

# Ambient noise surface wave tomography of Mt. Etna volcano structure during 2020-2021

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## 1. Motivation

How can Ambient Noise Tomography (ANT) improve our knowledge of the deep structure beneath Mt. Etna within the actively debated geodynamic context of Eastern Sicily?

### What?

- 1) Provides  $V_s$ , radial anisotropy models of Eastern Sicily;
- 2) Petroseismical models.

### How?

- 1) Improved Ambient Noise Tomography;
- 2) Development of a Petroseismical inversion framework.

## 2. ANT

- **Key components:** dispersive Rayleigh and Love waves;
- **Sensitivity:**  $V_s$  (Rayleigh  $\rightarrow V_{sv}$ , Love  $\rightarrow V_{sh}$ );
- **Lateral Resolution:** Station network density and geometry;
- **Vertical Resolution:** Function of the analyzed frequencies (via sensitivity kernels, e.g. Agius et al., 2023, G<sup>3</sup>);
- **Data Volume:**  $\propto N_s^2/2$ , continuous waveforms able to storage.

### Frequency domain

- Input data: Rayleigh and Love dispersion curves for available inter-station paths;
- No needs for phase correction [Kästle et al., 2016, GJI].

### Main Assumption & "Saving Grace"

**Assumption:** Diffuse wavefield [Boschi & Weemstra, 2015, Rev. Geophys].

#### Why it works anyway:

- Kästle et al., 2016, GJI: Azimuthal averaging recovers true velocity;
- Mulargia and Castellaro, 2008, PRL: On-axis (Fresnel zone) waves dominate correlation;
- Weaver et al., 2009, JASA: Negligible error at short distances.

