

According to the simple OTOR model:

$$I \sim F_1(D/D_{63\%}, R) \quad (1)$$

where the function  $F_1$  is defined by:<sup>1</sup>

$$F_1(D/D_{63\%}, R) \equiv 1 + \frac{1}{(1-R)} \mathcal{W} \left\{ -(1-R) \exp \left[ - \left( 1 - \frac{e-1}{e} (1-R) \right) D/D_{63\%} - (1-R) \right] \right\} \quad (2)$$

For the special case of  $R = 1$ , the above reduces to:<sup>2</sup>

$$F_1(D/D_{63\%}, 1) = 1 - \exp(-D/D_{63\%}) \quad (3)$$

Thus, the SSE model is simply OTOR with  $R=1$ .

In the SAR model, luminescence intensities ( $L_x$ ) are normalized by a intensities ( $T_x$ ) of a test dose ( $D_T$ ). Thus:

$$L_x/T_x = c \frac{F_1(D/D_{63\%}, R)}{F_1(D_T/D_{63\%}, R)} \quad (4)$$

All the physical constants in Eq. (4) have physical meaning:

- $D_{63\%}$  is the dose at which OSL intensity reaches 63% of saturation. (This is like  $b$  is the SSE model.) It is proportional to, among other things, the trap concentration.
- $R$  is the ratio of the recombination to retrapping rate constants.
- $c$  tests the validity of the SAR model. If SAR is perfect, then  $c=1$ . In practice, typically  $c = 1 \pm 0.1$ . If, for some material,  $c$  differs strongly from 1, then SAR is possibly not appropriate for that material.

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<sup>1</sup>I am using  $F_1$  here instead of simply  $F$  so that this function, which uses  $R$  as an argument, is not confused the one in the paper that uses  $Q$ .

<sup>2</sup>Note that Eq. (2) is singular as  $R \rightarrow 1$ . A lot of math (not shown) is required to go from Eq. (2) to Eq. (3).