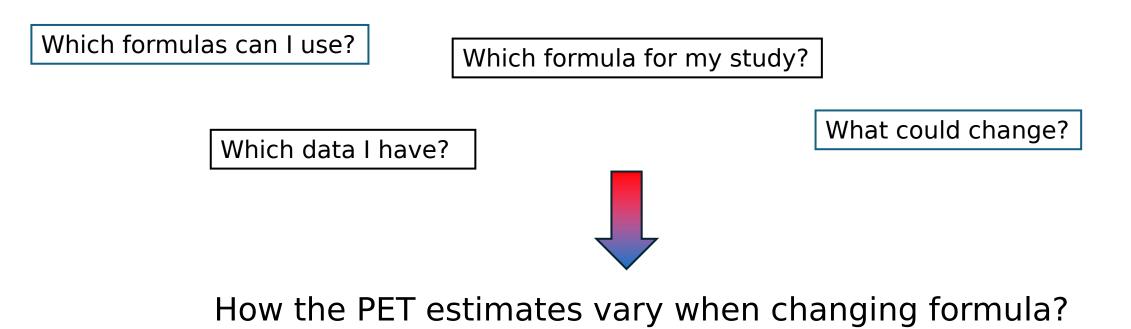


Giovanni Selleri, Mattia Neri, Elena Toth University of Bologna giovanni.selleri4@unibo.it



Which PET formulas for my rainfall-runoff modelling?

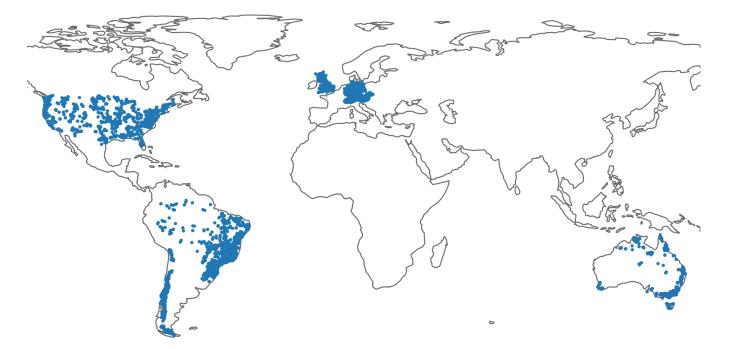
When rainfall-runoff modelling, there is usually the need to estimate PET (Potential Evapo-Transpiration) using a formula



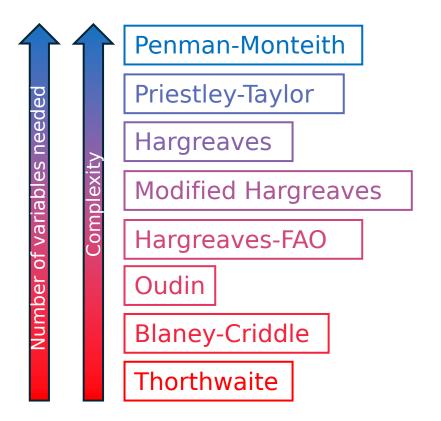


How the PET estimates vary when changing formula?

Caravan: an open source rainfall-runoff dataset



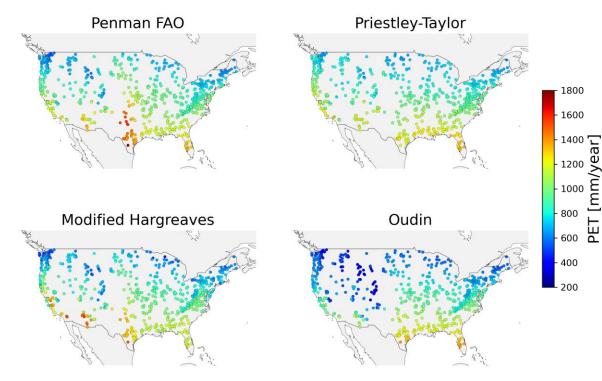
~5000 basins Hydro-meteorological timeseries at catchment scale PET formulas:





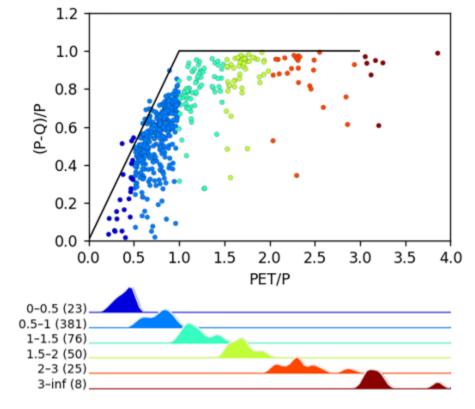
Analysis of PET estimates

Annual long-term average [mm/year]



CAMELS - US

Budyko framework for hydrological consistency



PET/P





Which PET formulas for my rainfall-runoff modelling?



PICO4.4



Giovanni Selleri, Mattia Neri, Elena Toth University of Bologna giovanni.selleri4@unibo.it



ALMA MATER STUDIORUM Università di Bologna



Summary

<u>Objectives</u>

PET formulas & Data

Analysis of PET estimates

<u>Hydrological consistency in Budyko</u>

Conclusions

Supplementary



Which PET formulas for my rainfall-runoff modelling?

Several PET formulas have been proposed to estimate PET at catchment scale

Choosing the formula is usually up to the single researcher, that each time must decide based on the input data available and their personal preferences

Our objectives are:

- Comparing the PET estimates at catchment scale
- Checking their hydrological consistency in the Budyko framework



PET formulas & Data

Formulas use meteorological data to estimate PET

The choice of the formula depends on data availability

We chose the data necessary for the Penman-Monteith formula (FAO version), which combines energy and mass balance (used as benchmark)

We selected other seven PET formulas among the most used in literature, which are less datademanding, down to a simple temperature-based equation

PET formulas: description

Penman FAO	Combines the energy balance and the mass transfer	(R _{solar} , R _{th} , T _{avg} , T _{max} , T _{min} , T _{dew} , Wind, Pressure)				
Priestley Taylor	Radiation based	(R _{solar} , R _{th} , T _{avg})				
Hargreaves	Radiation is estimated with latitude, and the difference Tmax- Tmin is used as proxy for the atmospheric turbidity	(T _{avg} , T _{max} , T _{min} , Latitude)				
Modified Hargreaves	The contribution of monthly precipitation is added to the calculation of turbidity	(T _{avg} , T _{max} , T _{min} , Precipitation, Latitude)				
Hargreaves-FAO*	The atmospheric turbidity term range is limited	(T _{avg} , T _{max} , T _{min} , Latitude)				
Oudin	Empirical based on temperature	(T _{avg} , Latitude)				
Blaney-Criddle*	Empirical based on temperature, elevation and daily light hours	(T _{avg} , Latitude, Elevation)				
Thorthwaite	Empirical based on temperature	(T _{avg})				

* Results not showed here for sake of brevity

interactive discussion



PET formulas: necessary variables

Penman FAO	Net solar radiation	Net thermal radiation	Tmean	Tmax	Tmin	Tdew	Wind speed	Pressure		
Priestley Taylor	Net solar radiation	Net thermal radiation	Tmean							
Hargreaves			Tmean	Tmax	Tmin					Latitude
Modified Hargreaves			Tmean	Tmax	Tmin				Precipitation	Latitude
Hargreaves-FAO*			Tmean	Tmax	Tmin					Latitude
Oudin			Tmean							Latitude
Blaney-Criddle*			Tmean							Latitude
Thorthwaite			Tmean							



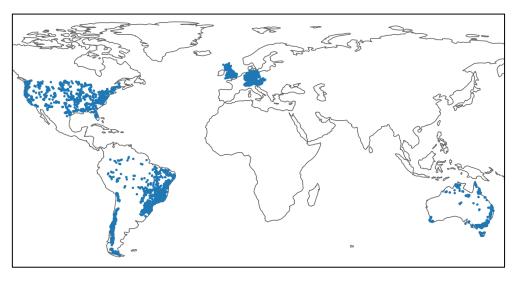
PET formulas & Data

Caravan: an open source rainfall-runoff dataset (Kratzert et al., 2023) https://github.com/kratzert/Caravan

Caravan contains hydro-meteorological daily timeseries at catchment scale:

- Streamflow observations from other large-sample datasets (CAMELS initiative)
- Meteorological timeseries derived from ERA5-Land reanalisys







PET formulas & Data

The time period of daily meteorological variables is 1951-2023

The interval of daily streamflow observations depends on the source dataset, most of the data are in the period 1981-2014

We selected \sim 5000 basins in Caravan:

Caravan region	Number of basins				
US	671				
Brazil	870				
Chile	505				
UK	671				
Australia	222				
Germany	1887				
Switzerland	269				



Analysis PET estimates

Distribution of PET annual average by formulas

Map of PET annual average

Map of the PET relative annual average (w.r.t. Penman FAO benchmark formula)

