradient changes. The sensitivity of precipitation to SST gradient changes is well represented
25 by the multi-model average.

26

27 **Key Points**

- 28 • Regional hydrological sensitivity is an important source of uncertainty in rainfall
29 projections over tropical oceans.
- 30 • Regional hydrological sensitivity can be constrained by components of rainfall-
31 temperature relationship that stay constant during warming.
- 32 • Regional hydrological sensitivity is linked to surface temperature gradients and this link is
33 well captured by the multi-model average.

34

35 **Plain Language Summary**

36 Understanding how precipitation will change over tropical oceans is important because these
37 changes influence the atmospheric circulation, which in turn affects the global climate and weather
38 patterns. Climate models disagree on their projections of precipitation changes over tropical oceans
39 in part due to a lack of understanding on how precipitation should respond to a given amount of
40 local surface warming. We find that the sensitivity of precipitation to future changes in local sea
41 surface temperature (which is commonly referred to as regional hydrological sensitivity) largely
42 depends on how precipitation varies with the local sea surface temperature in the present-day
43 climate. This allows us to constrain the projected precipitation sensitivity to future warming based
44 on the observed present-day precipitation-sea surface temperature relationship. We find that the
45 sensitivity of precipitation to local warming primarily depends on how such warming affects the

46 spatial gradient of surface temperature. This aspect of precipitation sensitivity is well represented
47 by the multi-model average but differs substantially among individual climate models.

48

49 **1. Introduction**

50 Tropical precipitation is a main component of the global hydrological cycle. Both tropical
51 land and oceanic precipitation changes have far-reaching implications on the global climate system
52 via atmospheric teleconnections (e.g., Chen et al., 2020; Lu et al., 2023). The projection of future
53 tropical precipitation is highly uncertain at regional scales (e.g., McSweeney & Jones, 2013). The
54 uncertainty in regional precipitation over tropical oceans is often attributed to the uncertainty in
55 sea surface temperature (SST) changes (Kent et al., 2015; Ma & Xie, 2013), because precipitation
56 changes generally follow local SST changes (S.-P. Xie et al., 2010). But SST is only half of the
57 equation. Chadwick (2016) showed that a considerable portion of the inter-model spread in tropical
58 precipitation changes persist when the models are driven by the same SST changes (their Fig. 5,
59 reproduced in Supplementary Figs. 1a, b). This suggests that the uncertainty in regional
60 precipitation changes (δP) is not only associated with local SST changes (δSST), but likely
61 precipitation sensitivity to local SST changes ($\delta P / \delta SST$) as well. However, regional hydrological
62 sensitivity (which describes precipitation change per degree local surface temperature change) has
63 not been thoroughly studied.

64 On the other hand, there has been great interest surrounding the global and tropical mean
65 hydrological sensitivity due to its substantial variance among climate models (DeAngelis et al.,
66 2015; Su et al., 2017; Watanabe et al., 2018; J. Zhang & Huang, 2023). The tropical mean
67 hydrological sensitivity (often calculated as the percentage change in tropical mean precipitation
68 per degree tropical mean surface warming) varies by roughly a factor of three among the Coupled

69 Model Intercomparison Project (CMIP) models (He & Soden, 2015). Means to constrain the
70 projected tropical mean hydrological sensitivity have been explored in recent studies (Ham et al.,
71 2018; Park et al., 2022). In comparison, regional hydrological sensitivity has received far less
72 attention. However, because the broader impacts of tropical precipitation changes depend more on
73 the regional distribution rather than the tropical mean of such changes (Lu et al., 2023),
74 understanding regional hydrological sensitivity is important from both scientific and pragmatic
75 points of view.

76 While hydrological sensitivity to future warming has been underexplored, it is useful to
77 review precipitation sensitivity to internal SST variations, where some progress has been made in
78 recent years. He et al. (2018) found that the equations that determine the precipitation sensitivity
79 to internal SST variability are the same as those governing the climatological mean SST-
80 precipitation relationship. This means that the response of precipitation per degree internal SST
81 variation is the same as the variation in climatological precipitation per degree climatological SST
82 variation (i.e., the slope of climatological precipitation in SST space, Figs. 1a, b). The implication
83 of such a finding is that during internal climate variations, changes in SSTs result in a geographical
84 reshuffling of convective and non-convective areas while the SST-precipitation relationship
85 remains constant. In addition, because internal precipitation variability is driven by a multitude of
86 factors, a major challenge in quantifying precipitation sensitivity to internal SST variability is to
87 derive a physically meaningful relationship between precipitation anomalies and SST anomalies
88 (Graham & Barnett, 1987; Lau et al., 1997; C. Zhang, 1993). The constancy in SST-precipitation
89 relationship during internal climate variations allows us to constrain models' precipitation
90 sensitivity to internal SST anomalies by using the observed climatological SST-precipitation

91 relationship. It was shown that climate models systematically underestimate precipitation
92 sensitivity to internal and seasonal SST variations (Good et al., 2020).

93 Although precipitation responds differently to internal and anthropogenic SST variations
94 (e.g., Kramer & Soden, 2016), it has been reported that certain aspects of SST-precipitation
95 relationship could remain constant during climate change. For example, Johnson & Xie (2010)
96 examined the tropical mean SST-precipitation relationship and argued that the present-day and
97 future relationship between precipitation and relative SST (SST_{rel} , defined as SST minus the
98 tropical mean SST) is roughly the same (their Fig. 3a). But this appears to be an oversimplification
99 when the three tropical basins are examined separately. As shown in Figure 1b, the Pacific
100 precipitation is projected to shift markedly upwards in SST_{rel} space, while the other two basins
101 exhibit moderate changes. The inter-basin differences in precipitation changes were recently
102 attributed to the thermodynamic intensification of boundary-layer moisture transport (He et al.,
103 2024). However, much of the changes in precipitation in SST_{rel} space appear to be associated with
104 changes in the basin mean precipitation. If we divide precipitation by the basin mean precipitation,
105 which we refer to as relative precipitation (P^*), P^* appears largely constant within each basin (Fig.
106 1d). Therefore, we hypothesize that the relationship between P^* and SST_{rel} does not change under
107 warming. If valid, this would allow us to derive the sensitivity of P^* to local SST_{rel} changes based
108 on the present-day SST_{rel} - P^* slope.

