

# Tectonic Reorganizations and Multistability of the Mantle-Plate System

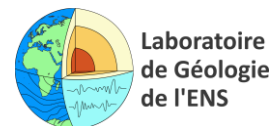
Ilyas Jaah<sup>1</sup>, Nicolas Coltice<sup>1</sup>, Alexandre Janin<sup>2,3</sup>, Nicolas Flament<sup>4</sup>

<sup>1</sup>Géoazur, Université Côte d'Azur, Nice, France

<sup>2</sup>Laboratoire de Géologie–CNRS UMR 8538, École normale supérieure–PSL University, Paris, France

<sup>3</sup>Department of Earth and Environmental Sciences, Boston College, Chestnut Hill, MA, USA

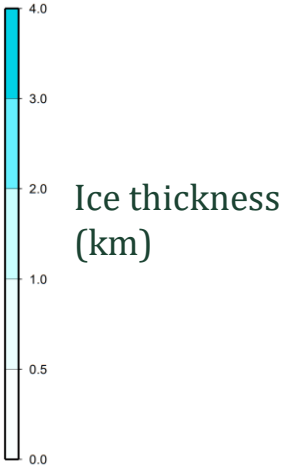
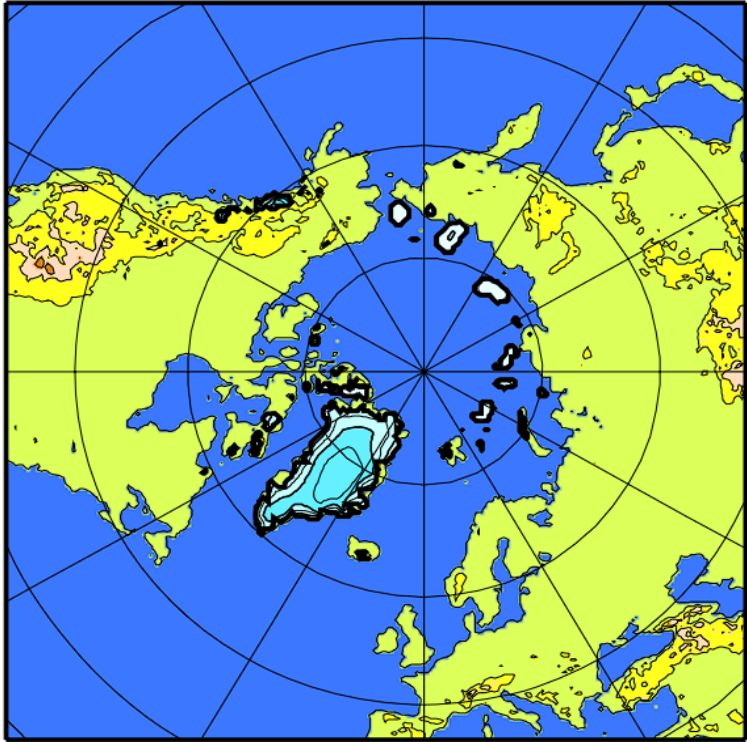
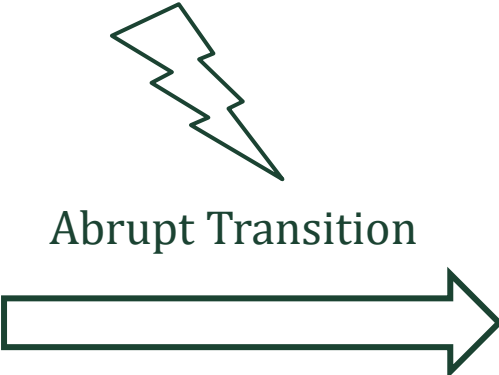
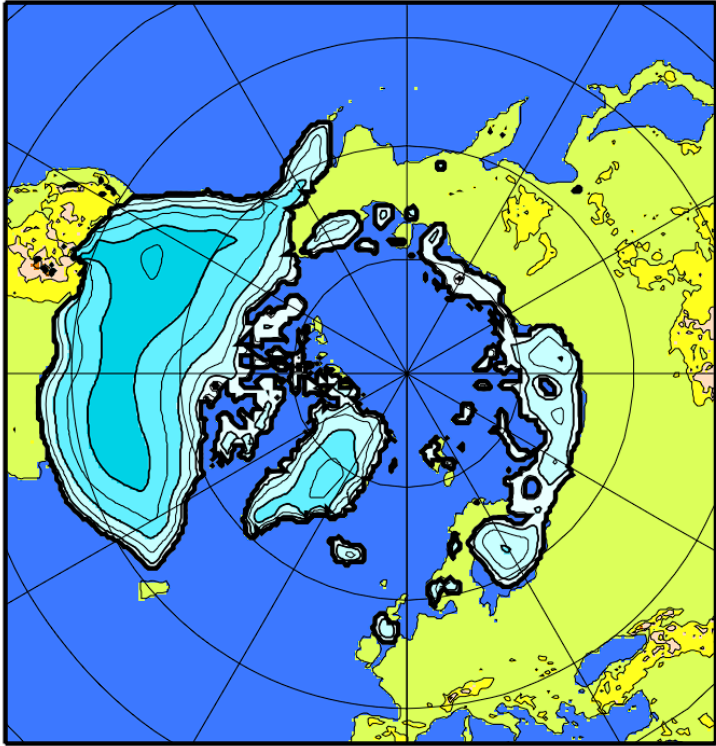
<sup>4</sup>School of Environmental Futures, School of Science, University of Wollongong, Northfields Avenue, NSW 2522, Australia