<u>Map of PET long term variability throughout the year</u>

Map of Aridity Index



PET annual average [mm/year] distribution

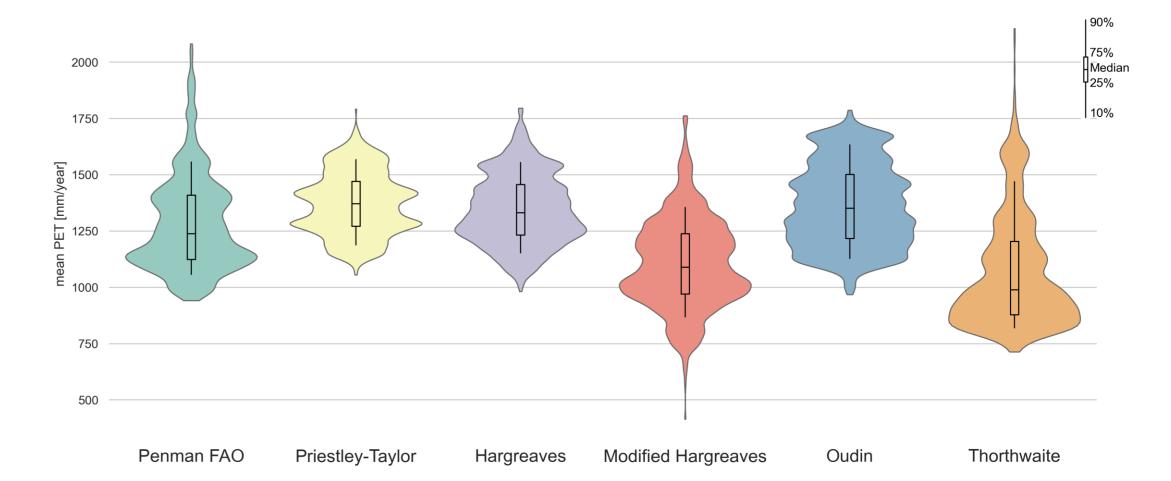
CAMELS - US





PET annual average [mm/year] distribution

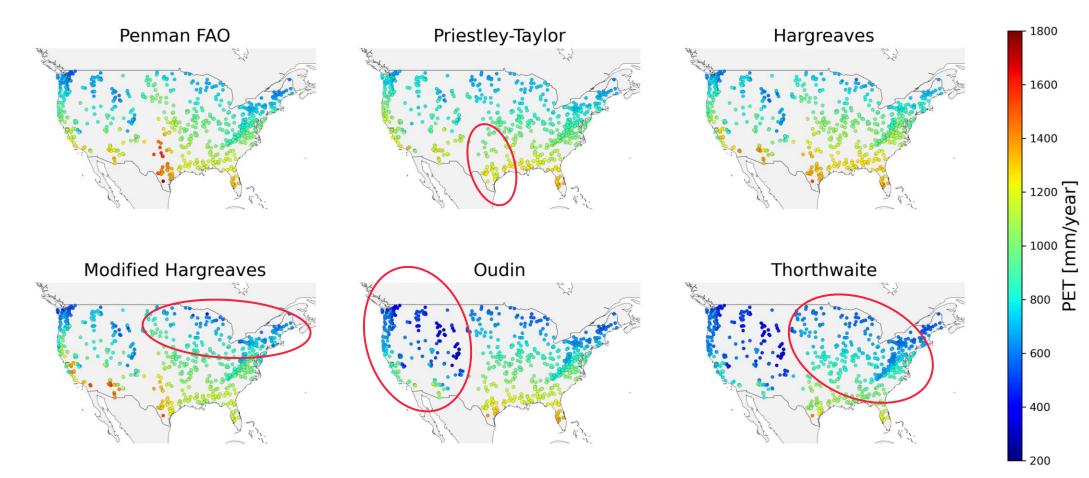
CAMELSBR - Brazil





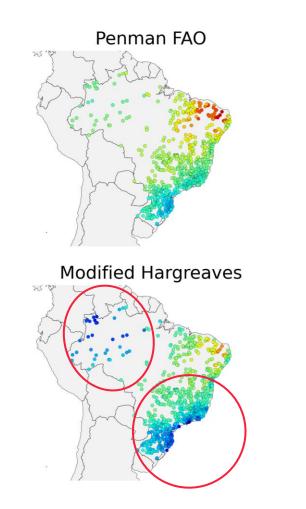
PET annual average [mm/year]

CAMELS - US

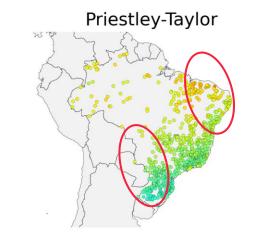




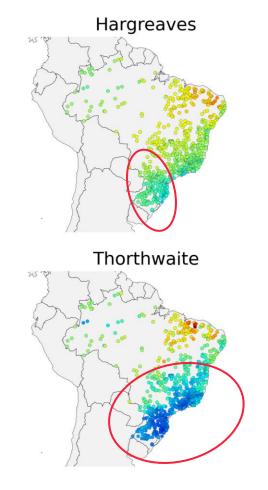
PET annual average [mm/year]

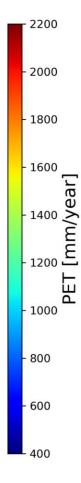


CAMELSBR - Brazil



Oudin





interactive discussion

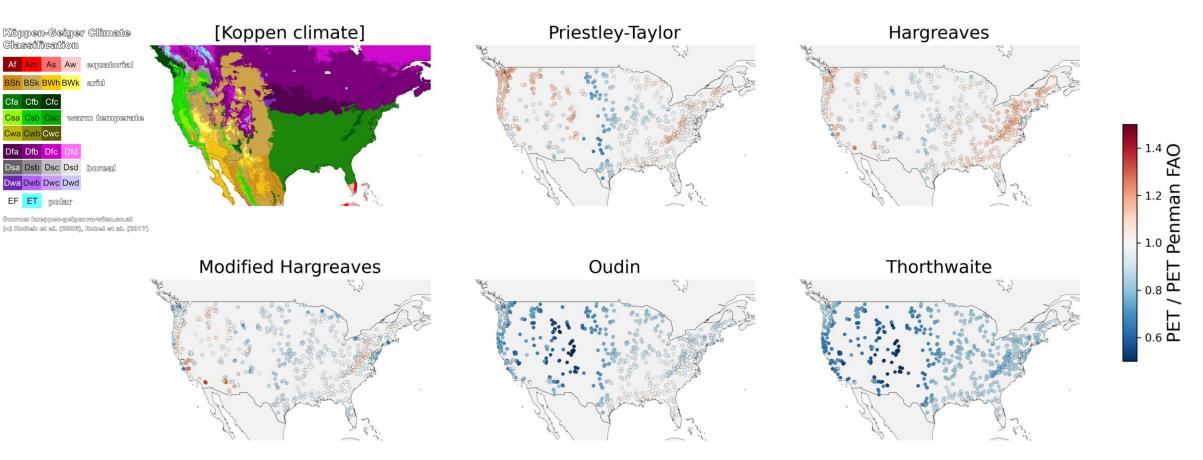
PET relative annual average

PET formula i PET Penman FAO





CAMELS - US



interactive discussion

PET relative annual average

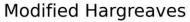
PET formula i PET Penman FAO





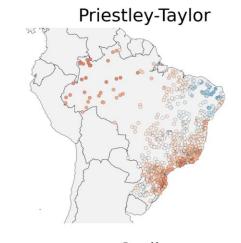
Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)







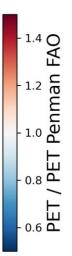
CAMELSBR - Brazil









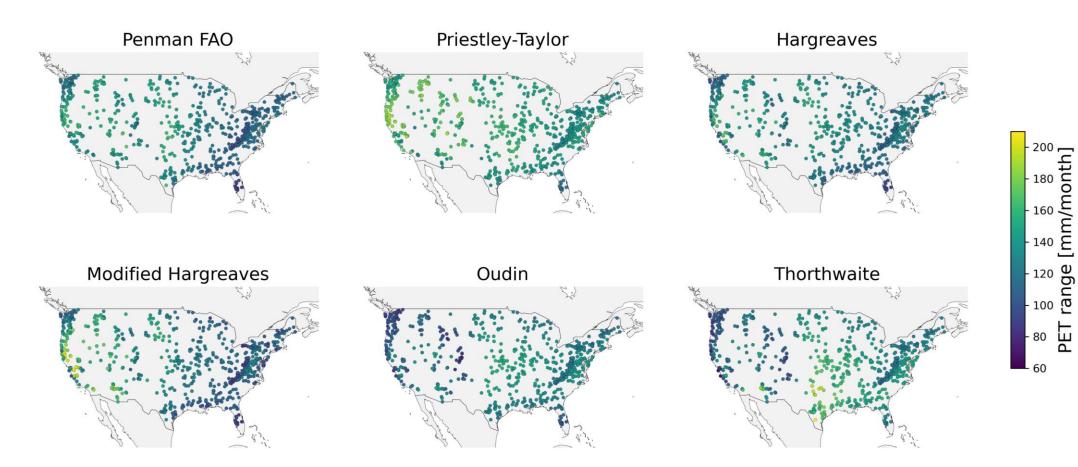




PET long term variability throughout the year

 $\max(PET_{monthly \, long \, term \, average}) - \min(PET_{monthly \, long \, term \, average}) \left[\frac{mm}{month}\right]$

CAMELS - US





PET long term variability throughout the year

 $\max(PET_{monthly \ long \ term \ average}) - \min(PET_{monthly \ long \ term \ average}) \left[\frac{mm}{monthl}\right]$



Modified Hargreaves



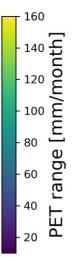
CAMELSBR - Brazil







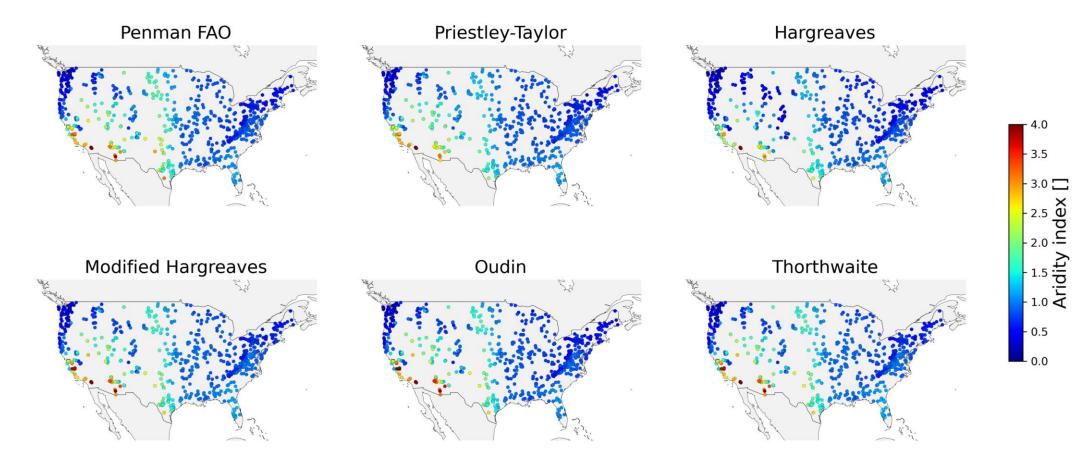




Aridity index $\frac{PET}{P}$





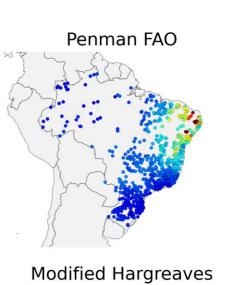


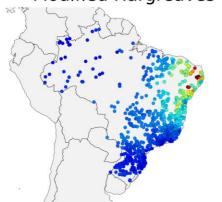
interactive discussion

Aridity index $\frac{PET}{P}$

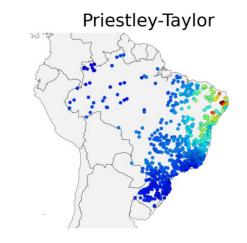




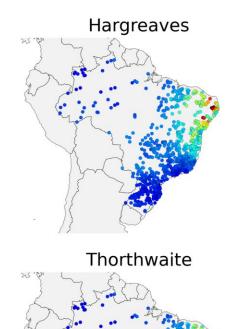


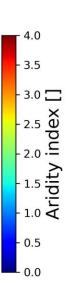


CAMELSBR - Brazil



Oudin







Hydrological consistency of PET

The Budyko space conceptually represents the coupled long-term water and energy balance (Budyko, 1974)