109 We will test the hypothesis by deriving an SST-based model of present-day and future
110 precipitation. This was often done by fitting precipitation to some nonlinear function of SST (e.g.,
111 Good et al., 2020; He et al., 2018; Neelin & Held, 1987). However, precipitation is affected by not
112 only the amplitude but also the spatial gradient of SST (Back & Bretherton, 2009b; Lindzen &
113 Nigam, 1987). The latter drives convection by inducing surface wind convergence (SC) and is a

114 dominant driver of future precipitation changes in tropical oceans (Duffy et al., 2020). These
115 processes can be quantified by a 2-mode model where precipitation is expressed as a function of
116 SST and SC (as a proxy for the effect of SST gradients, Back & Bretherton, 2009a; Duffy et al.,
117 2020). Here, we will introduce an upgraded version of the 2-mode model (Section 3). We will then
118 use it to quantify and constrain the sensitivity of P^* to SST_{rel} changes ($\partial P^*/\partial SST_{rel}$) and SST
119 gradient changes ($\partial P^*/\partial SC$, Section 4). We will finally discuss the implications of $\partial P^*/\partial SST_{rel}$
120 and $\partial P^*/\partial SC$ for regional hydrological sensitivity ($\partial P/\partial SST$) and tropical precipitation
121 projections (Section 5).

122

123 **2. Data**

124 We quantify $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ over tropical (20°S-20°N) oceans in both
125 observations and CMIP6 simulations. All datasets are interpolated onto a common 1° by 1°
126 horizontal grid and a 19-level pressure coordinate before they are analyzed. We take monthly mean
127 data but only analyze the seasonally varying climatological means.

128 The observed SST data is a merged product based on the Hadley Centre SST dataset version
129 1 and the National Oceanic and Atmospheric Administration optimum interpolation SST analysis
130 version 2 (Hurrell et al., 2008). The data ranges from 1979 to 2021 and is archived at 1° resolution.
131 To account for the uncertainty in individual precipitation observations, we average three widely
132 used precipitation datasets: 1) the Global Precipitation Climatology Project (GPCP) data version
133 2 from 1979 to 2021 at 2.5° resolution (Adler et al., 2003), 2) the Climate Prediction Center Merged
134 Analysis of Precipitation (CMAP) data from 1979 to 2021 at 2.5° resolution (P. Xie & Arkin, 1997),
135 and 3) the Tropical Rainfall Measuring Mission Project (TRMM) 3B43 data version 7 from 1998

136 to 2019 at 0.25° resolution (Huffman et al., 2010). While the results presented in this paper are
137 based on the average of the three precipitation observations, our conclusions do not change when
138 individual precipitation datasets are used instead.

139 To quantify the impacts of SST amplitude and SST gradients on the observed precipitation
140 (see Section 3), we use 3D atmospheric variables, including horizontal and vertical winds and dry
141 static energy (calculated from air temperature and geopotential height). These variables are taken
142 from reanalysis data during the period of 1979 to 2021. To minimize the effect of uncertainty
143 within individual datasets, we average three widely used reanalysis datasets: 1) ERA5 (the 5th
144 generation of the European Centre for Medium-Range Weather Forecasts reanalysis) on a 30km
145 horizontal grid and 137 vertical levels (Hersbach et al., 2020), 2) NCEP/DOE-II (the National
146 Center for Environmental Prediction and Department of Energy Reanalysis II) at 2.5° resolution
147 with 17 vertical levels (Kanamitsu et al., 2002), and 3) JRA-55 (the Japanese 55-year Reanalysis)
148 at roughly 1° resolution with 37 vertical levels (KOBAYASHI et al., 2015).

149 We analyze two CMIP6 simulations (Eyring et al., 2016) by drawing the 43 models
150 (Supplementary Table 1) that provide all necessary variables. The historical simulation is driven
151 by historical estimates of radiative forcing and land use. We use the last 30 years (1985-2014) of
152 the historical simulation to evaluate models against observations and to provide a baseline for
153 future changes. The projected future climate is calculated based on the last 30 years (2071-2100)
154 of the ssp585 simulation. ssp585 represents the upper boundary of the range of emission scenarios
155 included in CMIP6, and its radiative forcing reaches 8.5 W/m² by 2100.

156

157 **3. 2-mode model**

158 We apply a 2-mode model to dissect precipitation driven by SST amplitude and SST
159 gradient. The 2-mode model was originally created by Back & Bretherton (2009a). “2-mode”
160 refers to the fact that tropical precipitation is primarily associated with either a shallow or a deep
161 vertical velocity profile (Figs. 1e, f). The shallow mode features maximum updraft in the boundary
162 layer. The bottom-heavy structure is associated with strong boundary layer wind convergence
163 which is driven by low-level pressure gradients that result from the gradients of the underlying
164 SSTs (Back & Bretherton, 2009b; Lindzen & Nigam, 1987). The shallow mode is the main form
165 of precipitation in the Eastern Pacific convergence zone and is closely related to SC. The deep
166 mode peaks in the upper troposphere and can be attributed to atmospheric instability driven by a
167 high amount of near surface moist static energy (Back & Bretherton, 2009a). It is therefore
168 strongest in the warm pool regions but can also be affected by SST gradients, which can increase
169 low-level moist static energy by generating moisture convergence (Duffy et al., 2020). Our 2-mode
170 model largely follows the latest published version from Duffy et al. (2020), but with a few
171 modifications that lead to substantial improvements. We will use the 2-mode model to simulate
172 relative precipitation, which is the constrainable component of tropical precipitation changes (as
173 we will later show). The main steps of the 2-mode model are outlined below. We direct the readers
174 to Back & Bretherton (2009a) and Duffy et al. (2020) for details of the calculation, while pointing
175 out the modifications made herein.

