

Observed Yanai Wave Trajectories in the Western Equatorial Atlantic

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1 Background

- The western equatorial Atlantic is characterized by a zonal equatorial current system and the North Brazil current (NBC, Fig. 1).

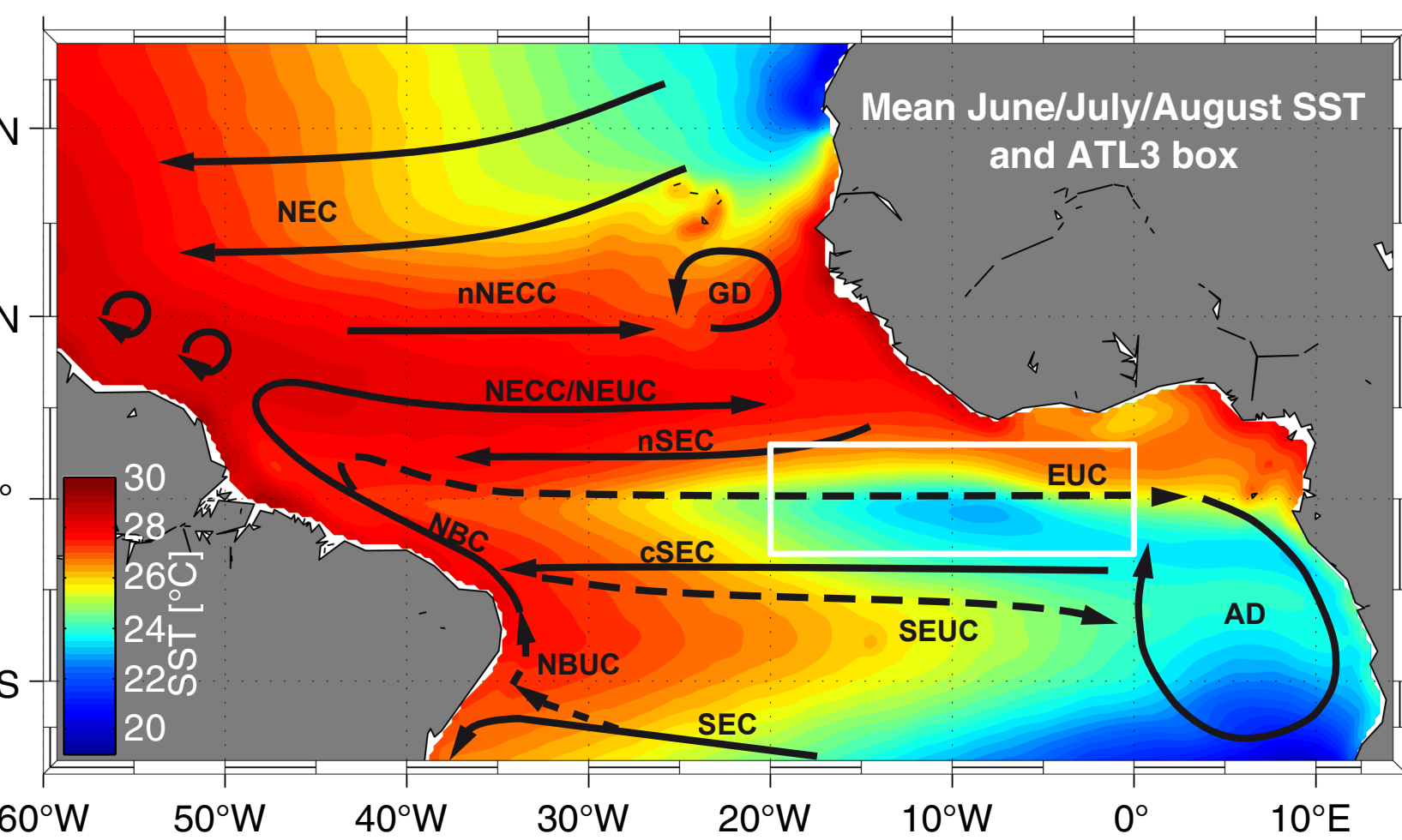
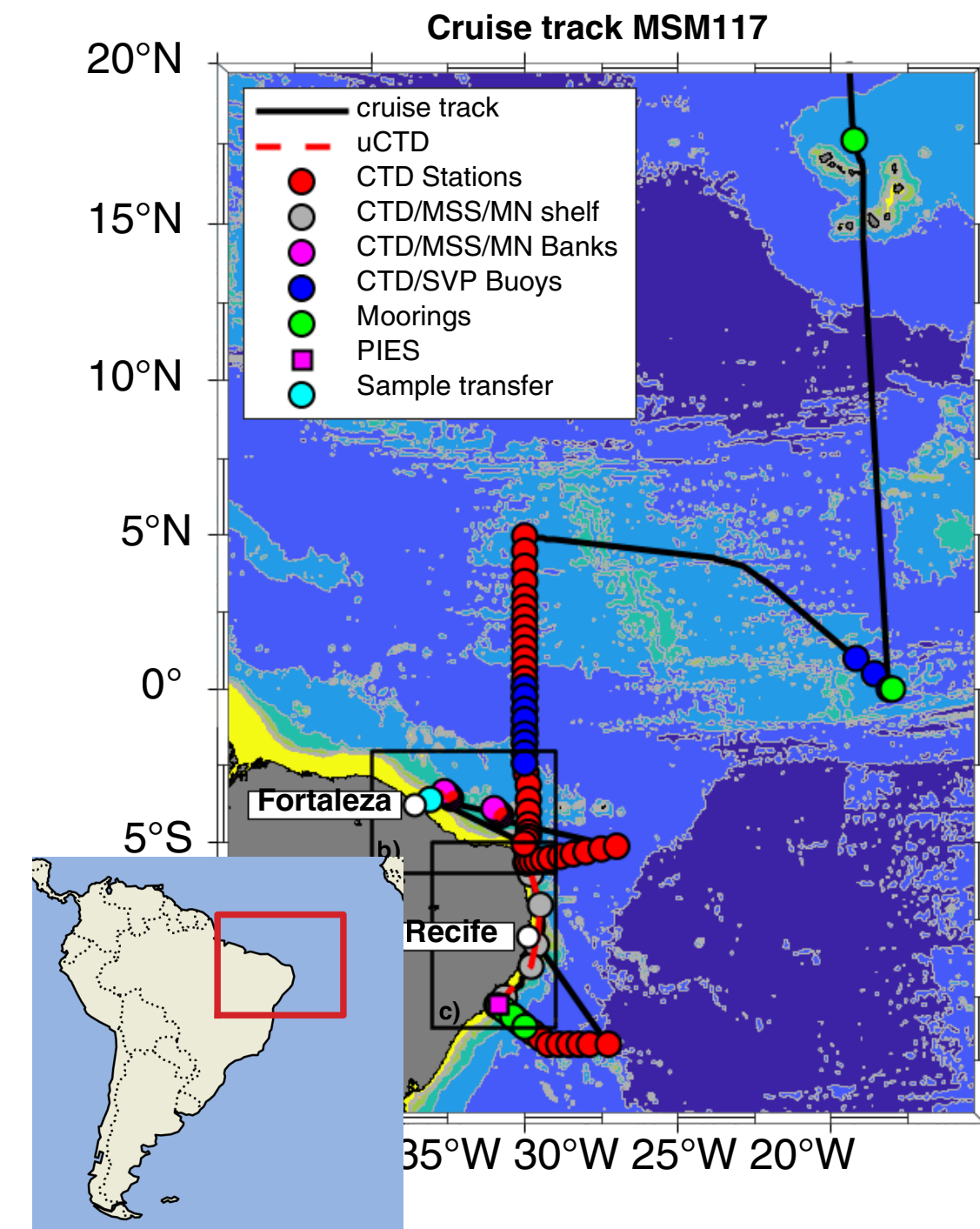