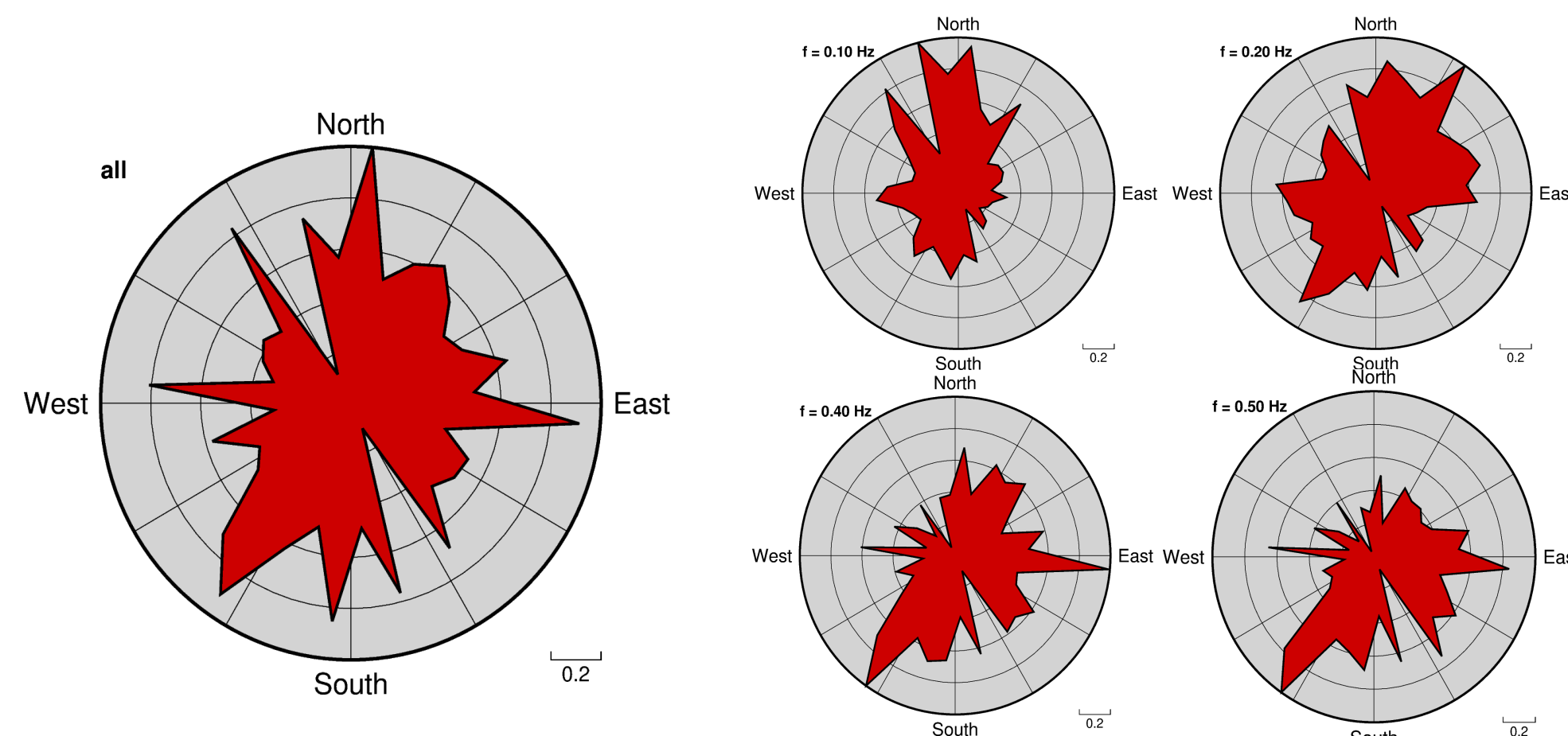


Figure 2: Wind roses as a function of frequency showing the directional power of ambient-noise sources for Rayleigh waves, derived from the coherent wavefield.

## 3. Data

### Array configuration

30 velocimeter from INGV network

- Minimum interstation distance accepted:  $\sim 27$  km (stability);
- 390 dispersion curves for Rayleigh, 370 for Love.

### Period Range

- 1st Jan 2020  $\rightarrow$  31st Dec 2021 (2 years)
- Avoids main fissural eruptions (2018-2019);
  - Seasonally balanced [Yang & Ritzwoller, 2008, G<sup>3</sup>].

### Frequency range

0.08 Hz  $\rightarrow$  0.50 Hz

- Sources: ocean waves [Yang & Ritzwoller, 2008, G<sup>3</sup>, Borzi et al., 2024, GJR Solid Earth];
- Avoids the characteristic 0.70 Hz volcanic tremor peak [Wegler and Seidl, 2009, GRL];
- Reduces effects of unfulfilled assumptions [Kästle et al., 2016, GJI, Tromp et al., 2010, GJI].