Catchment are scattered in a diagram using two dimensionless ratios:

- PET/Precipitation
- (Precipitation-Streamflow)/Precipitation

The assumption is no changes in water storages, therefore requiring multiyear averages

In the Budyko diagram we show also the distribution of aridity index (PET/Precipitation) and how it changes for different formulas



Hydrological consistency of PET

Data for Budyko:

Caravan provides daily observations of streamflow

For some catchments the timeseries is not continuous

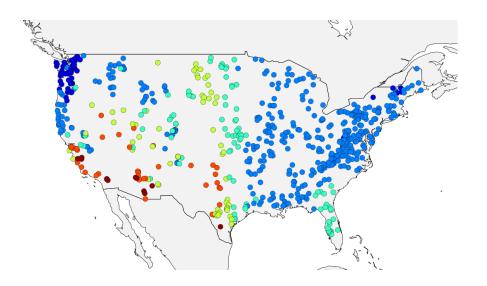
We filtered again the basins in Caravan, keeping only the ones with at least 30 full years of daily streamflow data available (\sim 3500 basins)



Budyko space

Colors of catchments in the plot are defined by the aridity index from Penman FAO

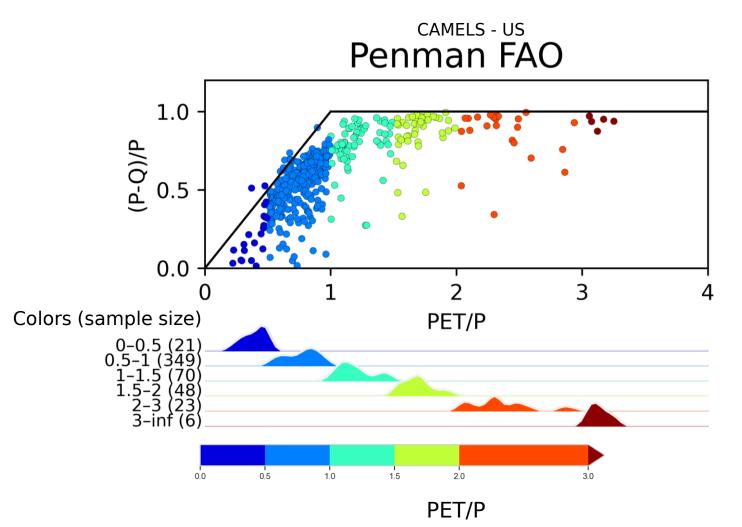
CAMELS - US Penman FAO 1.0 d/(D-d) 0.0 3 () PET/P 0.0 0.5 1.0 2.0 1.5 3.0 PET/P





Budyko space

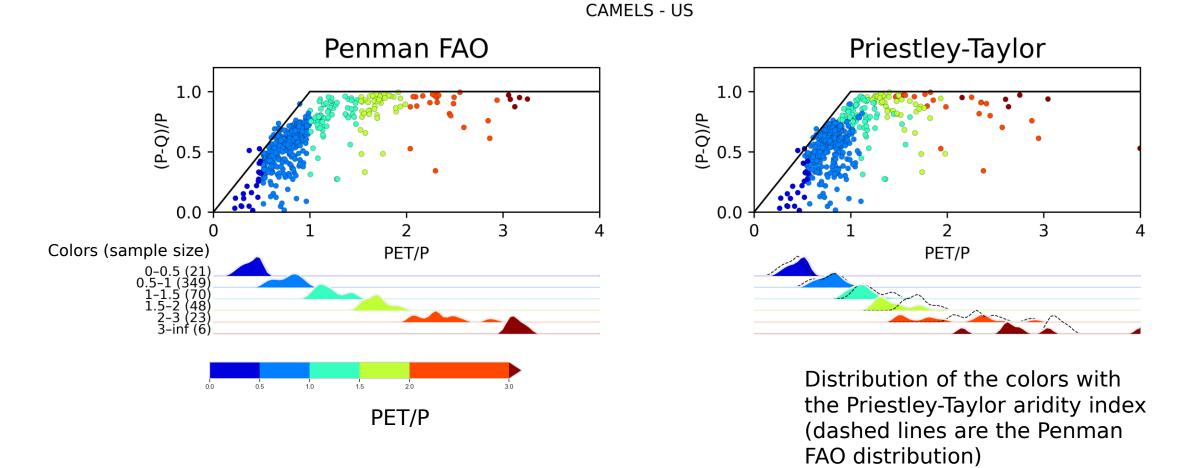
Colors of catchments in the plot are defined by the aridity index from Penman FAO





Budyko space

Colors of catchments in the plot are defined by he aridity index from Penman FAO

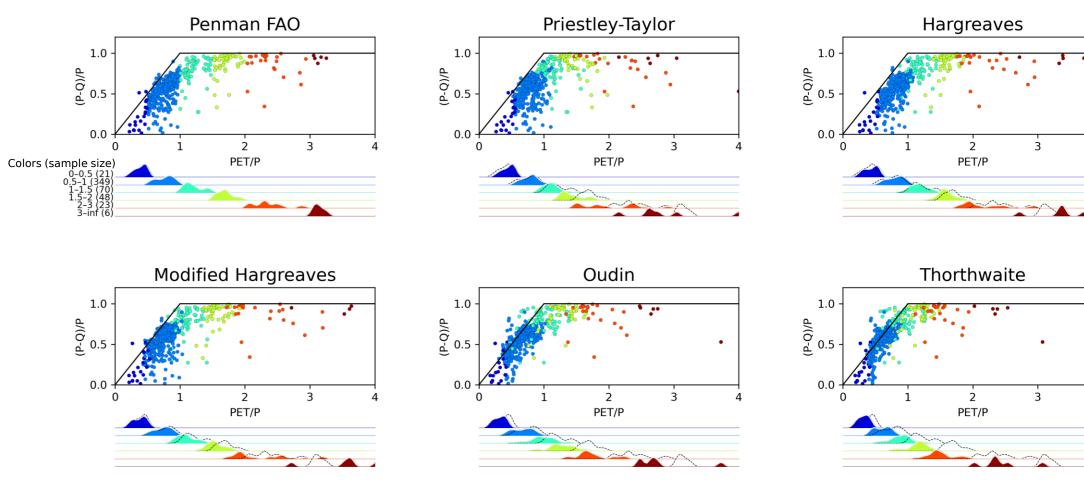




Δ

Budyko space

Colors of catchments in the plot are defined by the aridity index from Penman FAO



CAMELS - US

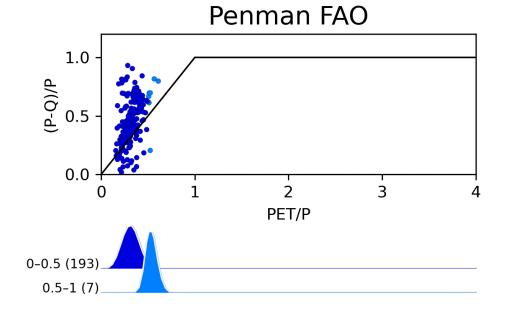


Limits of ERA5-Land data?

The ERA5-Land precipitation provided in Caravan differ from observation-based products, resulting in significantly lower efficiency in hydrological modelling (Clerc-Schwarzenbach et al., 2024)

Difference in precipitation can affect the positioning of catchments in the Budyko space

Budyko plots of European catchments (UK, Germany and Switzerland) show potential effects of this precipitation bias



CAMELSCH - Switzerland



Conclusions

PET estimates have significant variations changing formulas: such variation is not uniform among the same regions and across different countries.

Considering as benchmark the Penman-Monteith FAO, different formula are the best performing in different regions.

Aridity index estimation - and consequently the Budyko plot position - is strongly affected by the formula choice, especially for water-limited catchments.

Caravan precipitation (ERA5-Land data) are known to have issues (Clerc-Schwarzenbach et al., 2024) and this affects the Budyko analysis.