176 Analysis of the atmospheric energy budget reveals that the spatial distribution of tropical
177 precipitation is determined mainly by the column integrated vertical advection of dry static energy
178 (Back & Bretherton, 2009a):

179
$$LP^* = \frac{\langle \omega \frac{\partial s}{\partial p} \rangle}{[P]} + r \quad (1)$$

180 where L is the latent heat of condensation, P is precipitation, P^* is relative precipitation (i.e., P
181 divided by the basin mean precipitation, $[P]$), ω is pressure velocity, s is dry static energy, p is
182 pressure, and $\langle \rangle$ is a pressure weighted vertical integral over an atmospheric column. The residual
183 term (r) is the sum of horizontal advection of s , eddy transport of s , surface sensible heat flux, and
184 the atmospheric radiative cooling (i.e., the difference between surface and top of the atmosphere
185 radiation), all normalized by $[P]$. r has little spatial variation and is roughly equal to 1. We calculate

186 r as the difference between LP^* and $\langle \omega \frac{\partial s}{\partial p} \rangle / [P]$.

187 Equation 1 links precipitation to vertical velocity (ω); the latter is dissected into a deep
188 mode (subscript d) and a shallow mode (subscript s):

$$189 \quad \omega \approx o_d \Omega_d + o_s \Omega_s \quad (2)$$

190 where $\Omega(p)$ describes the vertical profiles of each mode and $o(x,y,t)$ describes the spatial and
191 seasonal variation. The deep and shallow modes are determined based on a linear combination of
192 the first two EOF modes of ω , while ensuring that the shallow mode has zero surface convergence
193 and the deep mode is orthogonal to the shallow mode (Back & Bretherton, 2009a). While in
194 previous 2-mode models, the dissection of the deep and shallow modes is done by using data of
195 the entire tropical oceans, we do it separately for individual basins. This is motivated by the fact
196 that the vertical profiles of ω differ substantially among basins. The Indian (Atlantic) basin has the
197 largest (smallest) peaks in both deep and shallow modes and such differences are more pronounced
198 in reanalysis than the CMIP6 multi-model mean (Figs. 1e, f). The reason for the inter-basin
199 differences is unclear but is likely associated with inter-basin differences in SST, humidity, and
200 land influences (He et al., 2024).

201 Following previous 2-mode models, we also separate r into deep and shallow modes by
202 linear multiple regression:

203
$$r \approx o_d R_d + o_s R_s + R_0 \quad (3)$$

204 where R_d , R_s , and R_0 are constant regression coefficients. While it is unclear how r is physically
 205 linked to o_d and o_s , Equation 3 is calculated solely for the mathematical purpose that both terms
 206 on the rhs of Equation 1 are dissected into deep and shallow modes. Combining Equations 1-3

207 yields the deep and shallow modes of P^* : $LP^* \approx LP_d^* + LP_s^* + R_0$, where $LP_d^* = \left(\langle \Omega_d \frac{\partial s}{\partial p} \rangle / [P] + \right.$
 208 $\left. R_d \right) o_d$ and $LP_s^* = \left(\langle \Omega_s \frac{\partial s}{\partial p} \rangle / [P] + R_s \right) o_s$. Spatial patterns of the deep and shallow precipitation

209 are shown in Supplementary Figure 2.

210 The shallow mode of P^* is related to SST gradients by linear regression: $P_s^* \approx A_s SC + C_s$,
 211 where A_s and C_s are regression coefficients. $SC = -\nabla(u_{925hPa}, v_{925hPa})$, where u_{925hPa} and v_{925hPa}
 212 are 925 hPa horizontal winds. Alternatively, the effect of SST gradients can be estimated by the
 213 Laplacian of SST, but ∇^2 SST is substantially worse at capturing the spatial features of precipitation
 214 compared to SC (Back & Bretherton, 2009a; Duffy et al., 2020).

215 The deep mode of P^* is related to SST amplitude and SST gradients by multiple regression:
 216 $P_d^* \approx b \times \exp(a \times SST_{rel}) + A_d SC + C_d$, where a , b , A_d and C_d are regression coefficients. The
 217 coefficients are determined via a nonlinear least squares analysis based on the trust region method
 218 (Conn et al., 2000). Here, we make two modifications with respect to previous 2-mode models.
 219 First, previous models estimated coefficients (i.e., a , b , A_d , and A_s) by using data of the entire
 220 tropical oceans. This yielded spatially uniform parameters. But as shown in Figures 1c and 1d, the
 221 SST_{rel} - P^* relationship varies substantially among basins, which indicates that the parameters may
 222 be basin dependent. The inter-basin differences in hydrological sensitivity were investigated in He

223 et al. (2024) and were attributed to inter-basin differences in boundary-layer relative humidity. To
224 account for the inter-basin variations, we estimate all coefficients separately for individual basins.

225 Second, previous 2-mode models assumed that the SST_{rel} -driven P_d is zero below a certain
226 convection threshold and grows linearly with SST above the convection threshold. This appears
227 somewhat inconsistent with the actual SST-P relationship, which shows gradual and nonlinear
228 precipitation growth throughout the SST space (Figs. 1a, b). Therefore, we use an exponential
229 function (i.e., $b \times \exp(a \times SST_{rel})$) to represent the SST_{rel} -driven P_d . On the other hand, we are
230 dealing with two SST_{rel} parameters (i.e., a and b). The two parameters both contribute positively
231 to the SST_{rel} -driven P_d but are negatively correlated among models (Fig. 2a). To simplify the
232 interpretation of the parameters, we set b constant while only allowing a to vary among models.
233 Specifically, we estimate both a and b for the observations. But for CMIP6 models, b is prescribed
234 for each basin as the observed values for both present-day and future simulations. The reason for
235 making a (instead of b) the effective SST_{rel} parameter is twofold. First, making a constant across
236 models instead would result in slightly greater root mean squared error (rmse) for the estimated
237 precipitation, suggesting that the inter-model variation in the SST_{rel} - P_d relationship is more
238 associated with a . Second, our choice is consistent with Good et al. (2020) who also used an
239 exponential function to describe the SST-driven precipitation and proposed that precipitation
240 sensitivity to SST should be represented by the coefficient within the exponent. Nevertheless,
241 whether a or b is made the effective SST_{rel} parameter does not affect our conclusions.

242 The above modifications result in substantial improvements in the 2-mode model (Figs.
243 3a-d). The rmse for the estimated observed precipitation is 0.89 mm/day, compared to the rmse of
244 2.30 mm/day in Back & Bretherton (2009a) and 2.08 mm/day in Duffy et al. (2020). The
245 improvement is almost entirely due to the incorporation of the inter-basin differences in Ω profiles

246 and sensitivity parameters. If the inter-basin variations are ignored, the rmse would increase to
247 2.03 mm/day, which is similar to previous versions.