# The Climate, a Multistable System

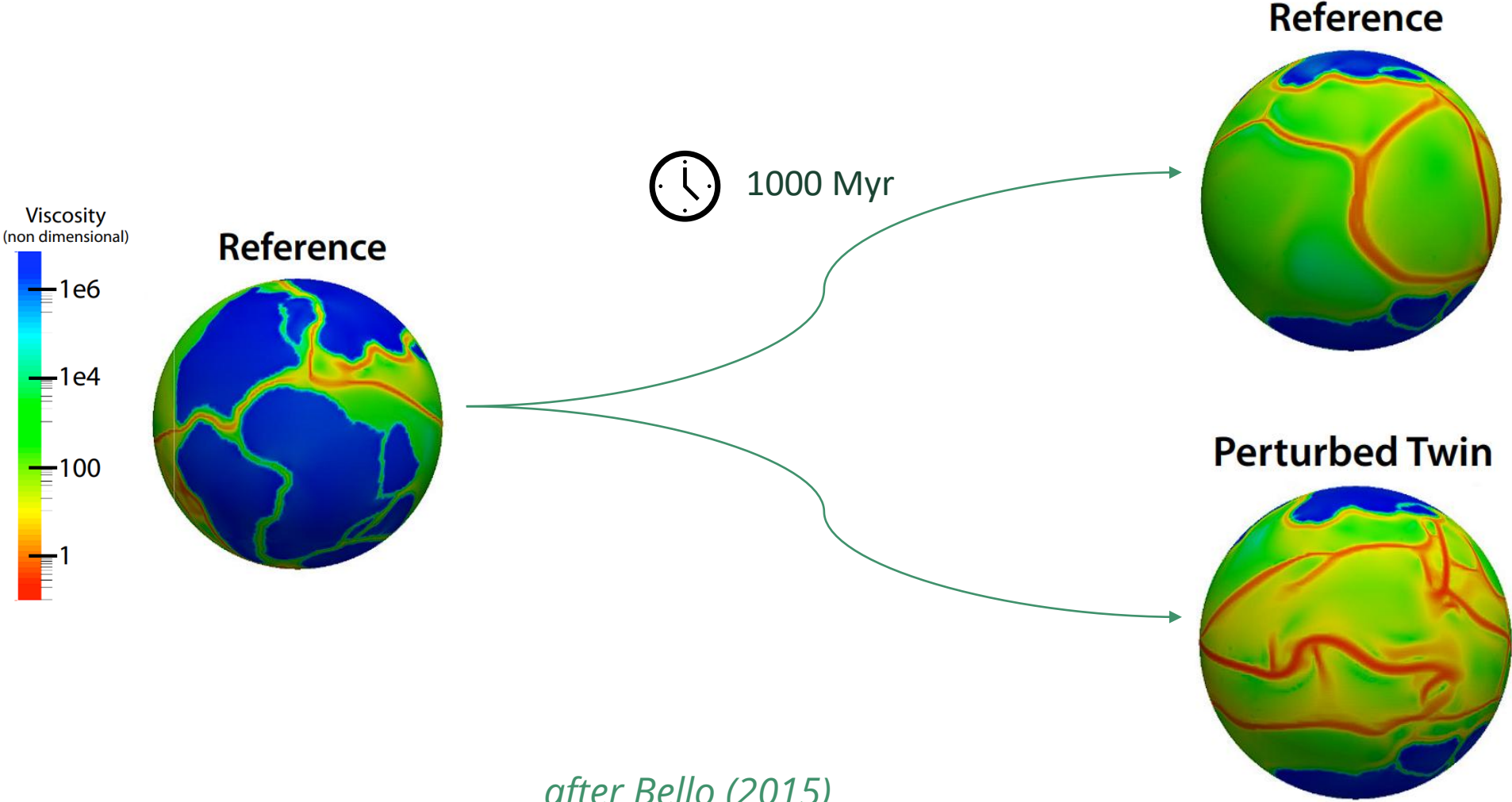
57 kyr BP

Present day