supplementary



Supplementary

PET annual average distribution

PET annual average

PET relative annual average

PET long term variability throughout the year

Aridity index

Budyko space

PET formulas

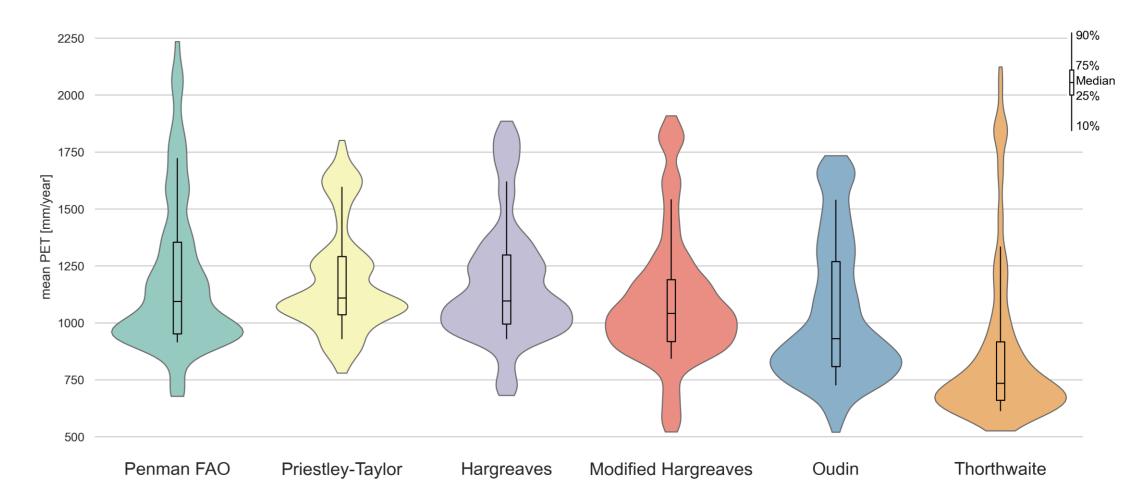


CAMELS - US





CAMELSAUS - Australia



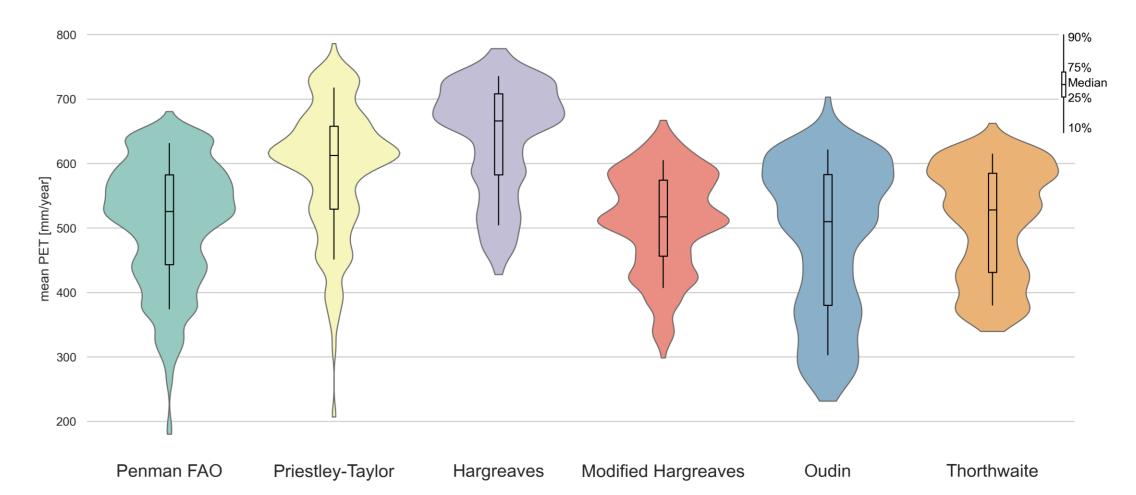


CAMELSBR - Brazil



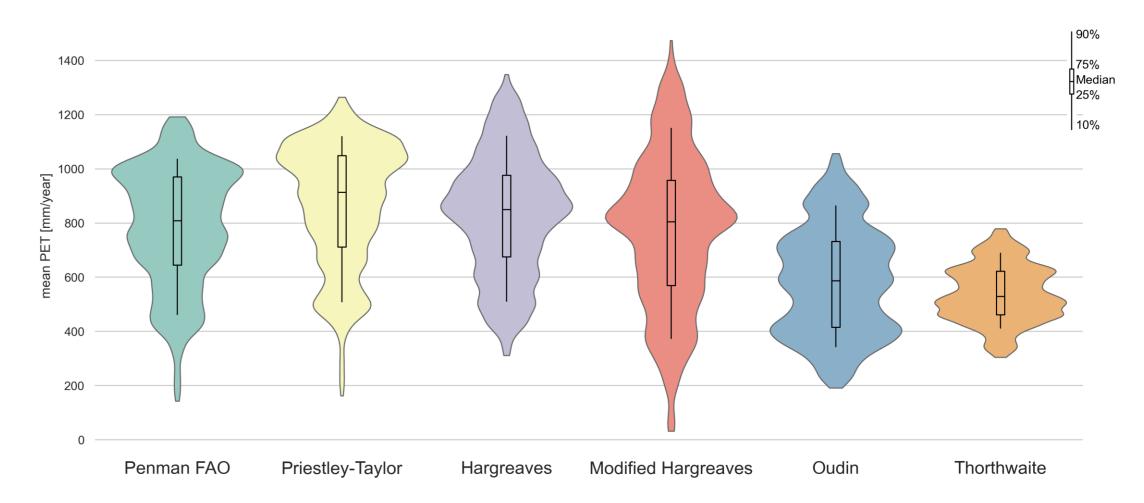


CAMELSCH - Switzerland





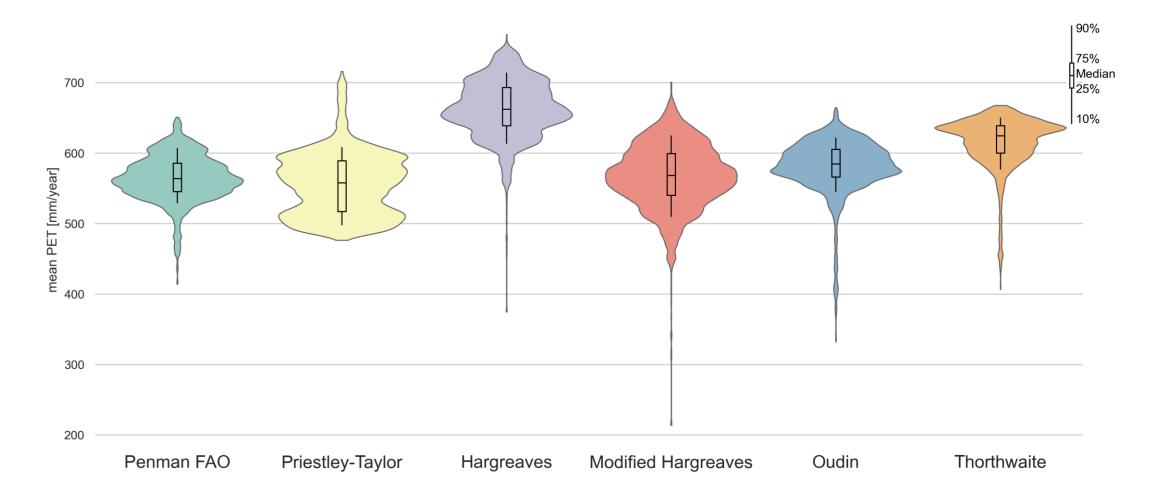
CAMELSCL - Chile





PET annual average distribution

CAMELSDE - Germany





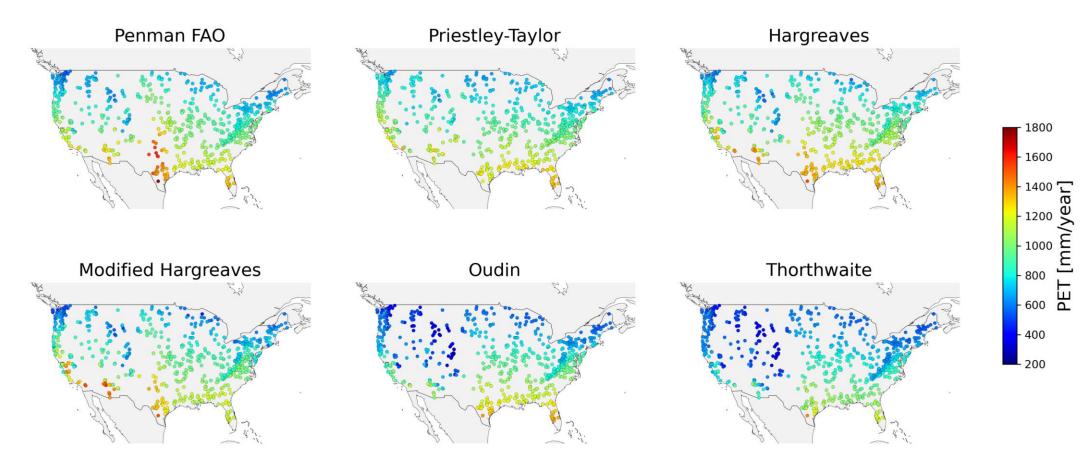
PET annual average distribution

CAMELSGB - UK





PET annual average



CAMELS - US

- 2200 - 2000 - 1800 **Luc**

- 1600

- 1400

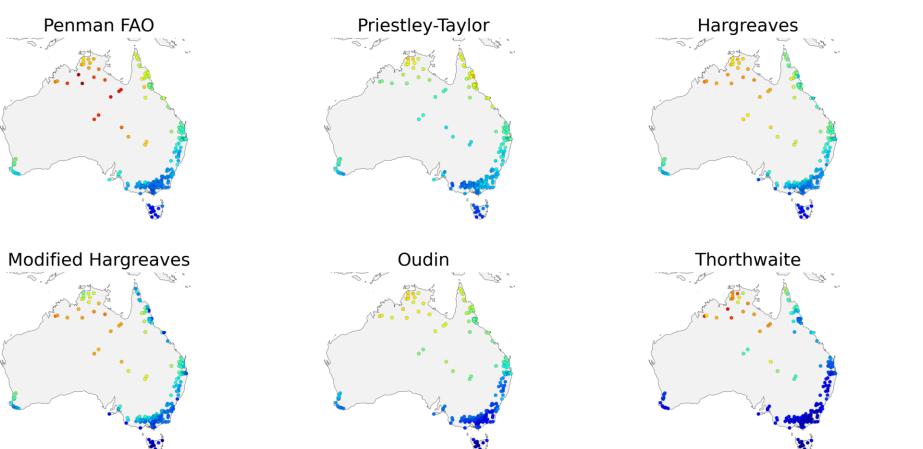
E 1200

- 1000 Ц

- 800 - 600 E



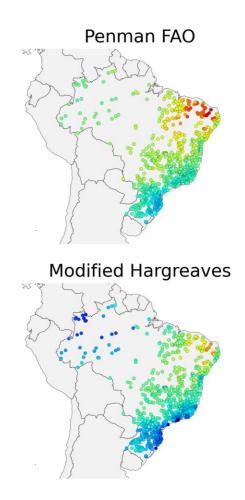
PET annual average



CAMELSAUS - Australia



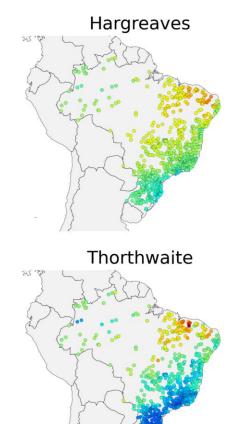
PET annual average

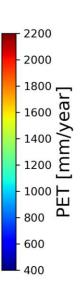


CAMELSBR - Brazil



Oudin



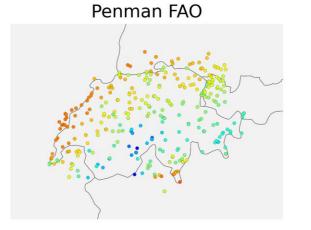




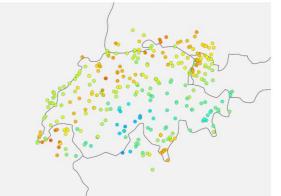
PET annual average

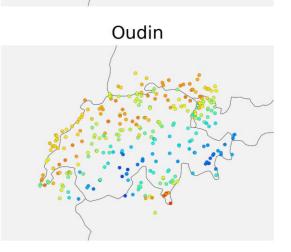
CAMELSCH - Switzerland

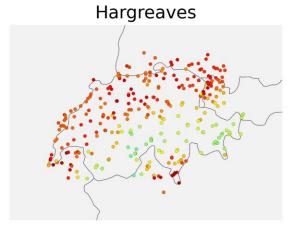
Priestley-Taylor



Modified Hargreaves

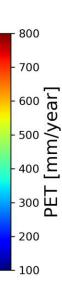






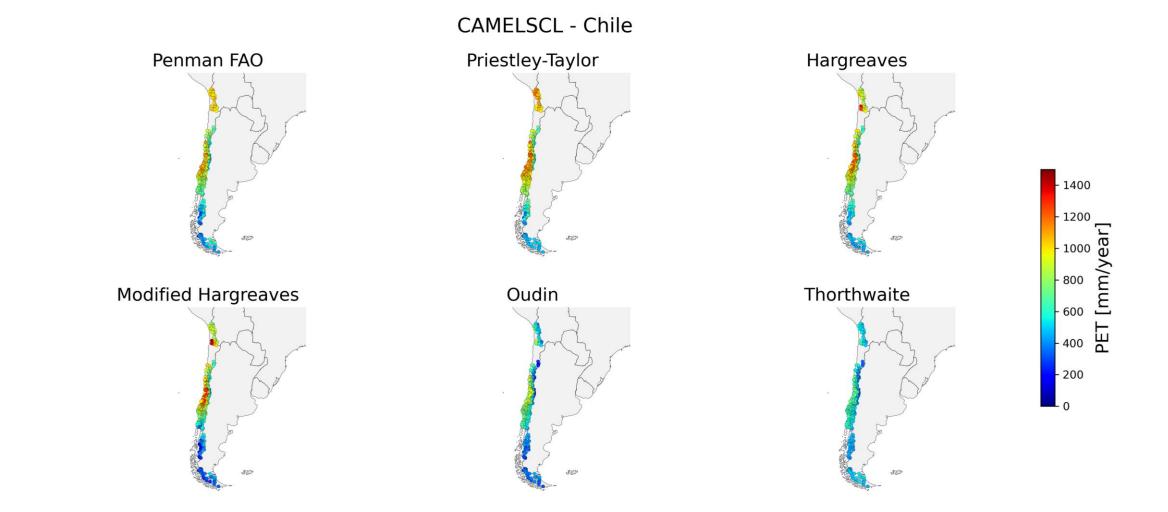






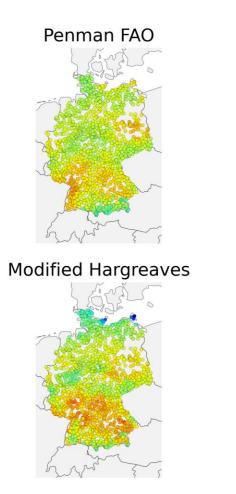


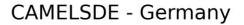
PET annual average





PET annual average

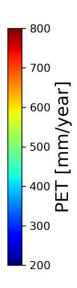








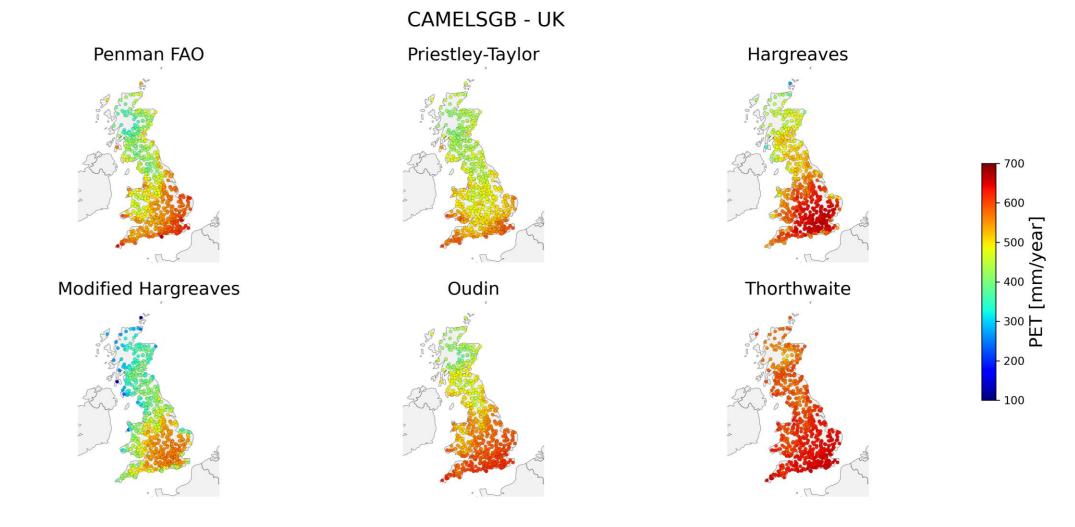




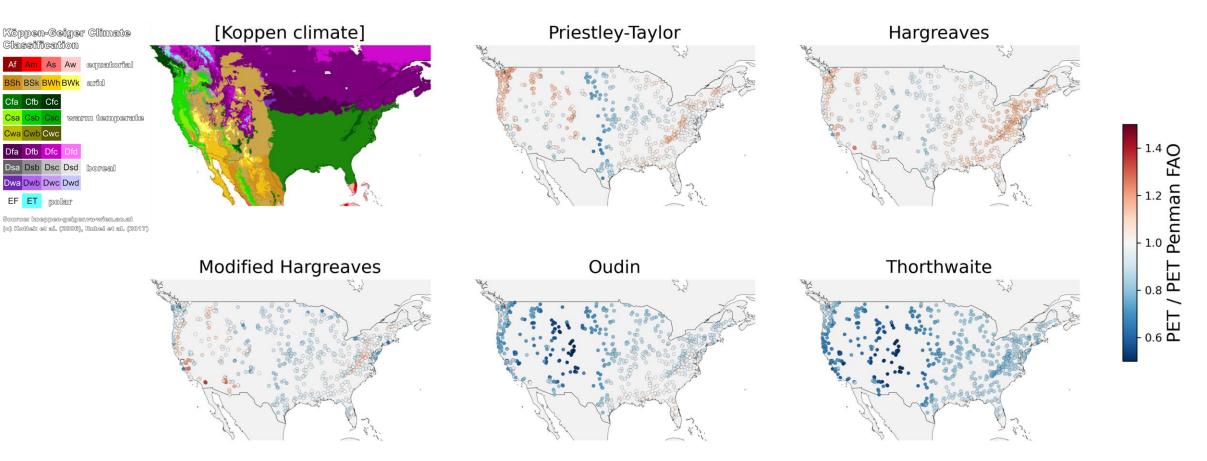
Hargreaves



PET annual average





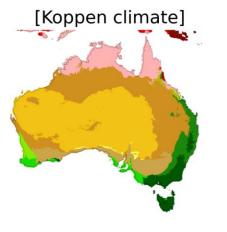