Figure 1: Surface (solid) and subsurface (dashed) tropical currents in the Atlantic with 1998-2009 mean June-August SST (in °C). Figure from [2].

- The NBC transports water northward across the equator as part of the Atlantic Meridional Overturning Circulation. [1]
- During cruise MSM117 in May and June, 2023, 8 surface drifters were deployed along 35°W (Fig. 2).

Figure 2: Cruise track of MSM117 in May-June, 2023, with stations and zoomed-out map of South America. [3]

2 Observations

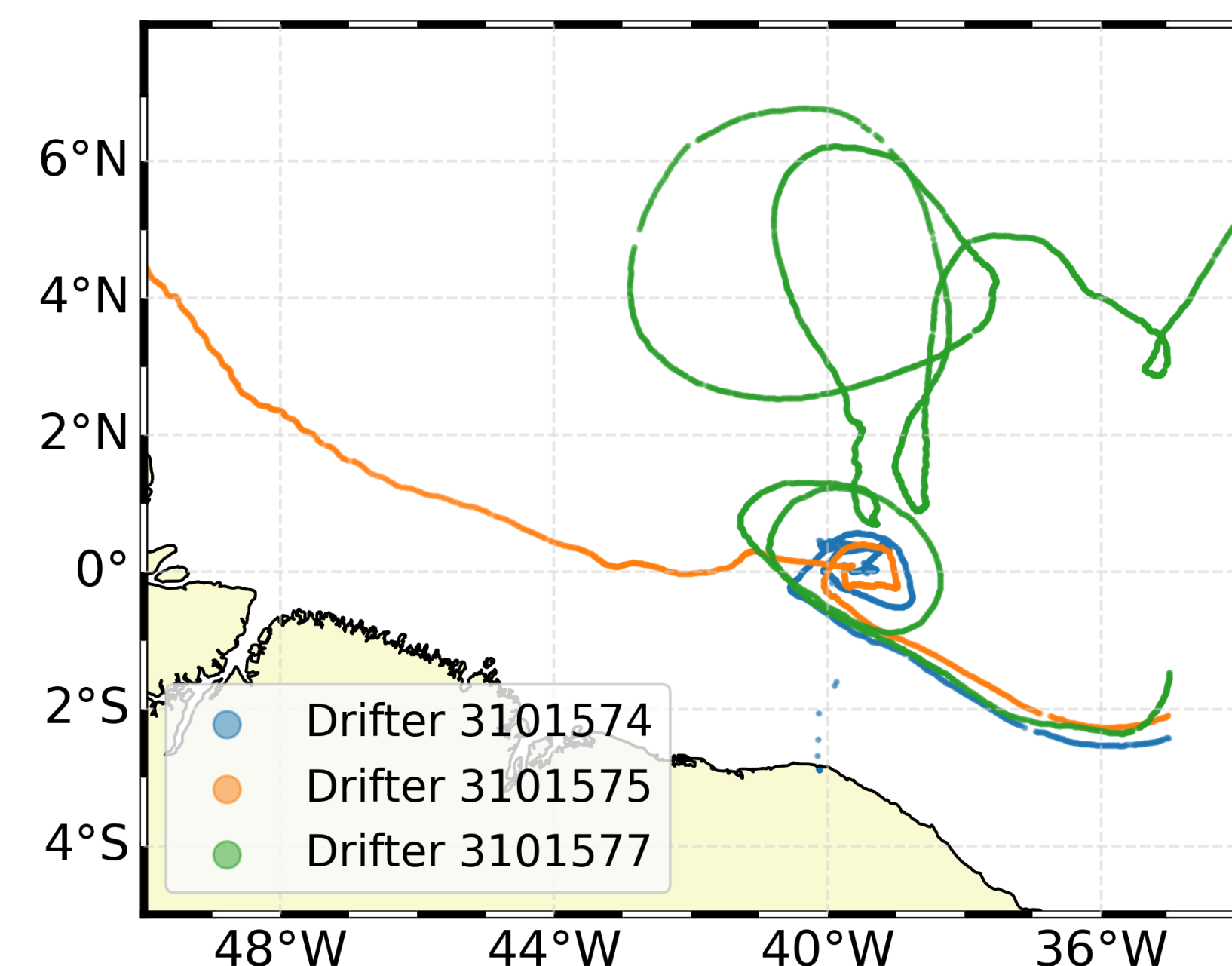


Figure 3: Trajectories of surface drifters deployed at 35°W during cruise MSM117 in May 2023 (data: [A]).

- Surface Velocity Program (SVP) drifters float with the upper 30m of ocean currents (Fig. 4).
- 3 drifters encountered a circular motion centered at the equator at about 40°W.
- The observed period was 14 days, with radii between 60 and 140 km (Fig. 3).