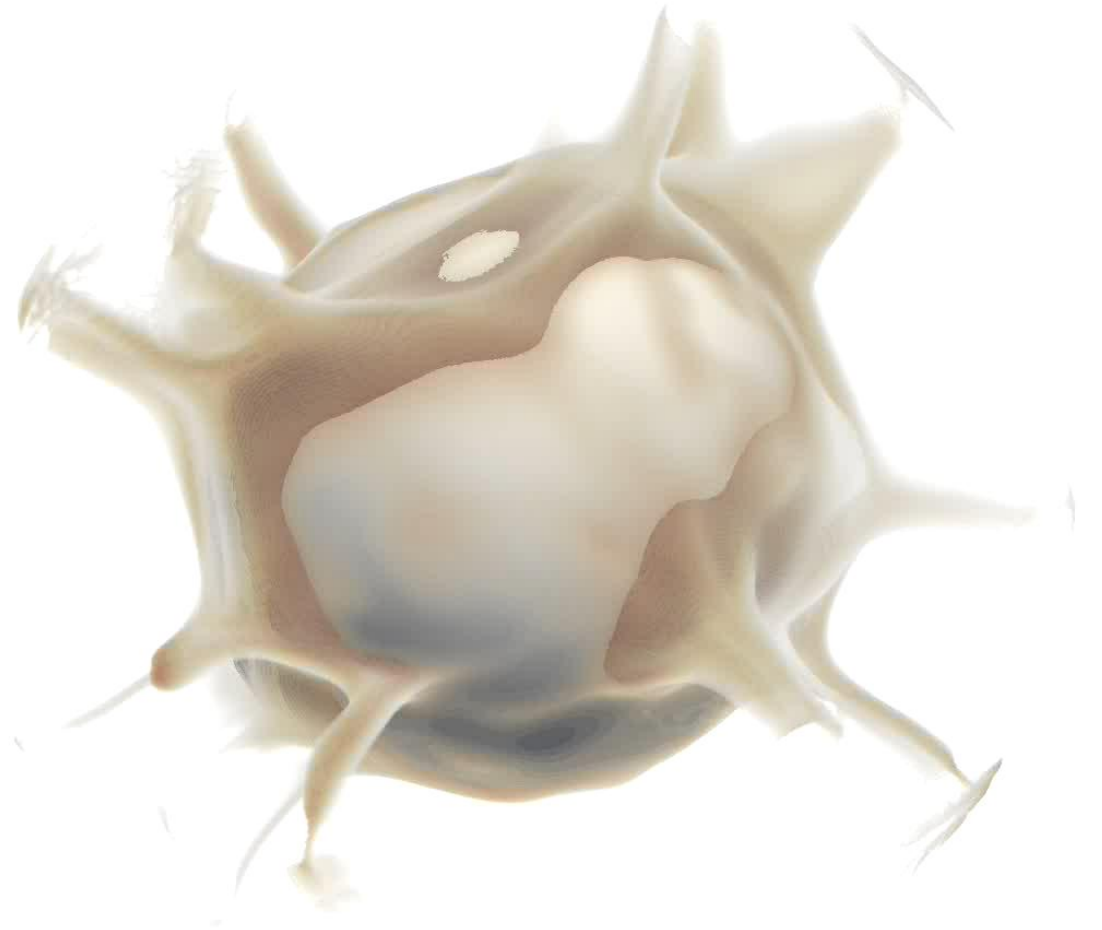
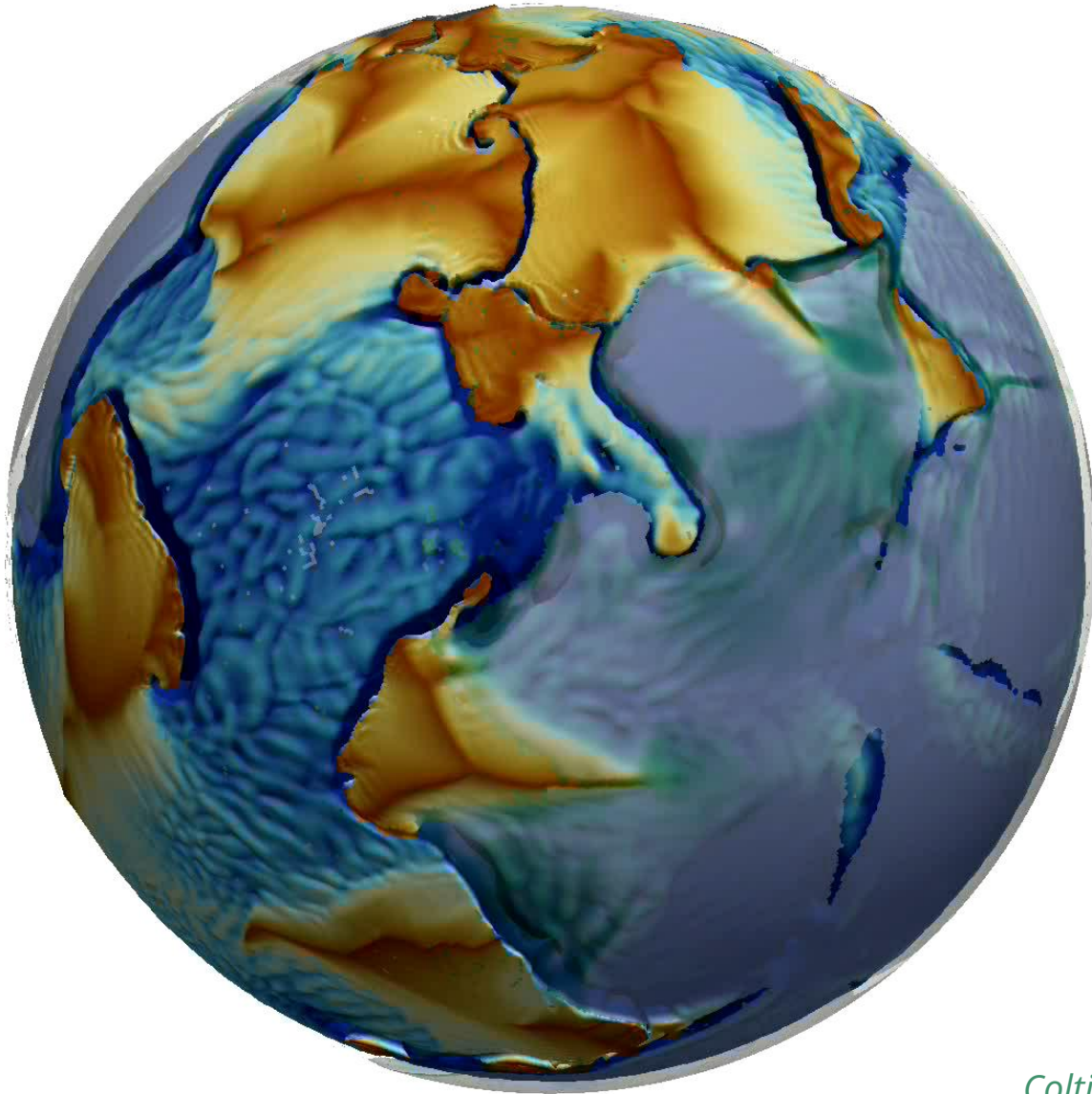
*Charbit et al., 2007*