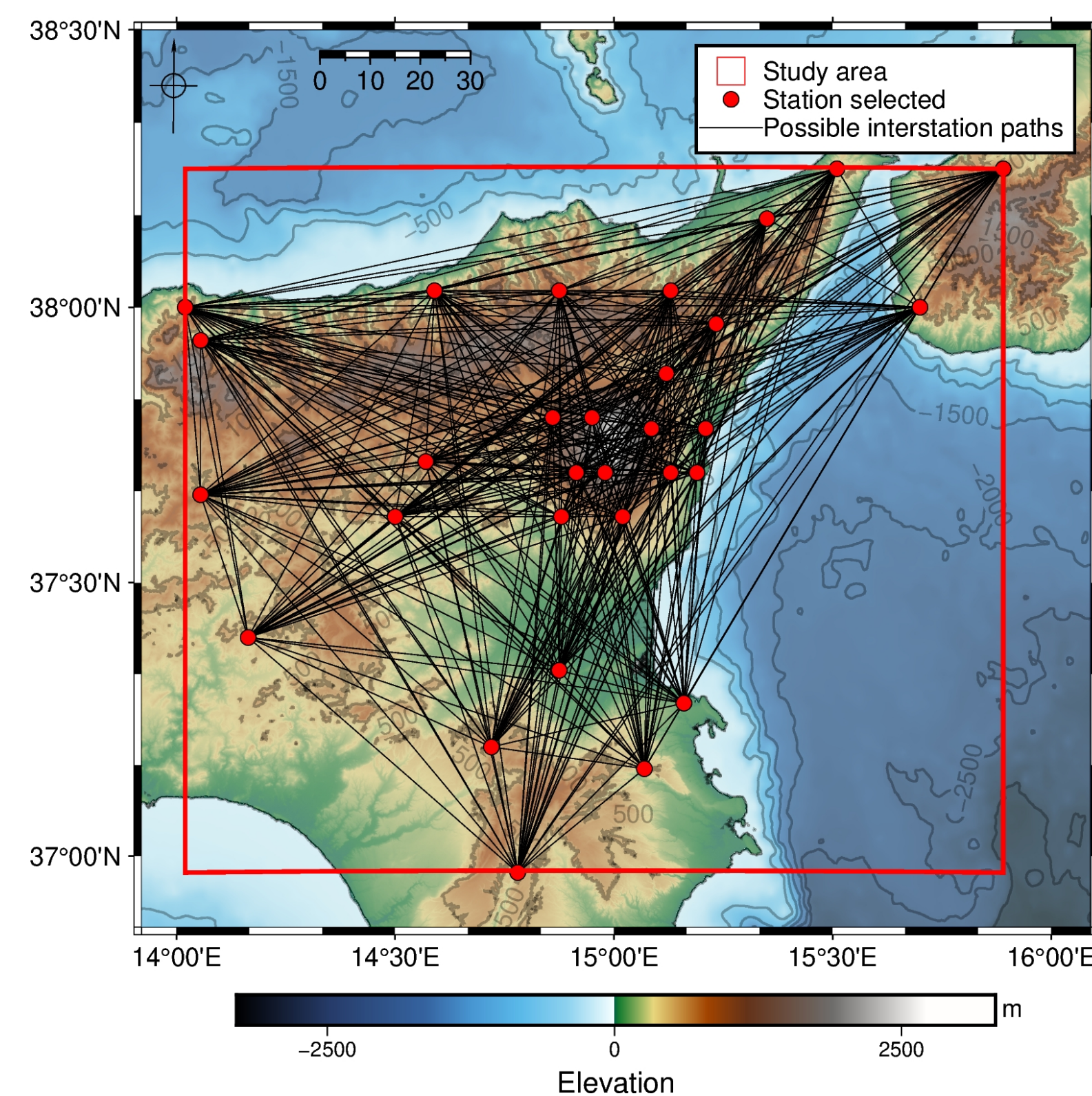


Figure 1: Study area (red square) and selected station network. Colored solid lines indicate the available interstation paths considered in the analysis.