248 The 2-mode model dissects P^* into components driven by SST amplitude and SST
249 gradients (SC):

$$250 \quad P^* \approx P^*(SST) + P^*(SC) + C_d + C_s + R_0/L \quad (4),$$

251 where $P^*(SST) = b \times \exp(a \times SST_{rel})$, and $P^*(SC) = (A_d + A_s)SC$. As shown in Figures 3e-h,
252 spatial variations in tropical precipitation are more associated with SC than SST_{rel} . Particularly in
253 the Atlantic basin, the impact of SST_{rel} is very small. This is likely because the Atlantic basin is
254 colder than the other two basins and the effect of SST amplitude only becomes significant at high
255 SSTs (He et al., 2018).

256 The 2-mode model captures the CMIP6 multi-model mean P^* changes reasonably well
257 (Figs. 4a, b). The most notable inconsistencies appear in the Equatorial regions, which is also an
258 issue for the previous 2-mode model (Fig. 2 of Duffy et al., 2020). The multi-model mean rmse
259 for the estimated precipitation changes is brought down to 0.49 mm/day compared to the 0.62
260 mm/day of Duffy et al. (2020). Consistent with Duffy et al. (2020), SC plays a substantially greater
261 role in the projected tropical precipitation changes than SST_{rel} (Figs. 4c, d). Note that Duffy et al.
262 (2020) attributed a portion of precipitation changes to the “wet-get-wetter” effect (their Fig. 2d),
263 which is absent here because we only consider changes in P^* rather than P .

264

265 **4. Regional precipitation sensitivity to anthropogenic SST_{rel} and SC changes**

266 The present-day and future parameters are not only highly correlated among GCMs but are
267 also similar in amplitude (Figs. 3b, c). Parameter a tends to be slightly lower at present-day, while
268 parameter A ($A = A_d + A_s$) is somewhat higher at present-day. Nevertheless, the differences

269 between present-day and future parameters are substantially smaller than the parameters
270 themselves. In Figure 4e, we estimate P* changes by the present-day parameters to calculate P* in
271 both historical and ssp585 simulations. The resulting P* changes are very similar to those in Figure
272 4b. This means that the present-day and future P* can be represented by the same 2-mode model
273 with only differences in SST_{rel} and SC . This confirms our hypothesis that the SST_{rel} -P* and SC -P*
274 relationships are essentially constant during climate change, while changes in P* are mainly
275 associated with the geographic reshuffling of SST_{rel} and SC . To further confirm this point, we show
276 that P* changes little in SST_{rel} - SC space (Supplementary Figure 3).

277 Because the present-day and future parameters are roughly the same, we can obtain P*
278 sensitivity to local SST_{rel} and SC changes by calculating the SST_{rel} and SC derivatives of Equation
279 4: $\partial P^* / \partial SST_{rel} = ab \times \exp(a \times SST_{rel})$, and $\partial P^* / \partial SC = A$.

280 Because we hold parameter b constant across models, $\partial P^* / \partial SST_{rel}$ is a function of a and
281 SST_{rel} . By comparing a of GCMs and observations, we find that $\partial P^* / \partial SST_{rel}$ is underestimated
282 by most GCMs (Fig. 2b). This is consistent with Good et al. (2020), who reported systematic
283 underestimations of precipitation sensitivity to internal and seasonal SST variations by CMIP
284 models. In addition, there is substantial inter-model variation in a . The uncertainty in a has greater
285 impacts on $\partial P^* / \partial SST_{rel}$ at higher SSTs. For example, the Pacific $\partial P^* / \partial SST_{rel}$ varies by a factor
286 of 1.7 among GCMs for $SST_{rel}=0$ and a factor of 3.4 for $SST_{rel}=2^\circ\text{C}$ (equivalent to present-day
287 SST of roughly 29°C).

288 The observational estimate of $\partial P^* / \partial SC$ is well represented by the CMIP6 multi-model
289 mean (Fig. 2c). While there are no systematic biases in $\partial P^* / \partial SC$, there is considerable inter-model

290 variance. $\partial P^*/\partial SC$ varies by a factor of 2.1, 2.2, and 2.8 for the Indian, Pacific, and Atlantic basin,
291 respectively.

292 How does biases and uncertainties in $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ affect the projection of
293 tropical precipitation? Because the multi-model mean $\partial P^*/\partial SC$ biases are small and because most
294 of the P* changes are associated with SC, the multi-model mean P* changes are not much affected
295 by biases in $\partial P^*/\partial SST_{rel}$. In Figure 4f, we estimate P* changes by using observational parameters
296 and found very similar results to those estimated with GCMs' historical parameters (Fig. 4e). To
297 assess how inter-model variations in $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ affect P* changes, we recalculate
298 the multi-model mean P* changes in the 2-mode model by using parameters from GCMs with the
299 lowest and highest $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ (Figs. 4g-j). While the impact of inter-model
300 variations in $\partial P^*/\partial SST_{rel}$ appears moderate, that of $\partial P^*/\partial SC$ is substantially greater. The impact
301 of $\partial P^*/\partial SC$ can also be appreciated by comparing P* changes in individual GCMs, as models with
302 the highest $\partial P^*/\partial SC$ project substantially more spatially varying P* changes (Supplementary
303 Figure 4). These results suggest that constraining $\partial P^*/\partial SC$ should help greatly to reduce the
304 uncertainty in tropical precipitation changes.

305

306 5. Discussions

307 $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ are quantitatively linked to regional hydrological sensitivity
308 (i.e., $\partial P/\partial SST$). Knowing $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$, one can easily obtain ∂P and then
309 $\partial P/\partial SST$, if [P] and changes in surface conditions (i.e., ∂SST and ∂SC) are also known.

310 (Uncertainties in $[P]$ contribute little to the uncertainty in regional precipitation changes as
311 demonstrated in Supplementary Figures 1c, d.) On the other hand, a separate discussion of
312 $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ is helpful for the physical interpretation of regional hydrological
313 sensitivity. The traditionally defined hydrological sensitivity interprets regional precipitation
314 changes as responses to changes in local SST amplitude (i.e., $\partial P = \partial P/\partial SST \times \partial SST$). However,
315 this can be misleading because regional precipitation changes over tropical oceans are primarily
316 driven by ∂SC , which are associated with SST gradients rather than the amplitude of local SSTs.