# Mantle Convection is a Chaotic System



*after Bello (2015)*

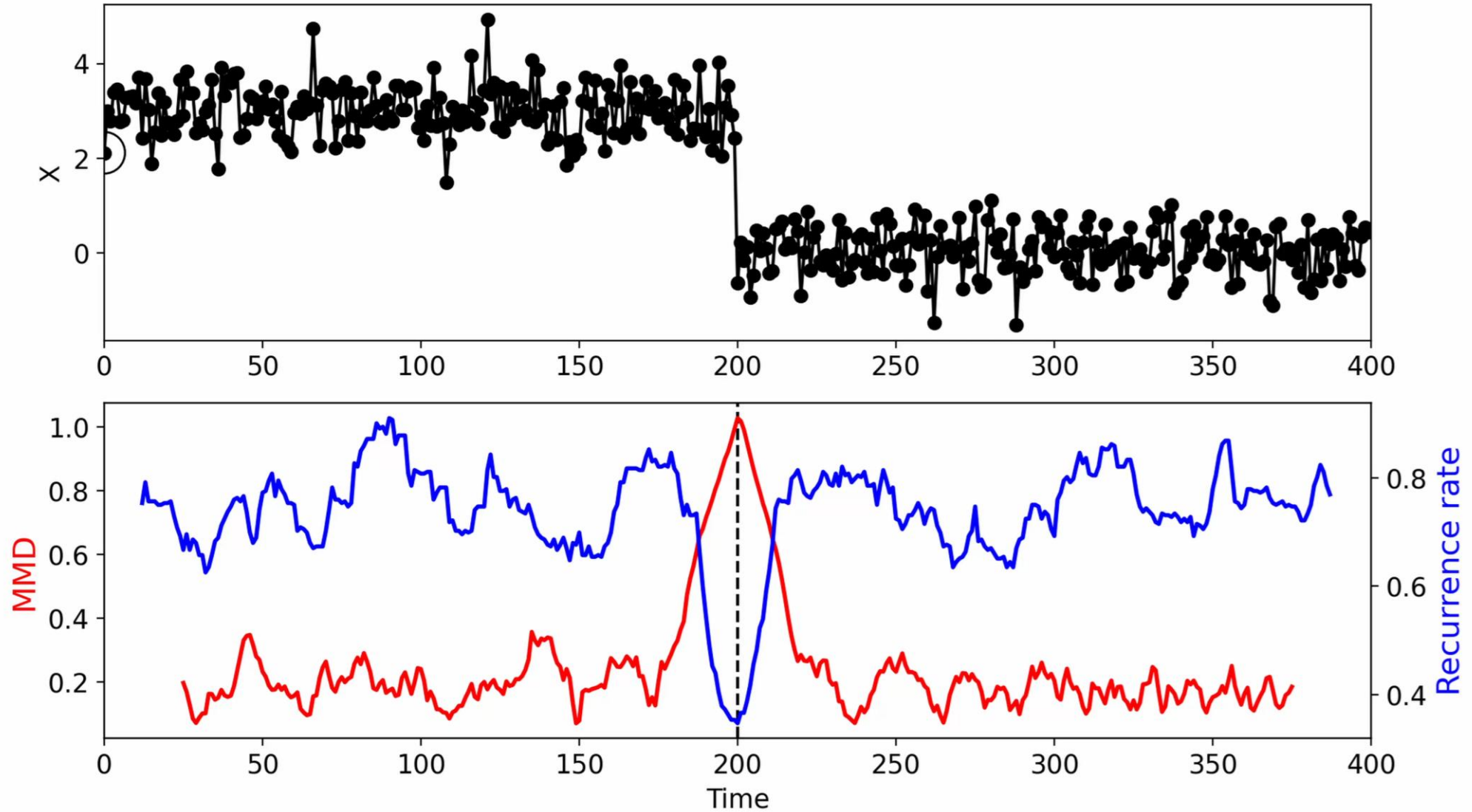
# Earth-like mantle convection model



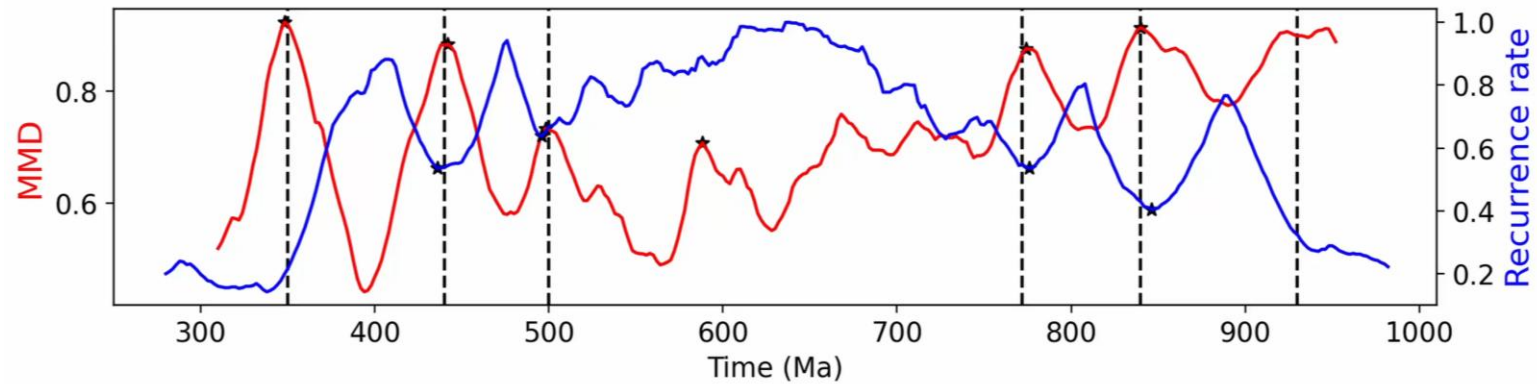
*Coltice et al. (2019)*

# Transition Identification

MMD and RR for synthetic data at time = 0

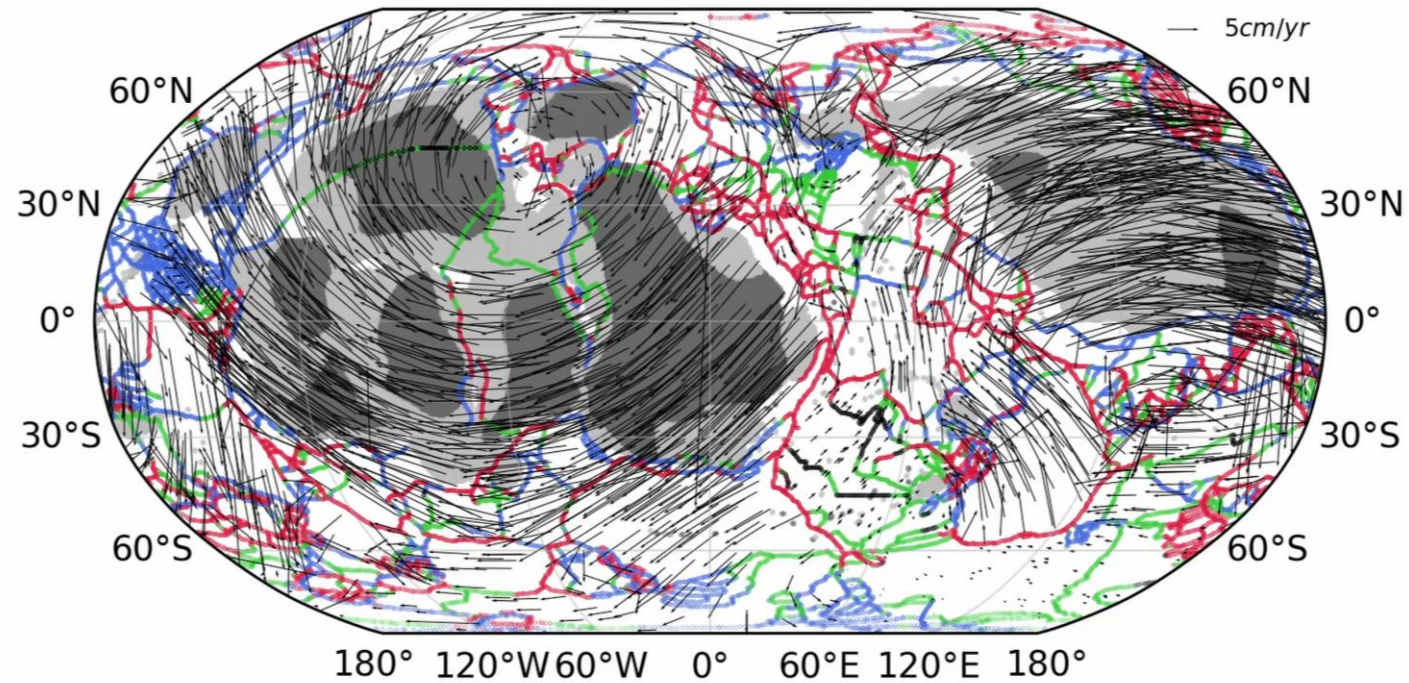


# Geodynamic Abrupt Transitions



Time: 250 Ma

180° 120°W 60°W 0° 60°E 120°E 180°



# Tectonic Reorganizations and Multistability of the Mantle-Plate System

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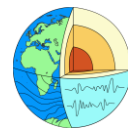
<sup>4</sup>School of Environmental Futures, School of Science, University of Wollongong, Northfields Avenue, NSW 2522, Australia



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de l'ENS



# Tectonic Reorganizations and Multistability of the Mantle-Plate System



European Research Council  
Established by the European Commission



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Why ?

How ?