## 4. Methodology (with SeisLib [Magrini et al., 2022, GJI])

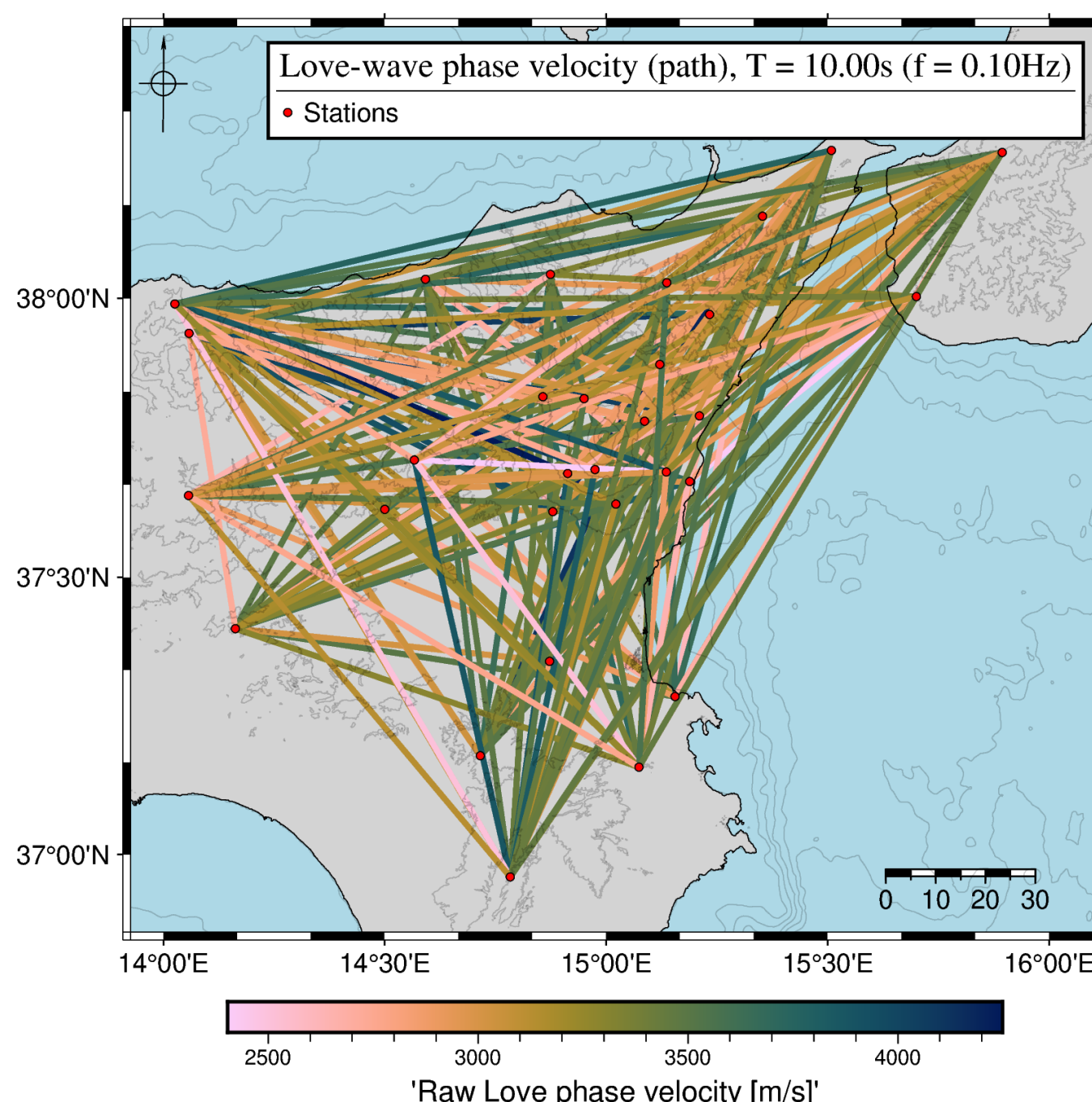
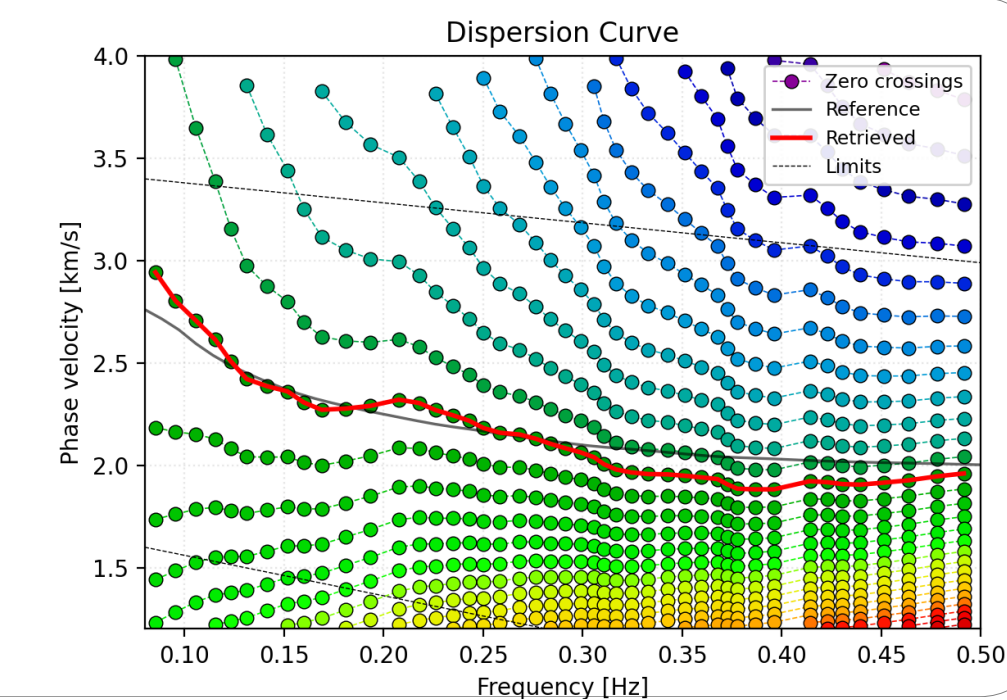


Figure 3: Inter-station paths used for inversion, each assigned its own phase-velocity value at  $v = 0.10$  Hz ( $T = 10.00$  s), extracted from the corresponding dispersion curve.