CAMELS - US

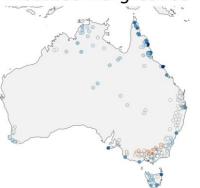




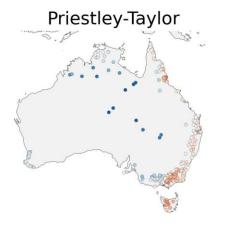
Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)

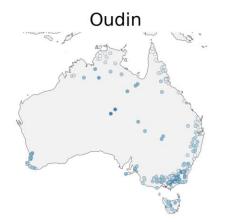


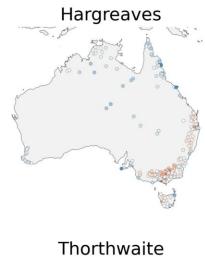


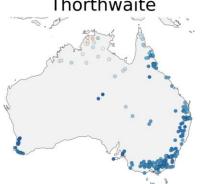


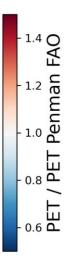








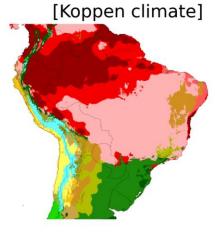








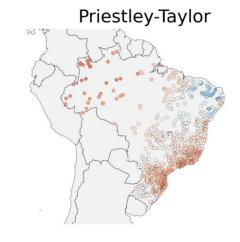
Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)



Modified Hargreaves



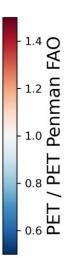
CAMELSBR - Brazil













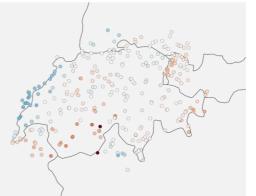


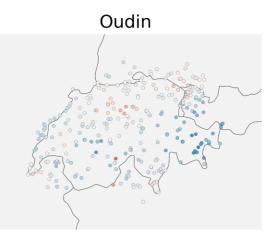
Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)

[Koppen climate]

A A S

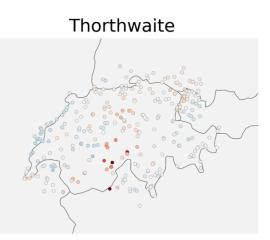
Modified Hargreaves

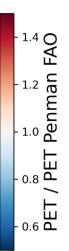




Priestley-Taylor

Hargreaves





CAMELSCH - Switzerland





Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)



Modified Hargreaves



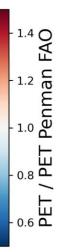
CAMELSCL - Chile





Hargreaves



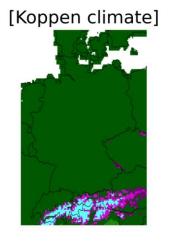




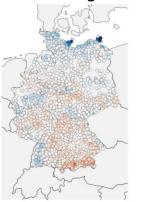


Köppen-Geiger Climate Classification Af An As Aw equatorial BSh BSk BWh BWk and Cfa Cfb Cfc Csa Csb Csc Cwa Cwb Cwc Dfa Dfb Dfc Dfd Dsa Dsb Dsc Dsd Dwa Dwb Dwc Dwd EF ET polar

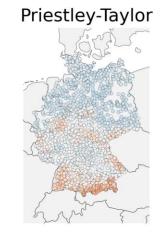
Source: koeppen-geiger.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)



Modified Hargreaves



CAMELSDE - Germany



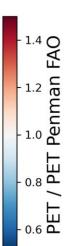


Hargreaves



Thorthwaite









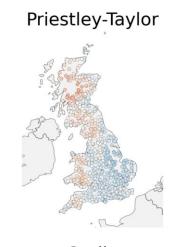
Source: koeppen-geigen.vu-wien.ac.at (c) Kottek et al. (2006), Rubel et al. (2017)