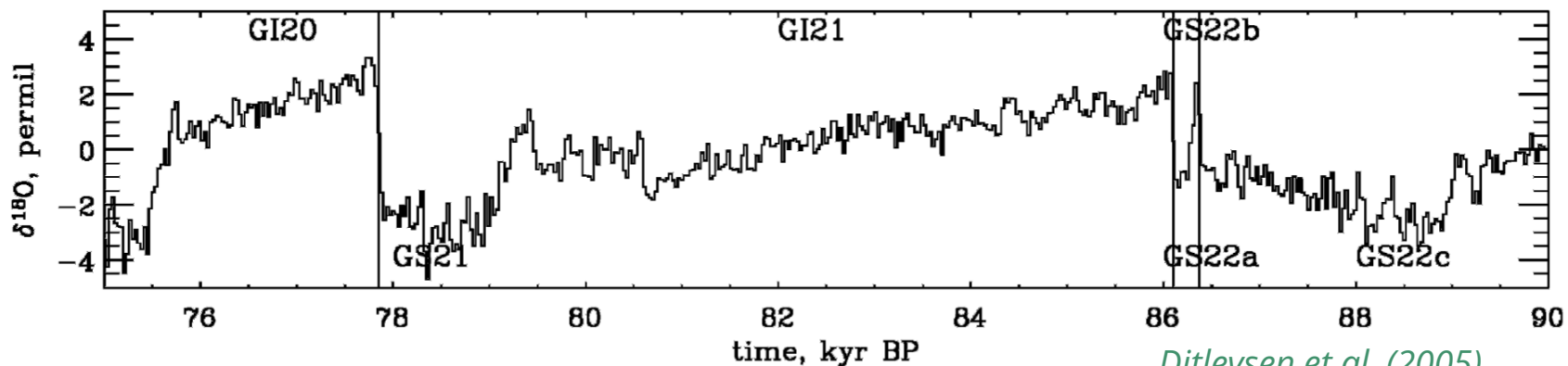
Results

Summary

# Background

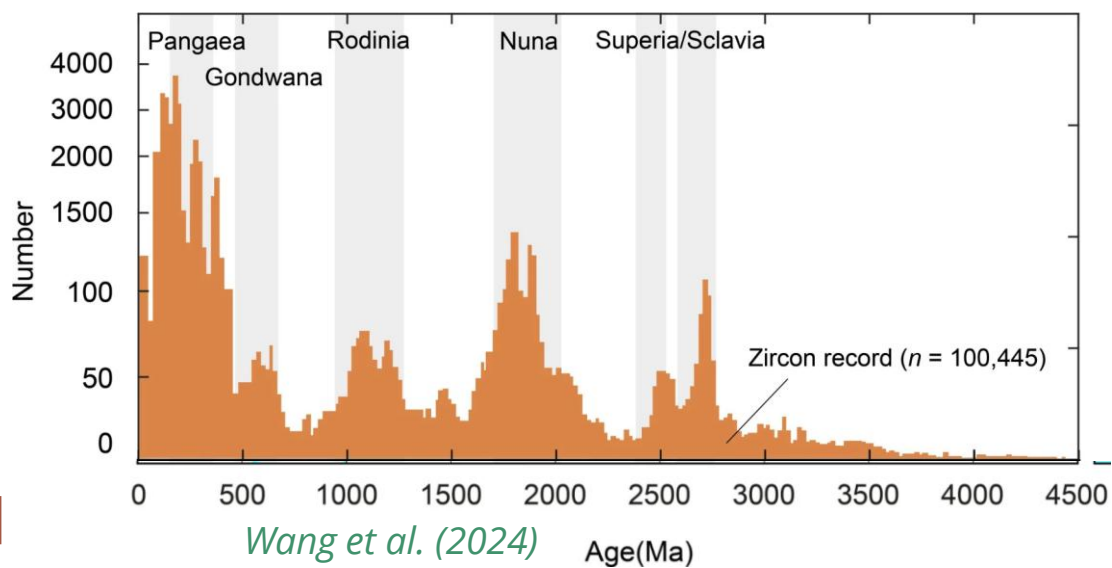


$\delta^{18}\text{O}$  record from ice cores from the GRIP



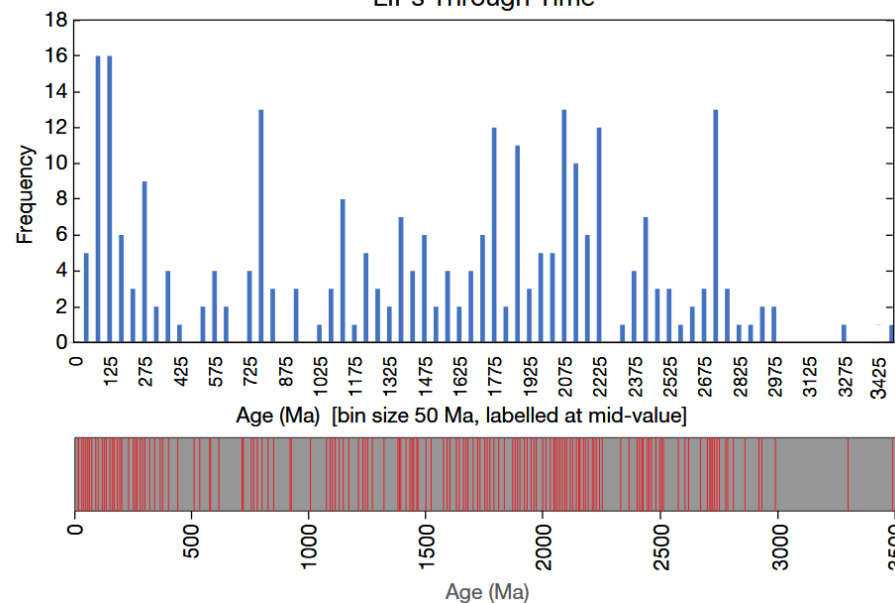
*Ditlevsen et al. (2005)*

Age frequency distribution of detrital zircons



*Wang et al. (2024)*

LIPs Through Time



Age (Ma)