### Picking of the dispersion curves (multiple branches arising from spurious arrivals)



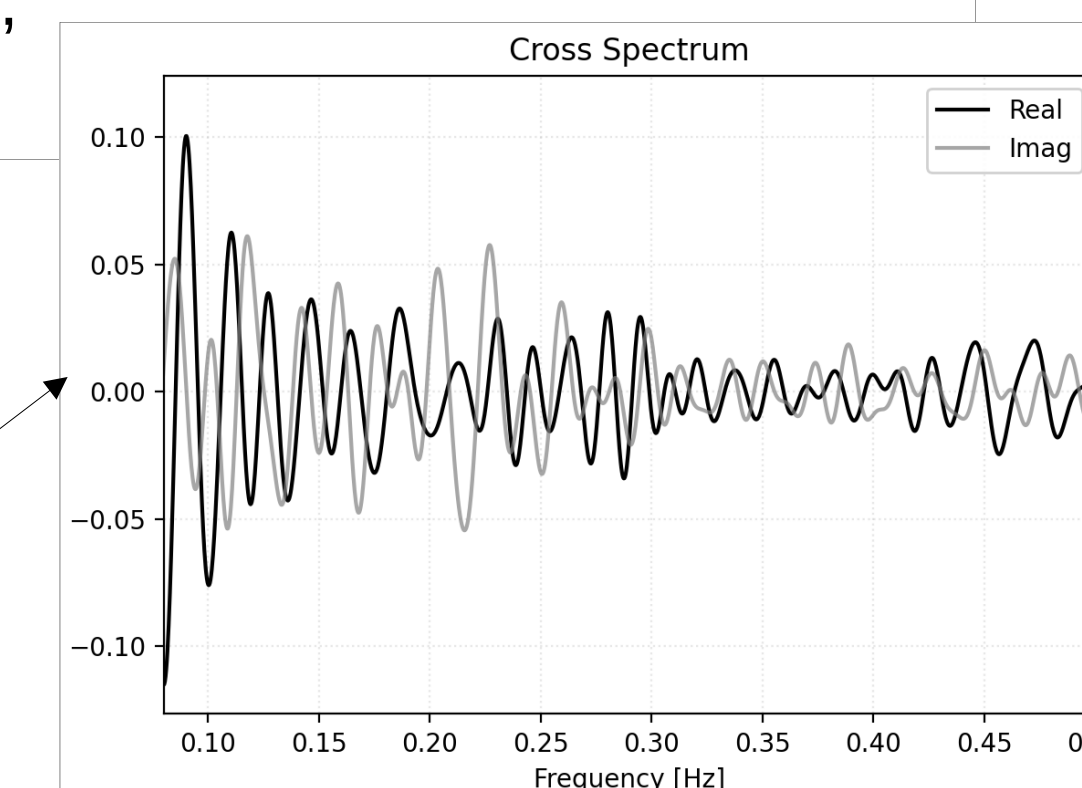
### Basic Pre-Processed waveforms

#### Earthquake Removal

- 2500+ events systematically removed;
- Reduced incoherent signal;
- Enforced diffuse wavefield assumption;
- Stabilized dispersion curve retrieval.

#### Cross-spectrum via Welch's method [Seatz et al., 2012, GJI]

- Improves diffuse wavefields assumption;
- Faster Cross-spectrum convergence;
- Robustness to transient signals;
- Improved statistical stability.



### The inverse problem Regularised Least Square

- Ray-theory approach [Boschi and Dziewoński, 1999, JGR Solid Earth];
- Handles ill-posed problems (e.g.,  $M > D$ );
- Roughness regularization.