317 In the 2-mode model, the SST-driven and SC-driven P_d is estimated by multiple nonlinear
318 regression. This can be potentially problematic because SST_{rel} and SC are not entirely independent
319 (with a spatial correlation of 0.6 in observations and reanalysis). Therefore, the effects of SST
320 amplitude and SST gradients may not be cleanly separated by statistical methods. The 2-mode
321 model partially addresses the problem by only allowing it to affect the attribution of the deep mode,
322 while the shallow mode is attributed to SC only.

323 However, our conclusion that regional hydrological sensitivity is mainly associated with
324 $\partial P^*/\partial SC$ rather than $\partial P^*/\partial SST_{rel}$ is consistent with dynamical considerations. He et al. (2024)
325 showed that tropical precipitation changes are determined by changes in boundary layer moist
326 static energy, which are a function of ∂SST and changes in boundary layer relative humidity ($\partial RH0$).
327 Therefore, regional hydrological sensitivity ($\partial P/\partial SST$) is primarily set by $\partial RH0$; the latter results
328 from changes in boundary layer moisture transport driven by ∂SC (Supplementary Fig. 5, modified
329 from He et al. 2024).

330 We derive constraints on $\partial P^*/\partial SST_{rel}$ and $\partial P^*/\partial SC$ based on the finding that the
331 relationship between P^* and SST_{rel} and that between P^* and SST gradients remain approximately

332 the same in a warm climate. This means that changes in SST geographically reshuffles P^* , while
333 the sensitivity of P^* to SST_{rel} and SST gradient changes is determined by the climatological SST-
334 precipitation relationship of each basin. Therefore, efforts to constrain regional hydrological
335 sensitivity should focus on improving models' present-day SST-precipitation and SC-precipitation
336 relationships.

337

338

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354

355

356 **Open Research**

357 All observational and reanalysis data and the CMIP6 outputs used in this paper are
358 publicly available at the following websites. CMIP6: <https://esgf-node.llnl.gov/projects/cmip6/>.
359 GPCP: <https://psl.noaa.gov/data/gridded/data.gpcp.html>. CMAP:
360 <https://www.psl.noaa.gov//data/gridded/data.cmap.html>. TRMM:
361 https://disc.gsfc.nasa.gov/datasets/TRMM_3B43_7/summary. ERA5:
362 [https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means?tab=form)
363 [means?tab=form](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means?tab=form). NCEP/DOE-II: <https://psl.noaa.gov/data/gridded/data.ncep.reanalysis2.html>.
364 JRA-55: https://jra.kishou.go.jp/JRA-55/index_en.html. Scripts used to analyze data and
365 generate plots are stored in the Zenodo online repository at <https://zenodo.org/records/10840557>.

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368 **References**

369 Adler, R. F., Huffman, G. J., Chang, A., Ferraro, R., Xie, P.-P., Janowiak, J., et al. (2003). The
370 Version-2 Global Precipitation Climatology Project (GPCP) Monthly Precipitation Analysis
371 (1979–Present). *Journal of Hydrometeorology*, 4(6), 1147–1167.
372 [https://doi.org/10.1175/1525-7541\(2003\)004<1147:TVGPCP>2.0.CO;2](https://doi.org/10.1175/1525-7541(2003)004<1147:TVGPCP>2.0.CO;2)

373 Back, L. E., & Bretherton, C. S. (2009a). A simple model of climatological rainfall and vertical
374 motion patterns over the tropical oceans. *Journal of Climate*, 22(23), 6477–6497.

375 Back, L. E., & Bretherton, C. S. (2009b). On the Relationship between SST Gradients, Boundary
376 Layer Winds, and Convergence over the Tropical Oceans. *Journal of Climate*, 22(15),
377 4182–4196. <https://doi.org/10.1175/2009JCLI2392.1>

378 Chadwick, R. (2016). Which Aspects of CO₂ Forcing and SST Warming Cause Most Uncertainty in
379 Projections of Tropical Rainfall Change over Land and Ocean? *Journal of Climate*, 29(7),
380 2493–2509. <https://doi.org/10.1175/JCLI-D-15-0777.1>

381 Chen, X., Zhou, T., Wu, P., Guo, Z., & Wang, M. (2020). Emergent constraints on future
382 projections of the western North Pacific Subtropical High. *Nature Communications*,
383 11(1), 2802.

384 Conn, A. R., Gould, N. I., & Toint, P. L. (2000). *Trust region methods*. SIAM.

385 DeAngelis, A. M., Qu, X., Zelinka, M. D., & Hall, A. (2015). An observational radiative constraint
386 on hydrologic cycle intensification. *Nature*, 528(7581), 249–253.
387 <https://doi.org/10.1038/nature15770>

388 Duffy, M. L., O’Gorman, P. A., & Back, L. E. (2020). Importance of Laplacian of Low-Level
389 Warming for the Response of Precipitation to Climate Change over Tropical Oceans.
390 *Journal of Climate*, 33(10), 4403–4417. <https://doi.org/10.1175/JCLI-D-19-0365.1>

391 Eyring, V., Bony, S., Meehl, G. A., Senior, C. A., Stevens, B., Stouffer, R. J., & Taylor, K. E. (2016).
392 Overview of the Coupled Model Intercomparison Project Phase 6 (CMIP6) experimental
393 design and organization. *Geoscientific Model Development*, 9(5), 1937–1958.

394 Good, P., Chadwick, R., Holloway, C., Kennedy, J., Lowe, J., Roehrig, R., & Rushley, S. (2020). High
395 sensitivity of tropical precipitation to local sea-surface temperature.