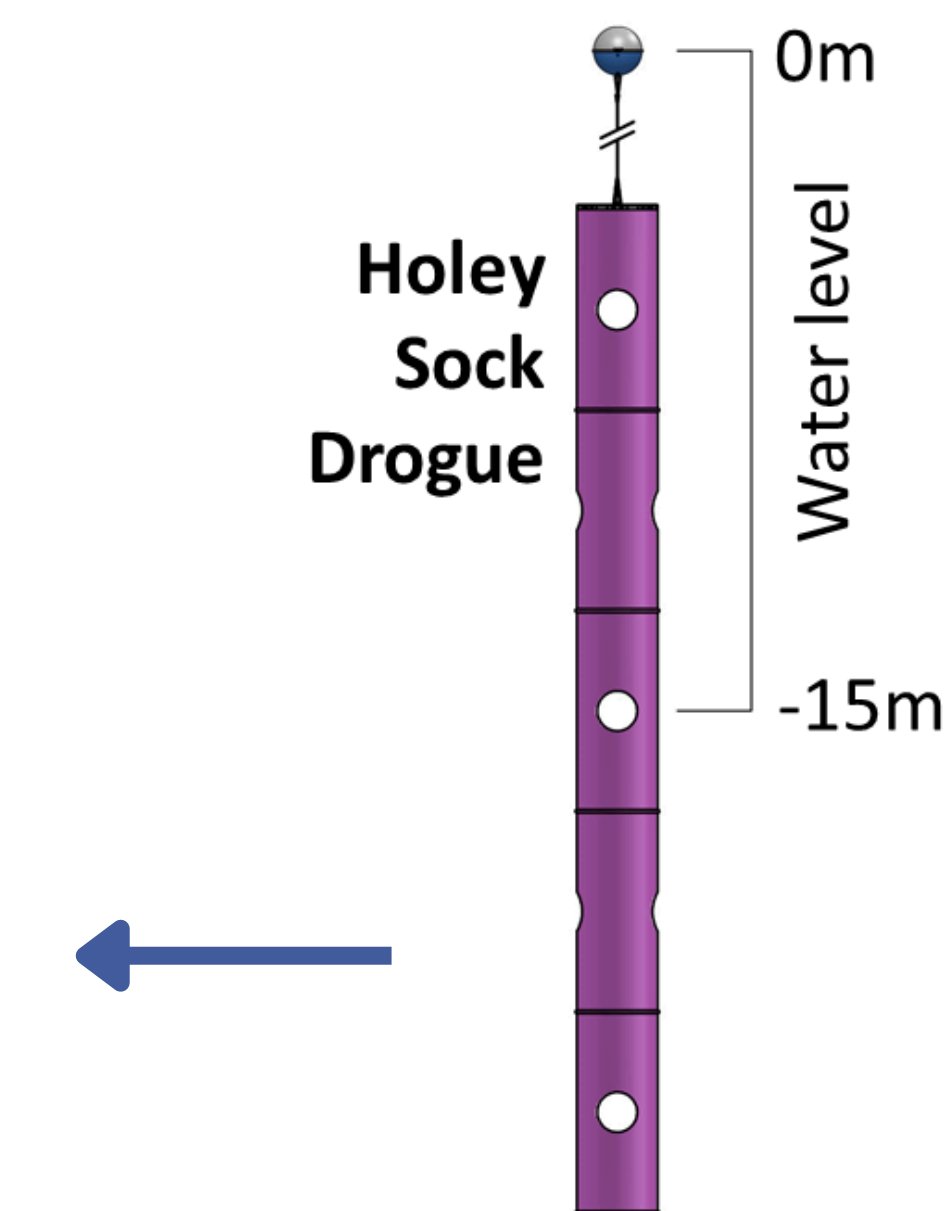


Figure 4: Sketch of a SVP drifter with head buoy and drogue (adapted from [B]).

Takeaway: Drifters followed circular trajectories centered at the equator.

3 Yanai Waves

- Yanai waves are trapped around the equator propagating eastward. They are observed in all ocean basins often with periods of 10 to 30 days and long wavelengths. [4]
- Yanai waves have a non-zero meridional velocity at the equator, necessary to move the drifters northward and out of the strong NBC.