## 5. Preliminary results

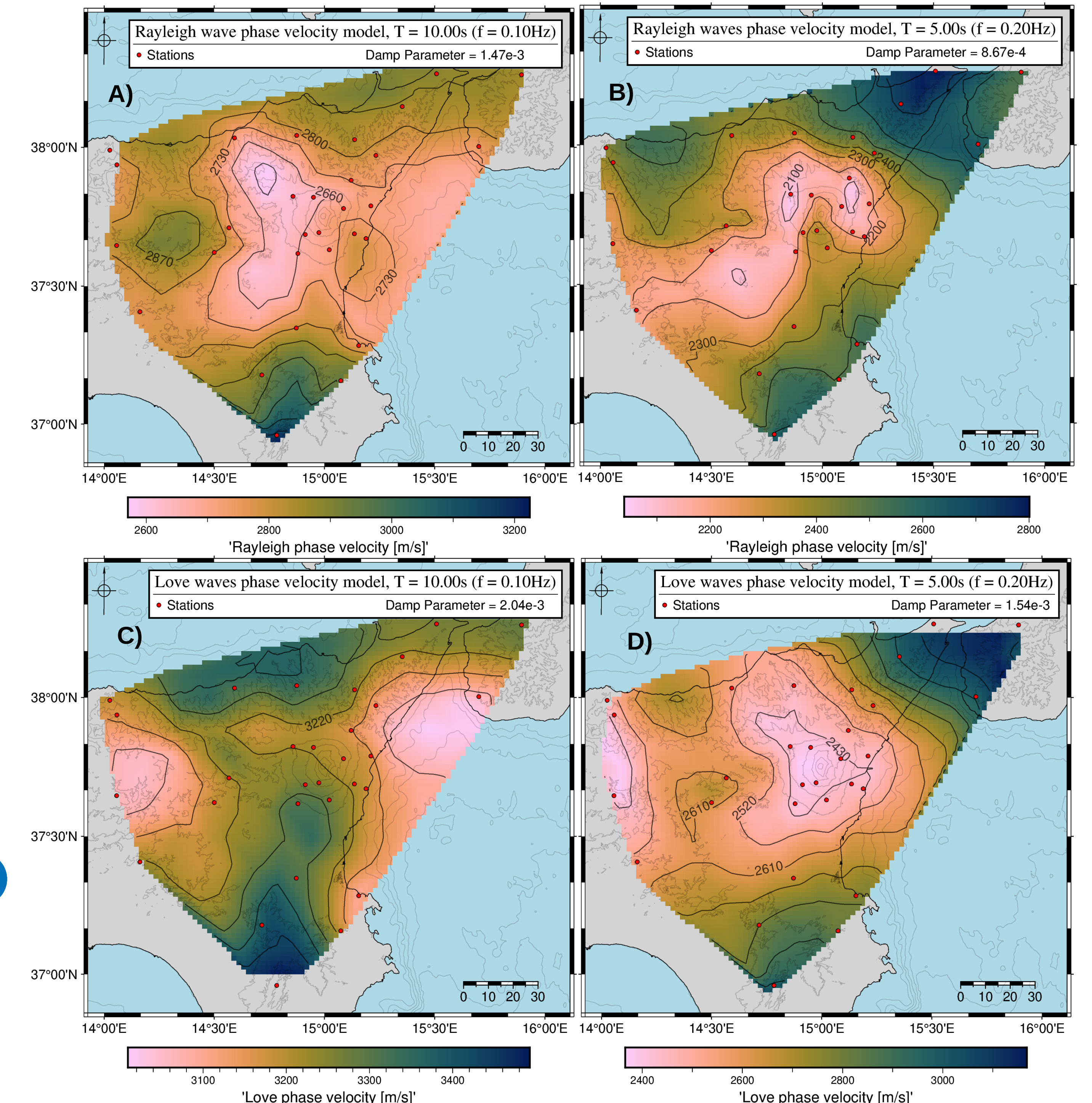


Figure 4: Rayleigh- and Love-wave phase-velocity models of Eastern Sicily obtained through inversion of interstation phase velocities derived from dispersion curves at selected frequencies using SeisLib.

## 6. Preliminary conclusions (pending Bayesian inversion)

- West and beneath Mt. Etna: low Rayleigh-wave velocity anomaly down to  $\sim 25$  km;
- Shallow Etna: potential high-velocity body [Lo Bue et al., 2024, GRL];
- Hyblean Plateau: high-velocity, rigid/cool crust;
- East Etna: low Love and Rayleigh wave velocities;
- Madonie/Nebrodi: low Love and Rayleigh wave velocities, possibly fractured medium.

## 7. Future works

### Bayesian Inversion (BayesBay [Magrini et al., 2025, SRL])

- **Joint Rayleigh-Love inversion:** estimation of  $V_s$  and radial anisotropy models:
  - Bias-free and data driven trans-dimensional Bayesian MCMC;
  - Uncertainty estimates based on ambient-noise power anisotropy.
- **Petroseismical framework inversion:**
  - Coupling MAGEMin [Riel et al., 2022, G<sup>3</sup>] petrological modelling with the BayesBay framework.

Wind rose and maps are generated with PyGMT (Tian et al., 2026, Zenodo, v0.18.0)