396 Graham, N. E., & Barnett, T. P. (1987). Sea Surface Temperature, Surface Wind Divergence, and
397 Convection over Tropical Oceans. *Science*, 238(4827), 657.
398 <https://doi.org/10.1126/science.238.4827.657>

399 Ham, Y.-G., Kug, J.-S., Choi, J.-Y., Jin, F.-F., & Watanabe, M. (2018). Inverse relationship between
400 present-day tropical precipitation and its sensitivity to greenhouse warming. *Nature*
401 *Climate Change*, 8(1), 64–69. <https://doi.org/10.1038/s41558-017-0033-5>

402 He, J., & Soden, B. J. (2015). Anthropogenic Weakening of the Tropical Circulation: The Relative
403 Roles of Direct CO₂ Forcing and Sea Surface Temperature Change. *Journal of Climate*,
404 28(22), 8728–8742. <https://doi.org/10.1175/JCLI-D-15-0205.1>

405 He, J., Johnson, N. C., Vecchi, G. A., Kirtman, B., Wittenberg, A. T., & Sturm, S. (2018).
406 Precipitation Sensitivity to Local Variations in Tropical Sea Surface Temperature. *Journal*
407 *of Climate*, 31(22), 9225–9238. <https://doi.org/10.1175/JCLI-D-18-0262.1>

408 He, J., Lu, K., Fosu, B., & Fueglistaler, S. (2024). Diverging Hydrological Sensitivity among Tropical
409 Basins. *Nature Climate Change*, Accepted.

410 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz-Sabater, J., et al. (2020).
411 The ERA5 global reanalysis. *Quarterly Journal of the Royal Meteorological Society*,
412 146(730), 1999–2049.

413 Huffman, G. J., Adler, R. F., Bolvin, D. T., & Nelkin, E. J. (2010). The TRMM multi-satellite
414 precipitation analysis (TMPA). In *Satellite rainfall applications for surface hydrology* (pp.
415 3–22). Springer.

416 Hurrell, J. W., Hack, J. J., Shea, D., Caron, J. M., & Rosinski, J. (2008). A new sea surface
417 temperature and sea ice boundary dataset for the community atmosphere model.
418 *Journal of Climate*, 21(19), 5145–5153. <https://doi.org/10.1175/2008JCLI2292.1>

419 Johnson, N. C., & Xie, S.-P. (2010). Changes in the sea surface temperature threshold for tropical
420 convection. *Nature Geosci*, 3(12), 842–845. <https://doi.org/10.1038/ngeo1008>

421 Kanamitsu, M., Ebisuzaki, W., Woollen, J., Yang, S.-K., Hnilo, J., Fiorino, M., & Potter, G. (2002).
422 Ncep–doe amip-ii reanalysis (r-2). *Bulletin of the American Meteorological Society*,
423 83(11), 1631–1644.

424 Kent, C., Chadwick, R., & Rowell, D. P. (2015). Understanding uncertainties in future projections
425 of seasonal tropical precipitation. *Journal of Climate*, 28(11), 4390–4413.
426 <https://doi.org/10.1175/JCLI-D-14-00613.1>

427 KOBAYASHI, S., OTA, Y., HARADA, Y., EBITA, A., MORIYA, M., ONODA, H., et al. (2015). The JRA-55
428 Reanalysis: General Specifications and Basic Characteristics. *気象集誌 第2 輯*, 93(1), 5–
429 48. <https://doi.org/10.2151/jmsj.2015-001>

430 Kramer, R. J., & Soden, B. J. (2016). The sensitivity of the hydrological cycle to internal climate
431 variability versus anthropogenic climate change. *Journal of Climate*, 29(10), 3661–3673.

432 Lau, K.-M., Wu, H.-T., & Bony, S. (1997). The Role of Large-Scale Atmospheric Circulation in the
433 Relationship between Tropical Convection and Sea Surface Temperature. *Journal of*
434 *Climate*, 10(3), 381–392. [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0442(1997)010<0381:TROLSA>2.0.CO;2)
435 [0442\(1997\)010<0381:TROLSA>2.0.CO;2](https://doi.org/10.1175/1520-0442(1997)010<0381:TROLSA>2.0.CO;2)

436 Lindzen, R. S., & Nigam, S. (1987). On the Role of Sea Surface Temperature Gradients in Forcing
437 Low-Level Winds and Convergence in the Tropics. *Journal of the Atmospheric Sciences*,
438 44(17), 2418–2436. [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0469(1987)044<2418:OTROSS>2.0.CO;2)
439 [0469\(1987\)044<2418:OTROSS>2.0.CO;2](https://doi.org/10.1175/1520-0469(1987)044<2418:OTROSS>2.0.CO;2)

440 Lu, K., He, J., & Simpson, I. R. (2023). Origins of uncertainty in the response of the summer
441 north Pacific subtropical high to CO2 forcing. *Geophysical Research Letters*, 50(22),
442 e2023GL105042.

443 Ma, J., & Xie, S.-P. (2013). Regional patterns of sea surface temperature change: a source of
444 uncertainty in future projections of precipitation and atmospheric circulation. *Journal of*
445 *Climate*, 26(8), 2482–2501. <https://doi.org/10.1175/JCLI-D-12-00283.1>

446 McSweeney, C. F., & Jones, R. G. (2013). No consensus on consensus: the challenge of finding a
447 universal approach to measuring and mapping ensemble consistency in GCM
448 projections. *Climatic Change*, 119(3), 617–629. [https://doi.org/10.1007/s10584-013-](https://doi.org/10.1007/s10584-013-0781-9)
449 0781-9

450 Neelin, J. D., & Held, I. M. (1987). Modeling Tropical Convergence Based on the Moist Static
451 Energy Budget. *Monthly Weather Review*, 115(1), 3–12. [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0493(1987)115<0003:MTCBOT>2.0.CO;2)
452 0493(1987)115<0003:MTCBOT>2.0.CO;2