*Ernst (2021)*

# Questions

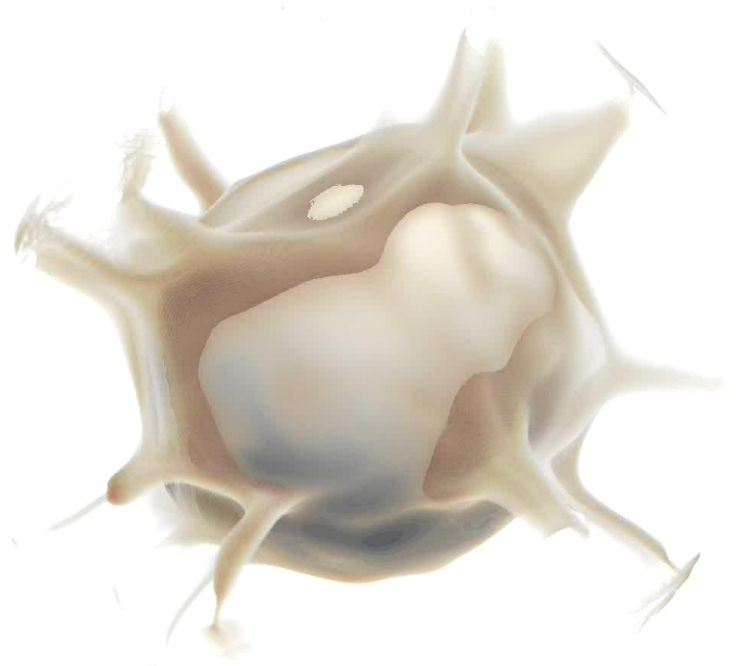
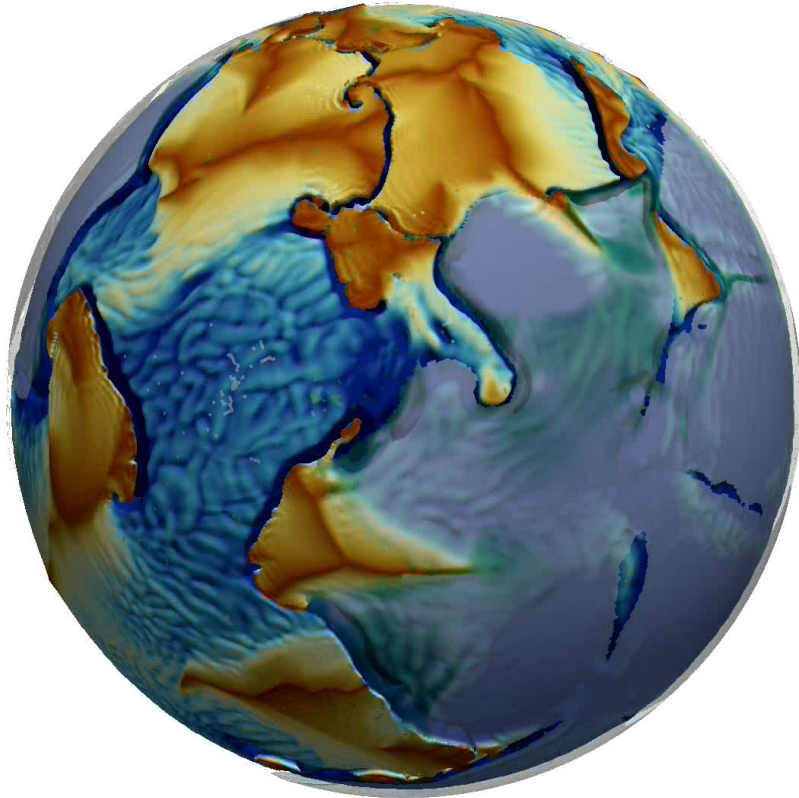
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- **Can we detect abrupt transitions between different states of mantle convection and plate tectonics ?**
- **Does these changes concern the lithosphere or the whole mantle ?**
- **Are tectonic changes fluctuations or global changes in dynamics ?**



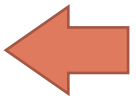
# Model and Data Extraction



- Data extracted from Coltice et al. (2019)
- Mantle convection model with non-linear rheology producing plate-like behaviour
- Reproduces major features of Earth's tectonics



*Coltice et al. (2019)*



# Detection of tectonic plates and boundaries



Magnitude of  
Velocity gradient



- Topological analysis of the magnitude of the velocity gradient
- Equivalent to watershed decomposition

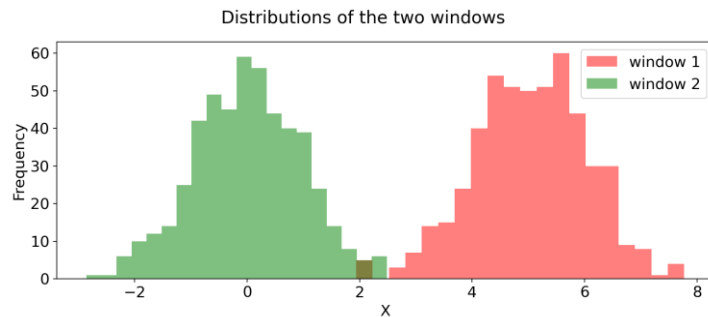
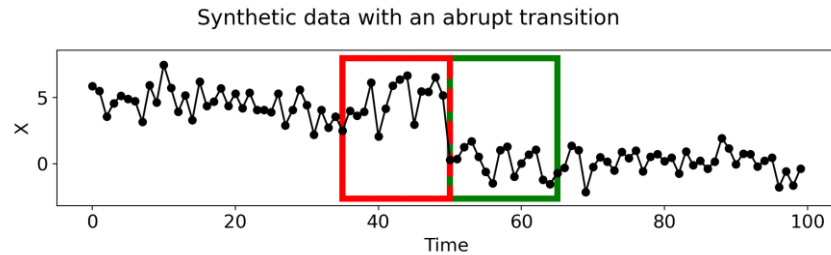
*Janin et al. (2025)*