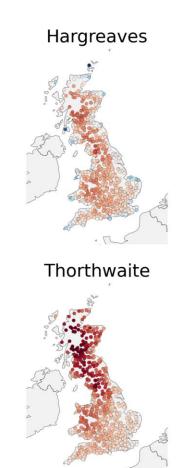
Modified Hargreaves

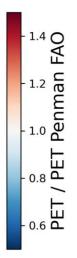


CAMELSGB - UK



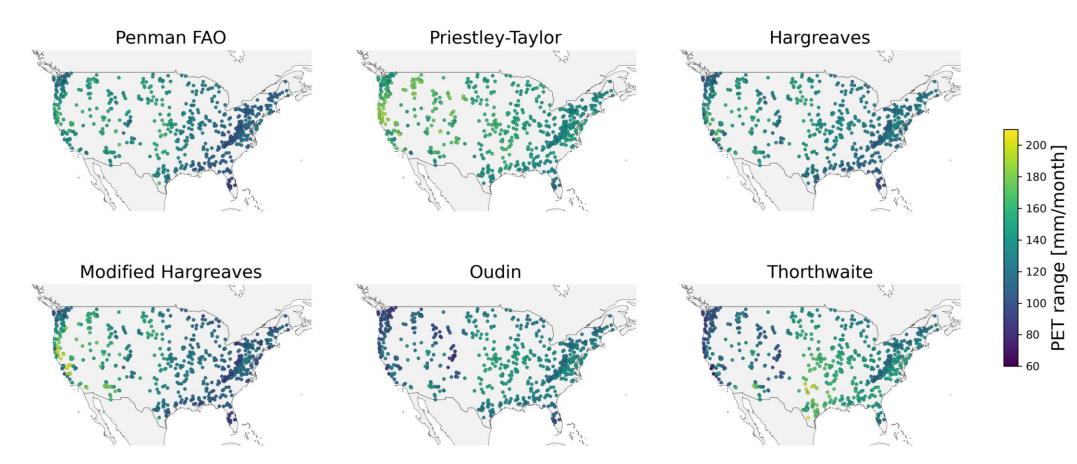
Oudin







CAMELS - US





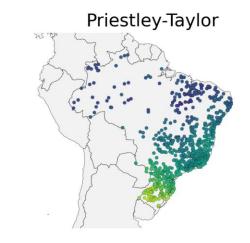
CAMELSAUS - Australia **Priestley-Taylor** Penman FAO Hargreaves Modified Hargreaves Oudin Thorthwaite

- 250 - 225 - 200 - 175 - 175 - 150 - 125 - 100 - 125 - 100 - 75 - 75 - 200 -

50



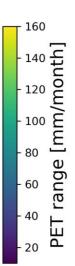
Penman FAO 345 Modified Hargreaves CAMELSBR - Brazil