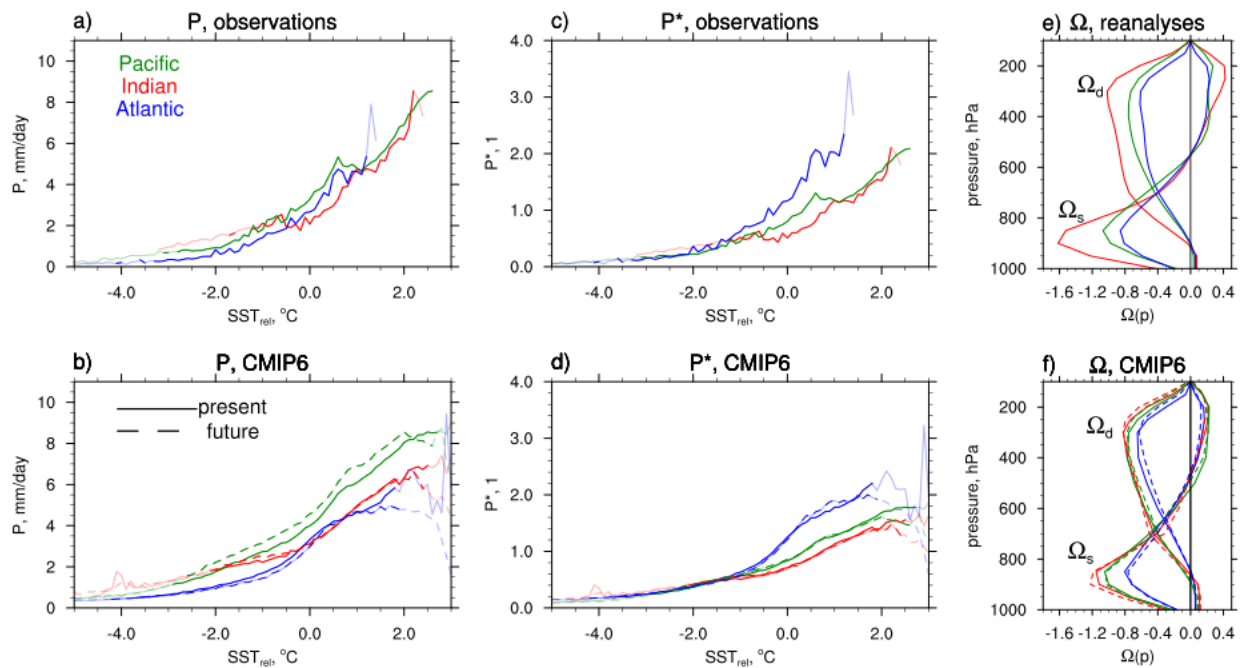
453 Park, I.-H., Yeh, S.-W., Min, S.-K., Ham, Y.-G., & Kirtman, B. P. (2022). Present-day warm pool
454 constrains future tropical precipitation. *Communications Earth & Environment*, 3(1), 310.

455 Su, H., Jiang, J. H., Neelin, J. D., Shen, T. J., Zhai, C., Yue, Q., et al. (2017). Tightening of tropical
456 ascent and high clouds key to precipitation change in a warmer climate. *Nature*
457 *Communications*, 8, 15771.

458 Watanabe, M., Kamae, Y., Shiogama, H., DeAngelis, A. M., & Suzuki, K. (2018). Low clouds link
459 equilibrium climate sensitivity to hydrological sensitivity. *Nature Climate Change*, 8(10),
460 901–906. <https://doi.org/10.1038/s41558-018-0272-0>

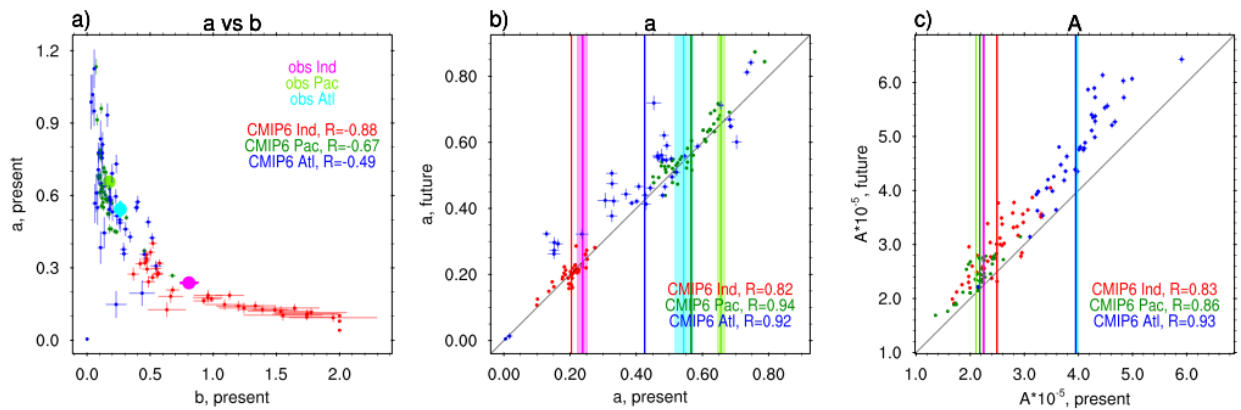
461 Xie, P., & Arkin, P. A. (1997). Global Precipitation: A 17-Year Monthly Analysis Based on Gauge
462 Observations, Satellite Estimates, and Numerical Model Outputs. *Bulletin of the*
463 *American Meteorological Society*, 78(11), 2539–2558. [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0477(1997)078<2539:GPAYMA>2.0.CO;2)
464 0477(1997)078<2539:GPAYMA>2.0.CO;2

465 Xie, S.-P., Deser, C., Vecchi, G. A., Ma, J., Teng, H., & Wittenberg, A. T. (2010). Global Warming
 466 Pattern Formation: Sea Surface Temperature and Rainfall. *Journal of Climate*, 23(4), 966–
 467 986. <https://doi.org/10.1175/2009JCLI3329.1>
 468 Zhang, C. (1993). Large-Scale Variability of Atmospheric Deep Convection in Relation to Sea
 469 Surface Temperature in the Tropics. *Journal of Climate*, 6(10), 1898–1913.
 470 [https://doi.org/10.1175/1520-0442\(1993\)006<1898:LSVOAD>2.0.CO;2](https://doi.org/10.1175/1520-0442(1993)006<1898:LSVOAD>2.0.CO;2)
 471 Zhang, J., & Huang, P. (2023). Different uncertainty in tropical oceanic and land precipitation
 472 sensitivities under global warming. *Atmospheric Research*, 106850.
 473
 474
 475