Generation mechanism

- In the ocean, Yanai waves can be generated e.g., by fluctuations in the meridional wind component. [5,6]

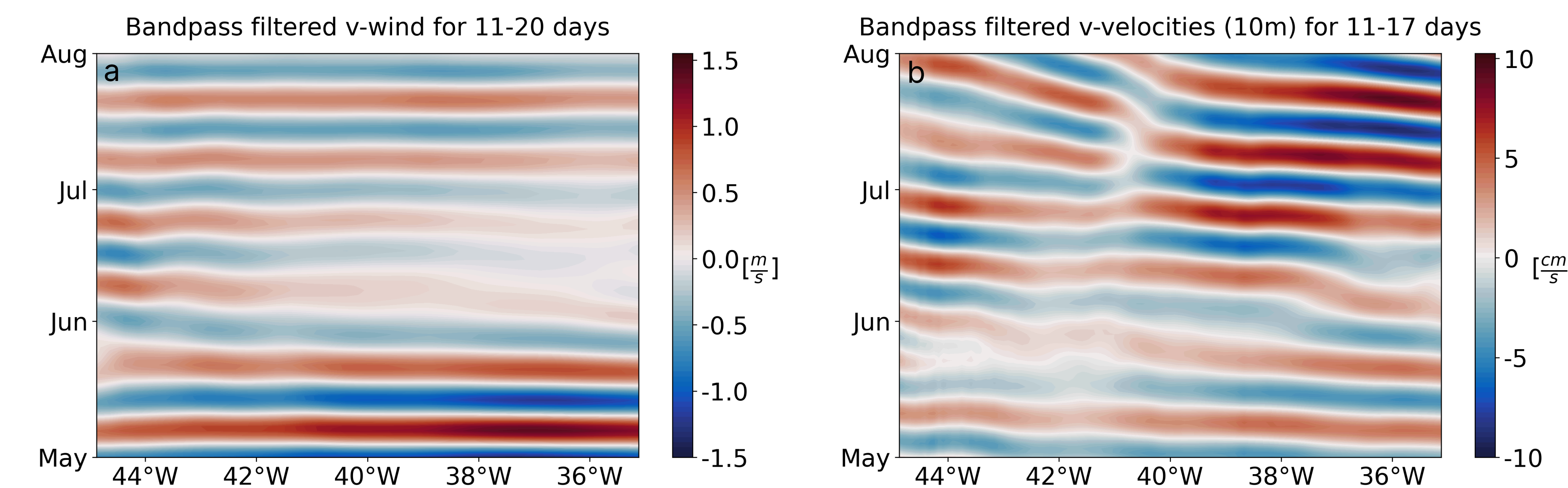


Figure 5: a) Bandpass filtered meridional wind component for 11-20 days [m/s] (data: [C]), b) upper 10m-surface currents for 11-17 days [cm/s] (data: [D]). Both panels are averaged over 1.5°N to 1.5°S.

- Biweekly fluctuations are visible in the meridional wind component (Fig. 5a) and the surface currents (Fig. 5b) consistent with a 14-day Yanai wave.

Takeaway: Yanai waves can be generated by meridional wind anomalies.

5 Discussion and Summary

- Drifters followed circular trajectories at 40°W centered at the equator with a period of 14 days.
- 14-day Yanai waves can be generated by biweekly fluctuations of the meridional wind component.
- Observed situation is reproducible in about 10% of the cases using a mean state velocity field combined with a 14-day Yanai wave velocity field.
- Most favorable conditions are amplitudes >0.6 m/s, wave phases that generate northward velocities at the equator, and deployment locations south of the equator.
- Rarely observed before: Drifters tend to leave the equator quickly due to poleward Ekman transport.
- Further investigation of mooring or ship-based velocity data could confirm the presence of a 14-day Yanai wave.

4 Reproducing the Observations with Artificial Drifter Trajectories

Drifter Trajectories

- The situation was reproduced using a simple model calculating artificial drifter trajectories (Fig. 6).
- The next position $(x(i+1), y(i+1))$ is obtained using the previous position $(x(i), y(i))$ and a velocity field (u, v) that contains a climatological background field and Yanai wave velocities:

$$x(i+1) = x(i) + [u_{Yanai}(x(i), y(i)) \cdot A + u_{Background}(x(i), y(i))] \cdot dt$$
$$y(i+1) = y(i) + [v_{Yanai}(x(i), y(i)) \cdot A + v_{Background}(x(i), y(i))] \cdot dt$$

where:

- dt : time step was set to 20 min;
- A : amplitude of the Yanai wave was estimated by the cross-equatorial drift velocity.