Oudin

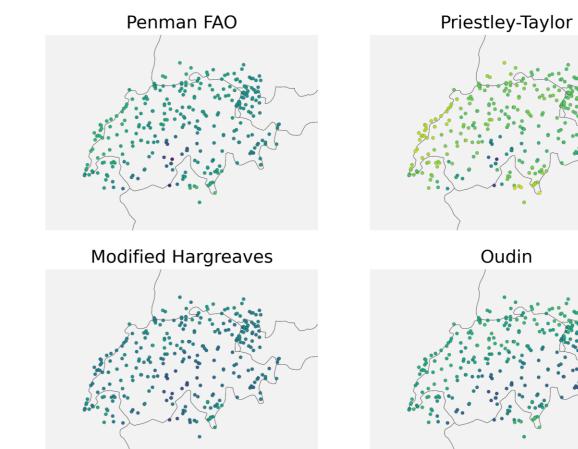


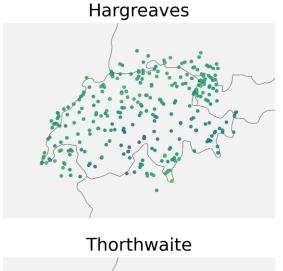




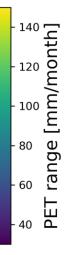


CAMELSCH - Switzerland

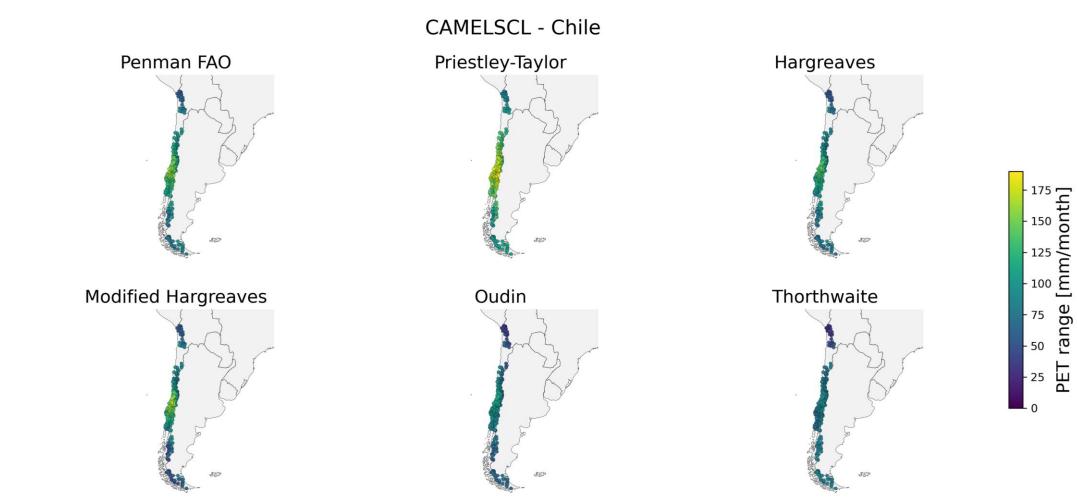






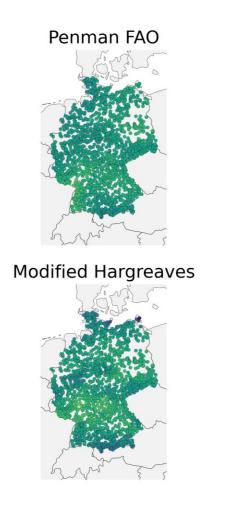








CAMELSDE - Germany

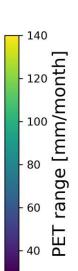




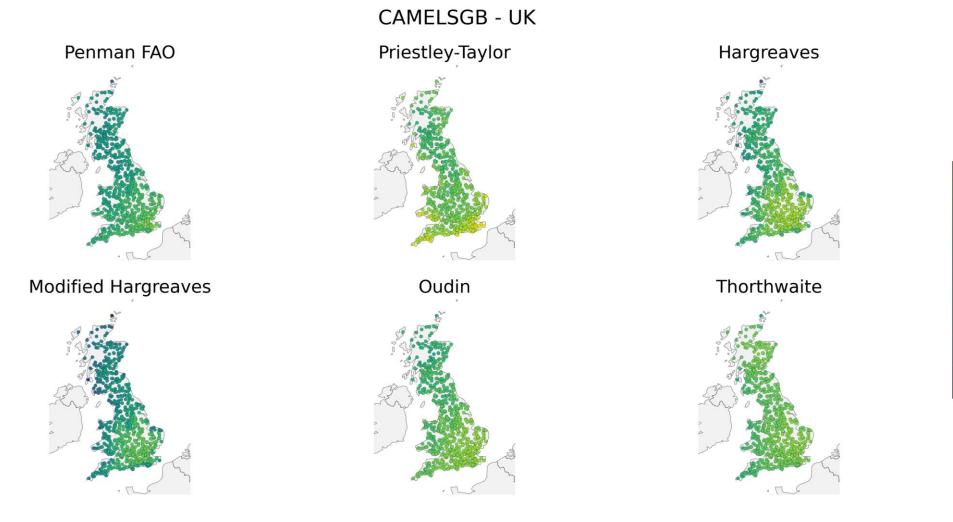


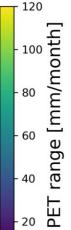






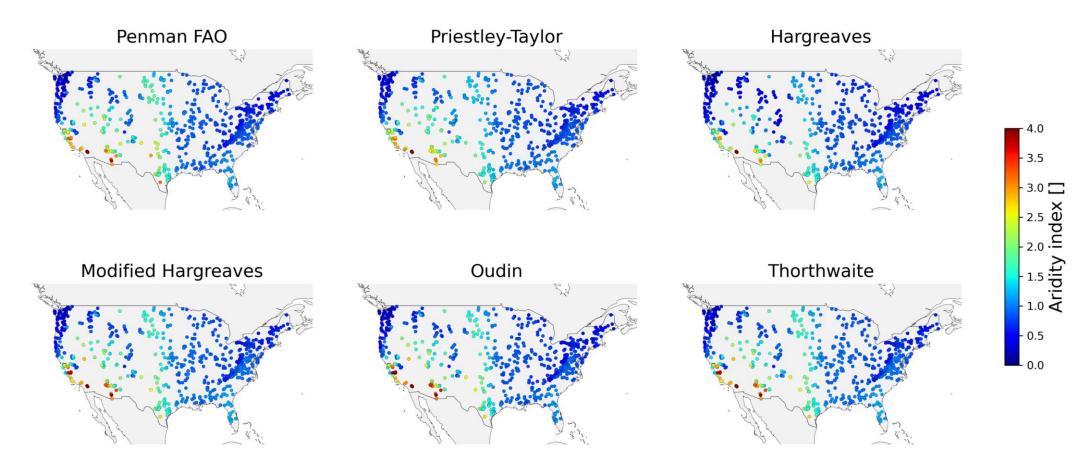








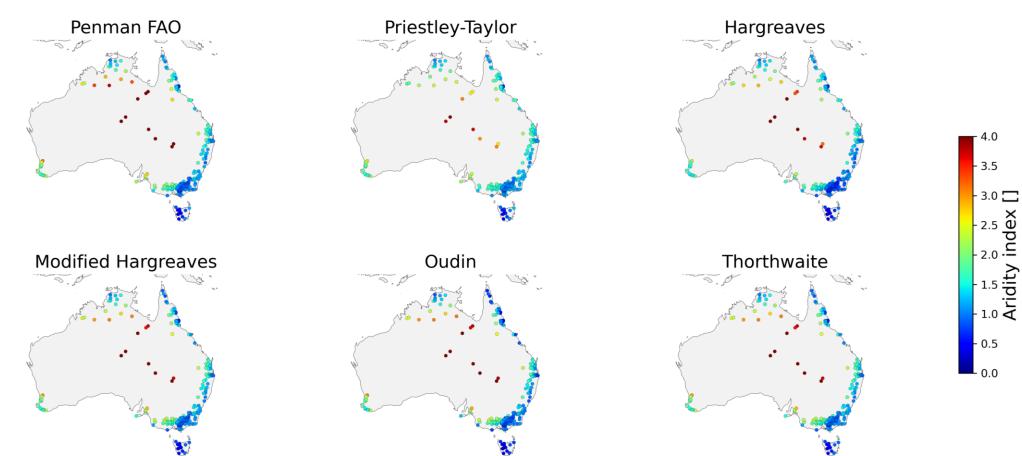
Aridity index



CAMELS - US



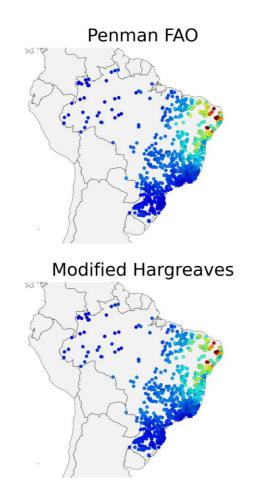
Aridity index



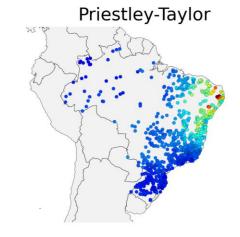
CAMELSAUS - Australia

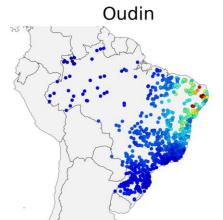


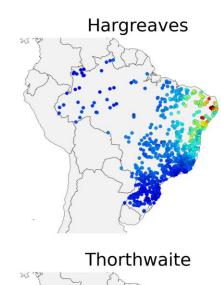
Aridity index

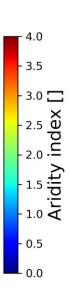






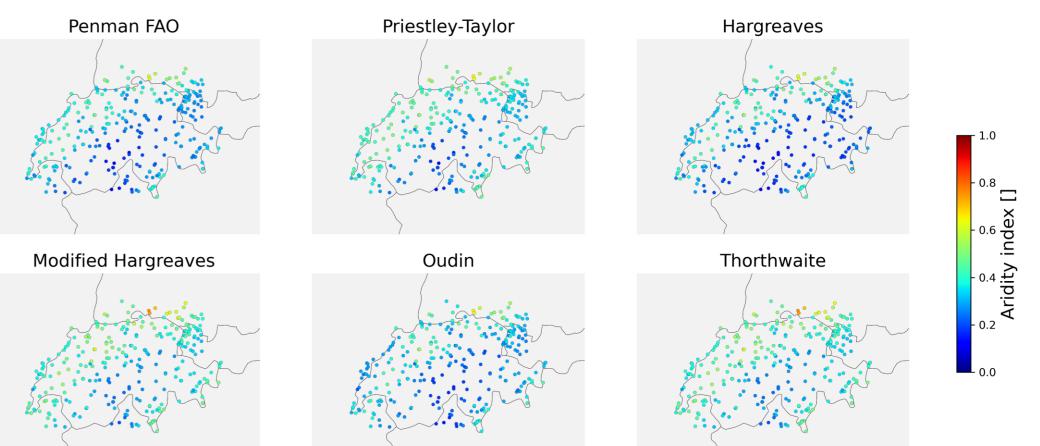








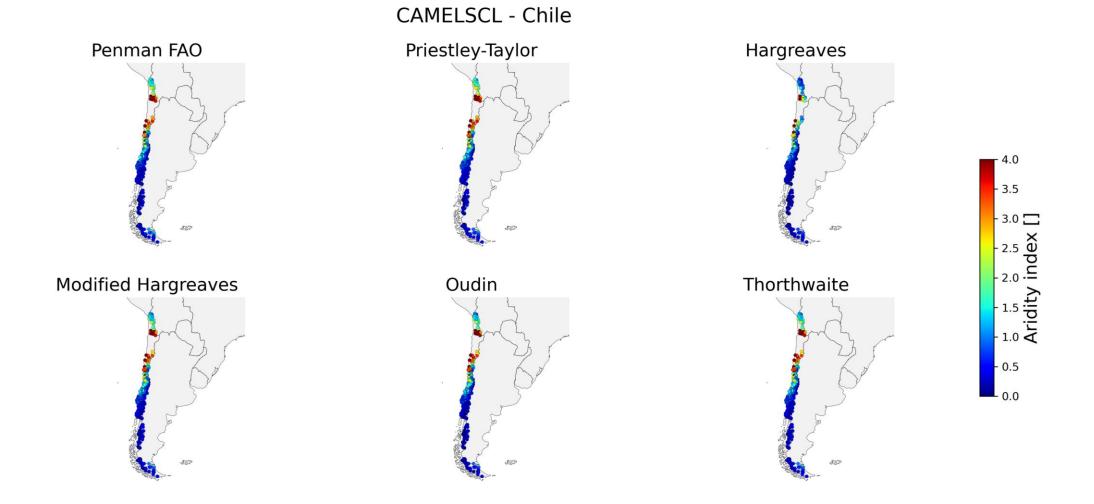
Aridity index



CAMELSCH - Switzerland

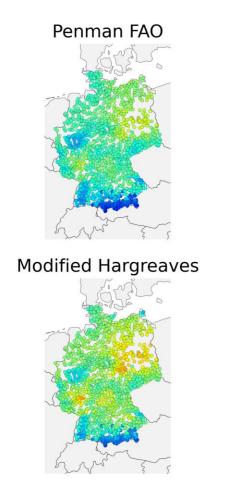


Aridity index





Aridity index



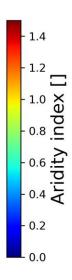
CAMELSDE - Germany





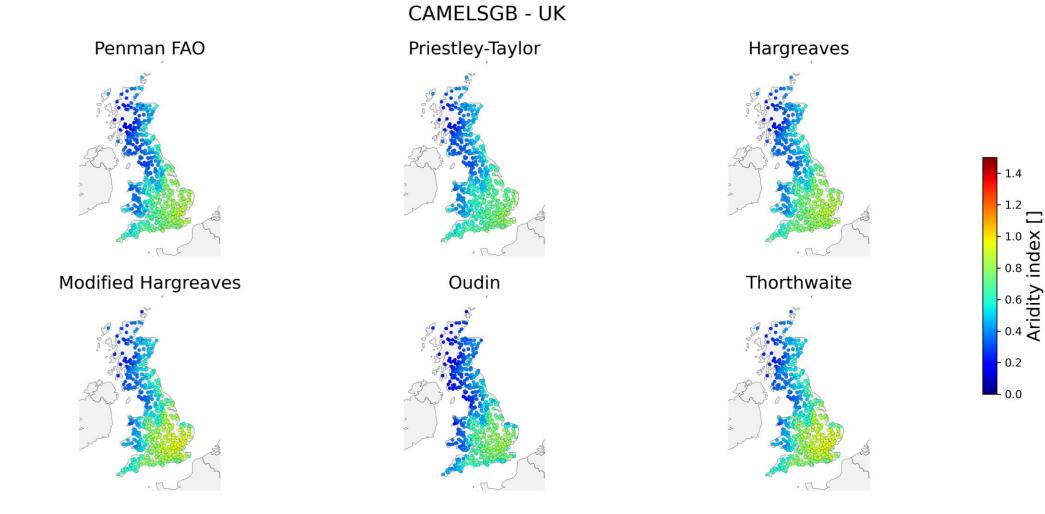
Hargreaves





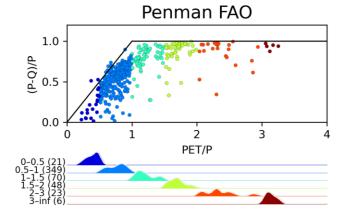


Aridity index

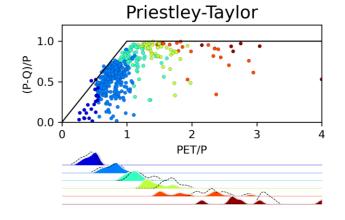


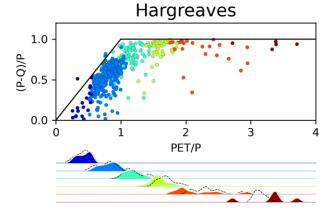


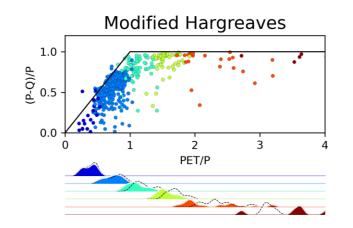
Budyko space

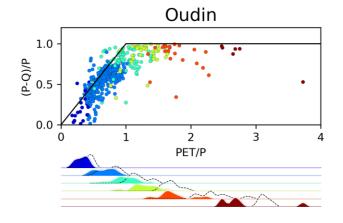


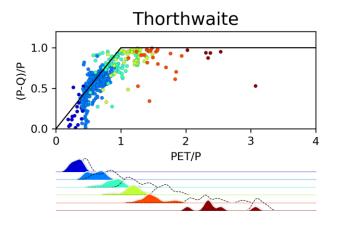
CAMELS - US





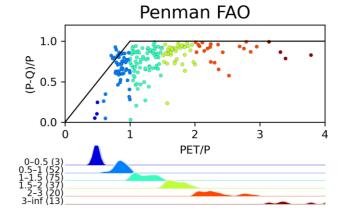




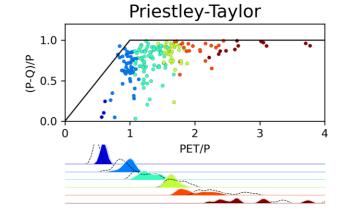


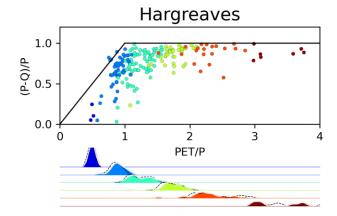


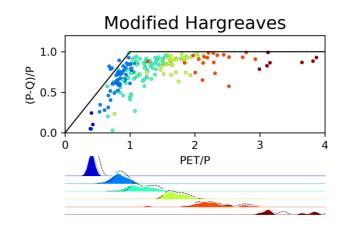
Budyko space

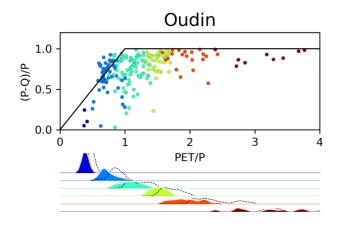


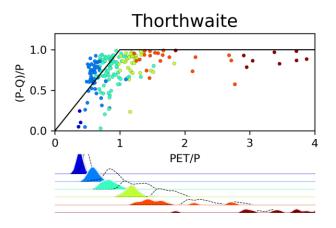
CAMELSAUS - Australia





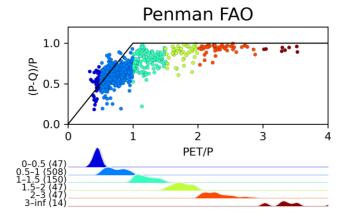








Budyko space





2

PET/P

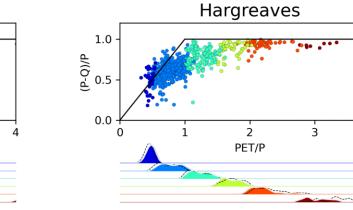
3

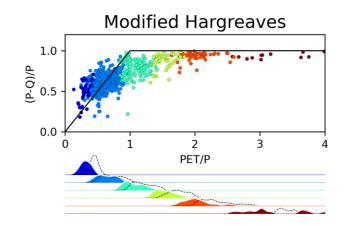
d/(O-d)