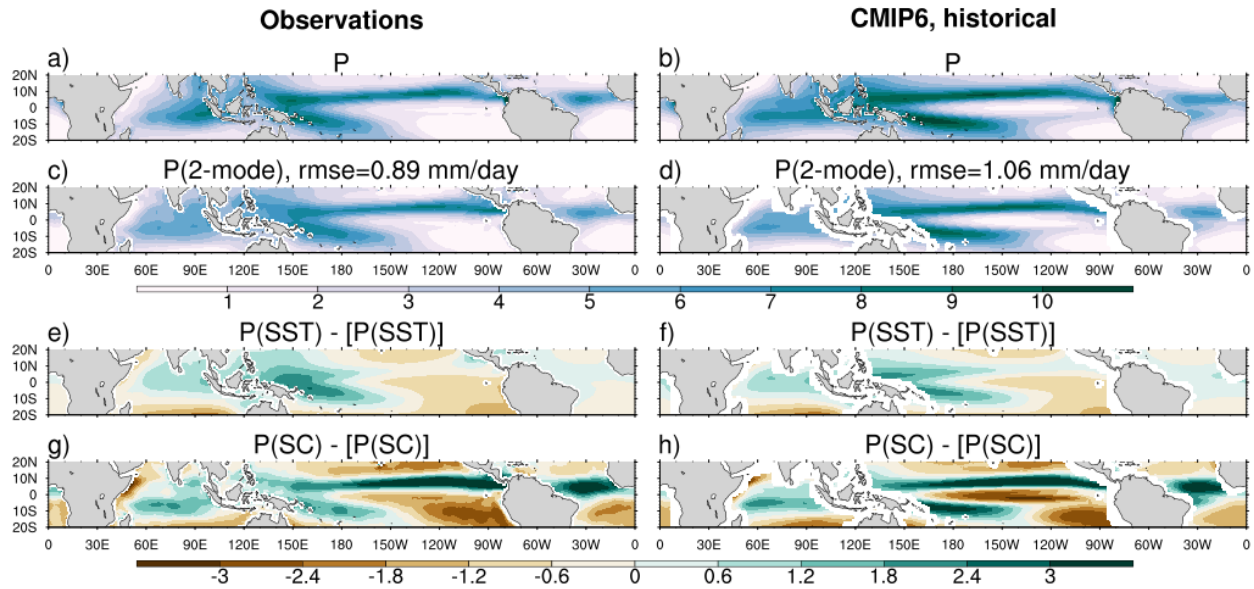


476
 477 **Figure 1.** a-b) Basin precipitation averaged for 0.1 SST_{rel} bins from observations (a) and CMIP6
 478 multi-model mean historical and ssp585 simulations (b). SST_{rel} bins that account for less than 0.5%

479 of the basin area are shown in semitransparent colors. c-d) Same as a-b) but for relative
 480 precipitation. e-f) Vertical profiles of deep and shallow pressure velocity profiles from reanalysis
 481 (e) and CMIP6 multi-model mean historical and ssp585 simulations (f).
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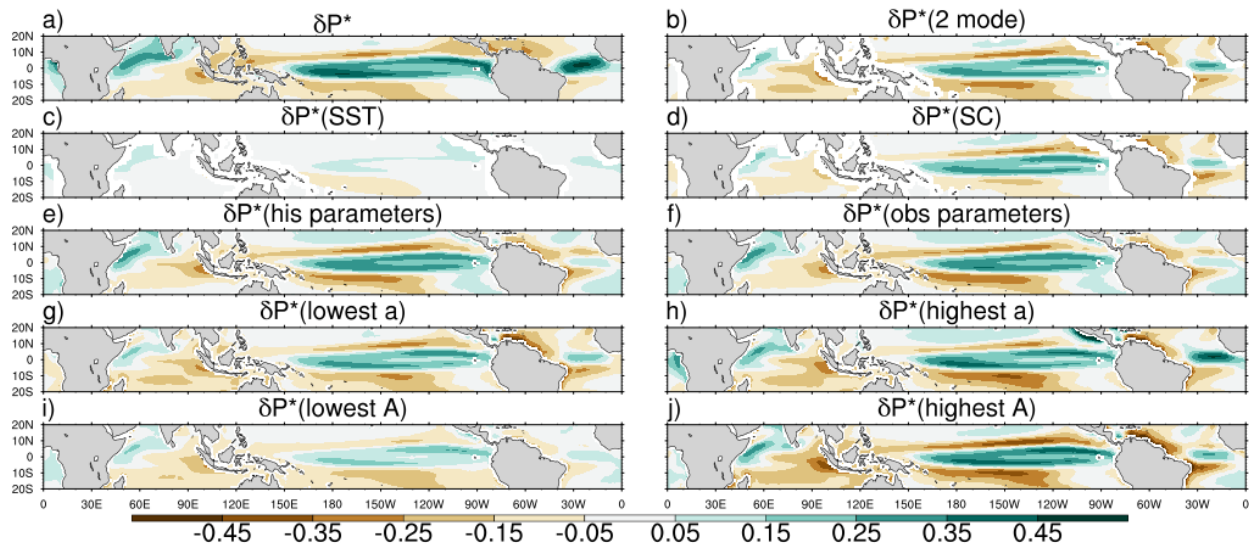
483
 484 **Figure 2.** Relationships between present-day a and b (a), present-day and future a (b), and present-
 485 day and future A (c). Individual GCMs are represented by the small dots, and the vertical lines in
 486 (b) and (c) represent the multi-model mean. Inter-model correlation coefficients are shown by texts.
 487 Observations are represented by the large dots in (a) vertical lines in (b) and (c) in lighter colors.
 488 The 95% uncertainty range is represented by the crosses for the individual GCMs in all panels and
 489 observations in (a) and is represented by the semitransparent shading for the observations in (b)
 490 and (c).
 491



492

493 **Figure 3.** Present-day precipitation (a-b), estimated precipitation by the 2-mode model (c-d), and
 494 SST-driven and SC-driven precipitation (e-h) from the observations (left) and the CMIP6 multi-
 495 model mean (right). The 2-mode model estimates P^* and P is obtained by multiplying P^* by the
 496 observed or GCMs' $[P]$. In (e-h), the basin mean $P(\text{SST})$ and $P(\text{SC})$ are removed in order to
 497 emphasize their spatial variations.

498



499

500 **Figure 4.** a-b) CMIP6 multi-model mean P^* changes from GCMs (a) and the 2-mode model (b).
501 c-d) Multi-model mean P^* changes due to changes in SST (c) and SC (d). e-f) Multi-model mean
502 P^* changes from the 2-mode model by using GCMs' historical parameters (e) and observational
503 parameters (f). g-h) Same as (b) except replacing parameter a of all GCMs with those from GCMs
504 with the lowest a (g) and highest a (h). i-j) Same as (g-h) except for parameter A .