Yanai Wave Velocities

- Yanai waves can be described using the linearized gravity-reduced shallow water equations on an equatorial β -plane.
- Yanai wave velocities (u_{Yanai}, v_{Yanai}) can be described as solutions to the dispersion relation $\frac{\omega}{c} - k - \frac{\beta}{\omega} = 0$. [7]

$$u_{Yanai} = -\frac{\omega y}{c} e^{-\frac{\beta y^2}{2c}} \sin(kx - \omega t)$$
$$v_{Yanai} = e^{-\frac{\beta y^2}{2c}} \cos(kx - \omega t)$$

where:

- ω : wave frequency; k : zonal wave number;
- $c = 1.3$ m/s: gravity wave speed (2. baroclinic mode);
- β : meridional gradient of the Coriolis parameter.

Artificial Drifter Experiment

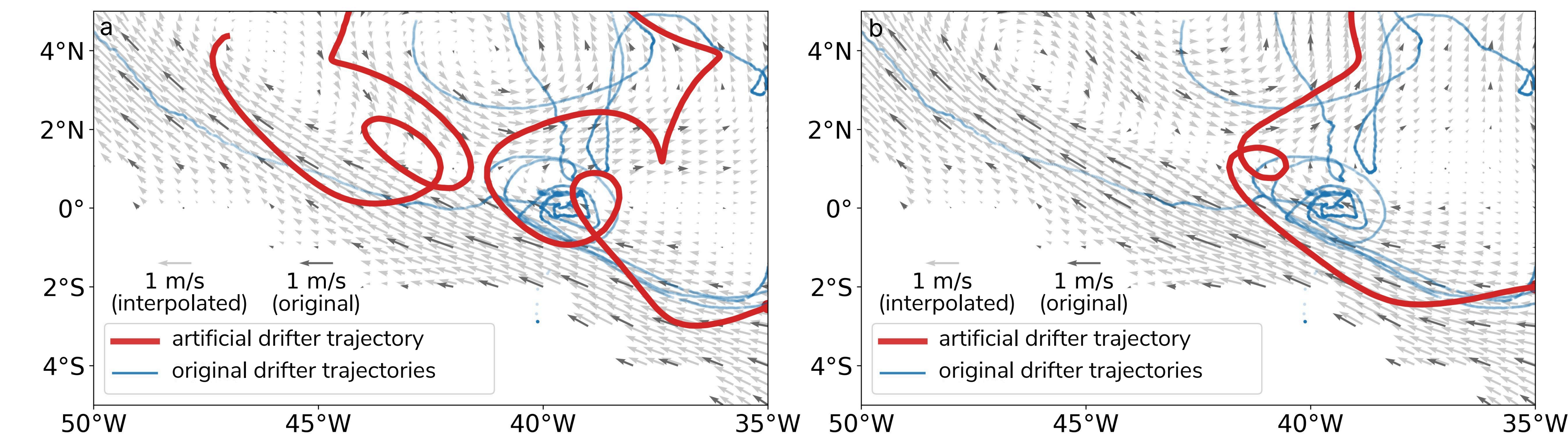


Figure 6: Examples of observed (blue) and artificial (red) drifter trajectories with an interpolated (light grey arrows) climatological background field averaged over the upper 15m (data: [E]).

Throughout the experiment, initial conditions were varied:

- amplitude of the Yanai wave 0.5-0.7 m/s
- phase of the Yanai wave 0-2 π
- deployment position of the artificial drifter $x(0)$ and $y(0)$
- background field, monthly climatological fields for May, June, and July derived from drifter data.

In total, 1,447 (40°W) and 434 (35°W) artificial drifters were deployed. About 10% reproduced a scenario close to the observations.

Takeaway: In certain conditions, Yanai waves can produce circular trajectories at the surface.

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Data

- [A] Drifter trajectories: https://osmc.noaa.gov/erddap/tabledap/OSMC_flattened.html
- [B] Lagrangian Drifter Laboratory of Scripps Institution of Oceanography (<https://gdp.ucsd.edu/ld/>), 04/26
- [C] Wind: <https://www.remss.com/measurements/ccmp/> [8]
- [D] Currents: https://data.marine.copernicus.eu/product/GLOBAL_MULTIYEAR_PHY_001_030 description doi: <https://doi.org/10.48670/moi-00021>
- [E] Drifter climatology: https://www.aoml.noaa.gov/phod/gdp/mean_velocity.php [9]

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