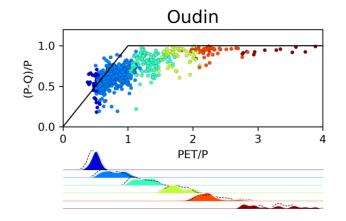
0.0

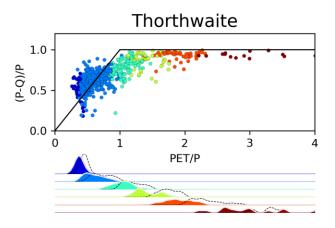
0

1



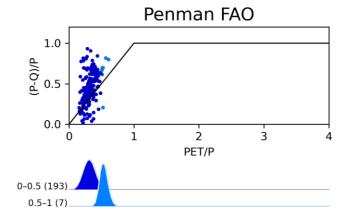




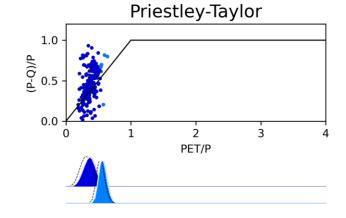


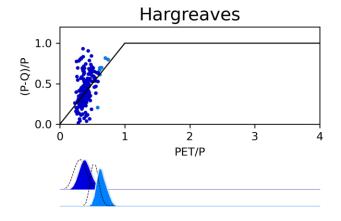


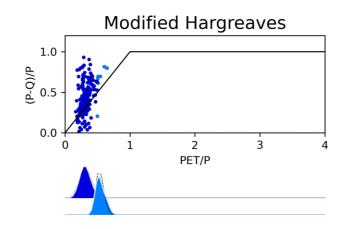
Budyko space

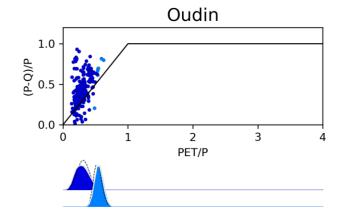


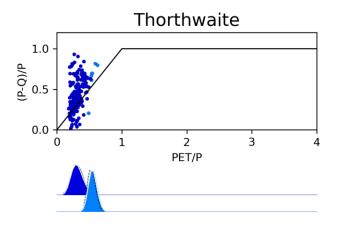






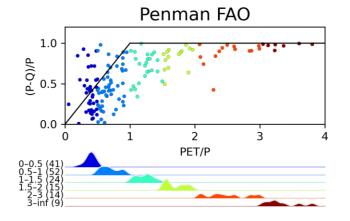


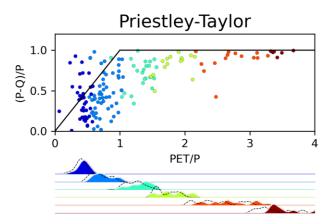




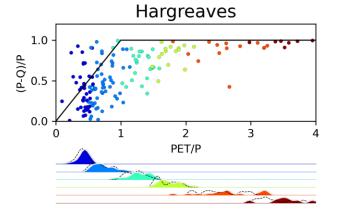


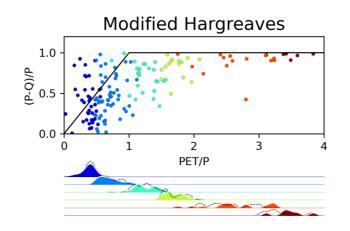
Budyko space

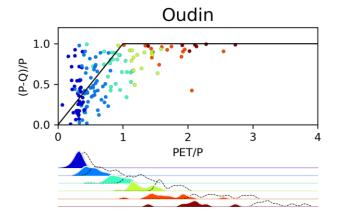


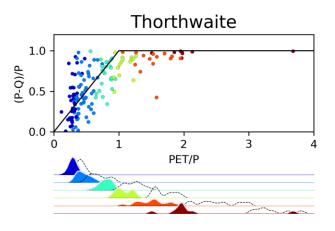


CAMELSCL - Chile



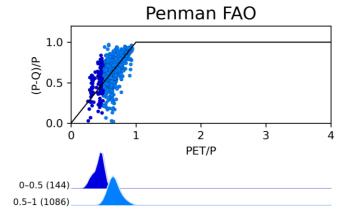




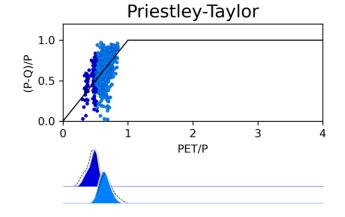


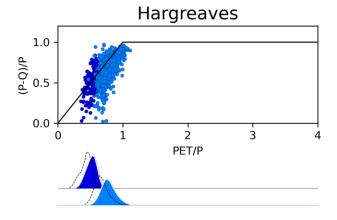


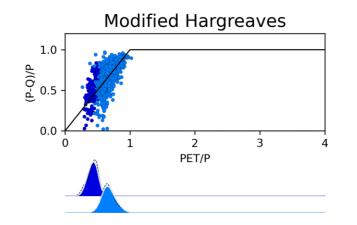
Budyko space

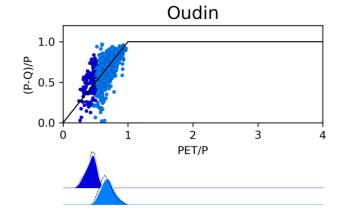


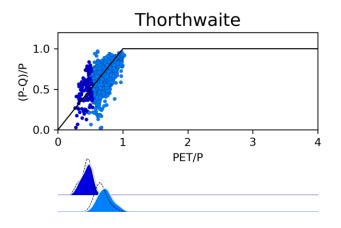
CAMELSDE - Germany





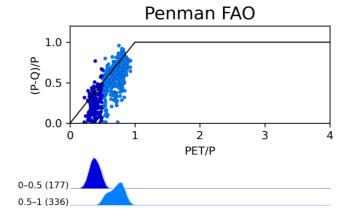


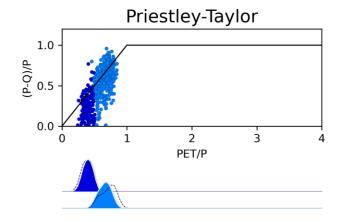




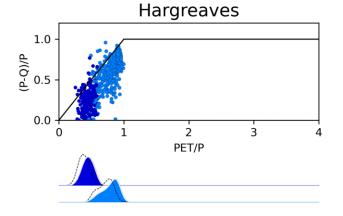


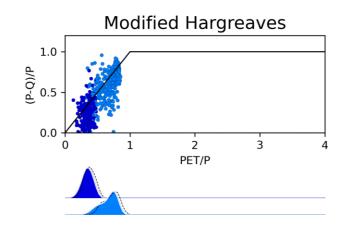
Budyko space

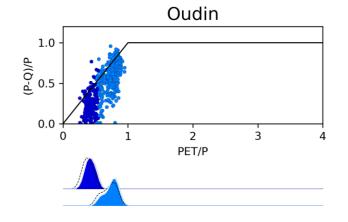


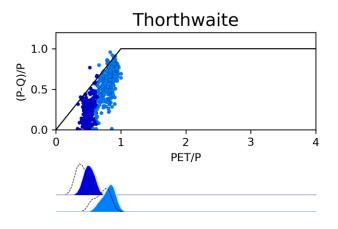


CAMELSGB - UK













PET formulas:

FAO Penman-Monteith

Priestley-Taylor

<u>Hargreaves</u>

Modified Hargreaves

<u>Oudin</u>

Thorthwaite



FAO Penman-Monteith (Allen & Pereira, 1998)

$$PET = \frac{0.408\Delta(R_n - G) + \gamma \frac{900}{T + 273}u_2(e_s - e_a)}{\Delta + \gamma(1 + 0.34u_2)} \text{ [mm/day]}$$

- Δ : Slope of the saturation vapor pressure curve (kPa/°C)
- R_n : Net radiation at the crop surface (MJ/m²/day)
- G: Soil heat flux density (MJ/m²/day)
- γ: Psychrometric constant (kPa/°C)
- T: Mean daily air temperature at 2m height (°C)
- u₂: Wind speed at 2m height (m/s)
- e_s: Saturation vapor pressure (kPa)
- e_a: Actual vapor pressure (kPa)



Priestley-Taylor (Priestley & Taylor, 1972)

$$PET = \alpha \cdot \frac{\Delta \cdot (R_n - G)}{\lambda_v \cdot (\Delta + \gamma)} \cdot 1000 \ [mm/day]$$

- α : Empirical constant = 1.26
- Δ : Slope of saturation vapor pressure curve (kPa/°C)
- R_n: Net radiation (MJ/m²/day)
- G: Soil heat flux (MJ/m²/day)
- λ : Latent heat of vaporization (MJ/kg)
- γ: Psychrometric constant (kPa/°C)



Hargreaves (Hargreaves & Samani, 1985)

 $PET = 0.0023 \cdot R_{a} \cdot (T_{avg} + 17.8) \cdot \sqrt{T_{max} - T_{min}} [mm/day]$

- R_a: Extraterrestrial radiation (MJ/m²/day)
- T_{avg}: Average daily temperature (°C)
- T_{max}: Maximum daily temperature (°C)
- T_{min} : Minimum daily temperature (°C)



Modified Hargreaves (Adam et al., 2006)

 $PET = 0.0013 \cdot R_{a} \cdot (T_{avg} + 17) \cdot (T_{max} - T_{min} - 0.0123P)^{0.76} [mm/day]$

- R_a: Extraterrestrial radiation (mm/day)
- T_{avg}: Average daily temperature (°C)
- T_{max} : mean maximum daily temperature for a given month (°C)
- T_{min} : mean minimum daily temperature for a given month (°C)
- P is the precipitation for a given month (mm)



Oudin (Oudin et al., 2005)

$$PET = \frac{R_a \cdot (T_{avg} + 5)}{\lambda \cdot 100} \ [mm/day]$$

- R_a: Extraterrestrial radiation (MJ/m²/day)
- T_{avg}: Average daily temperature (°C)
- λ : Latent heat of vaporization (2.45 MJ/kg)



Thornthwaite (Thornthwaite, 1948)

$$PET = 16 \cdot \left(\frac{10 \cdot Tavg}{I}\right)^{a} \cdot \frac{N}{12} \cdot \frac{d_{m}}{30}$$

- T_{avg}: Average daily temperature (°C)
- N: Hours of light of the day
- d_m : Days in the month
- I: Annual heat index

$$I = \sum_{i=1}^{12} \left(\frac{T_i}{5} \right)^{1.514}$$

- T_i: average long-term temperature of month i
- a: Empirical exponent

 $a = 0.492 + 1.792e^{-5} I - 771e^{-7} I^{2} + 675e^{-9} I^{3}$



Other references

Earth maps: Made with Natural Earth. Free vector and raster map data @ naturalearthdata.com