# Transition Detection



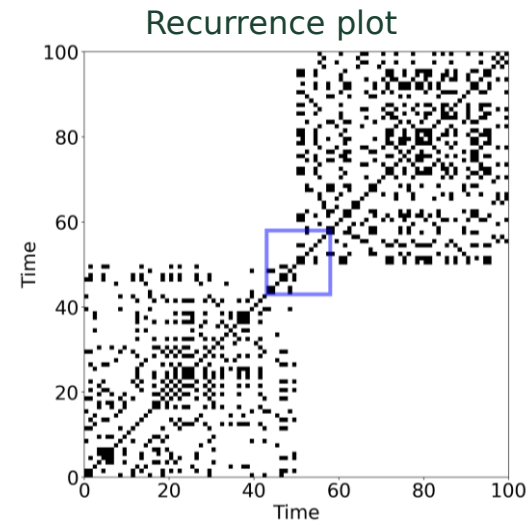
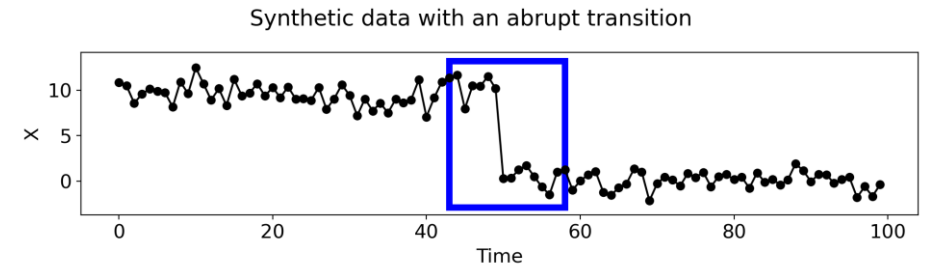
## Maximum Mean Discrepancy : Distances between distribution



$$MMD^2(X, Y) = \frac{1}{m(m-1)} \sum_i \sum_{j \neq i} k(\mathbf{x}_i, \mathbf{x}_j) - 2 \frac{1}{m \cdot m} \sum_i \sum_j k(\mathbf{x}_i, \mathbf{y}_j) + \frac{1}{m(m-1)} \sum_i \sum_{j \neq i} k(\mathbf{y}_i, \mathbf{y}_j)$$

$$k(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(\frac{-\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2}\right)$$

## Recurrence Rate : Recurrence in the variables



$$R(i, j) = \begin{cases} 1 & \text{if } \|\vec{x}(i) - \vec{x}(j)\| \leq \varepsilon \\ 0 & \text{otherwise,} \end{cases}$$

$$RR = \frac{1}{N^2} \sum_{i,j=1}^N R(i, j).$$

→ Transitions should correspond to MMD maxima

→ Transitions should correspond to RR minima

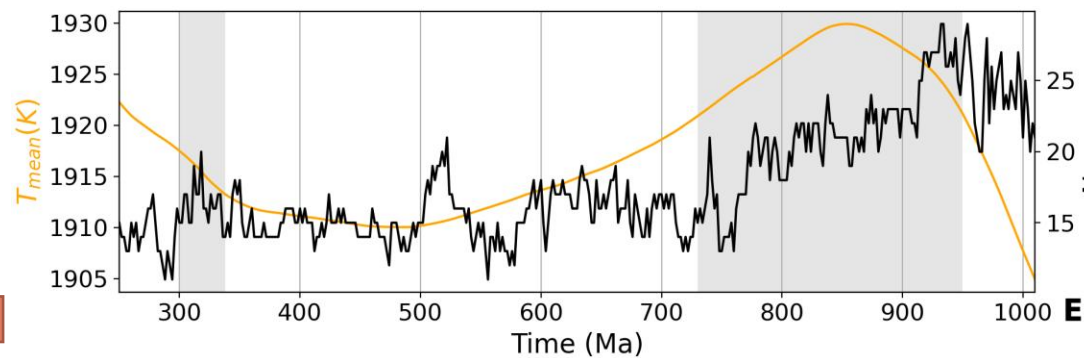
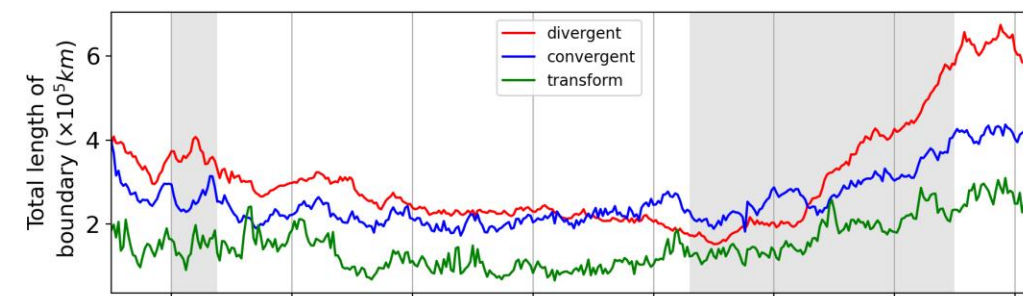
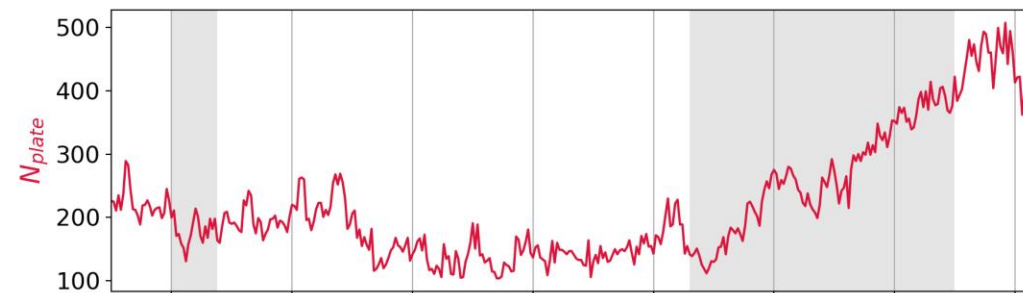


# Dataset



Rapid continental motion

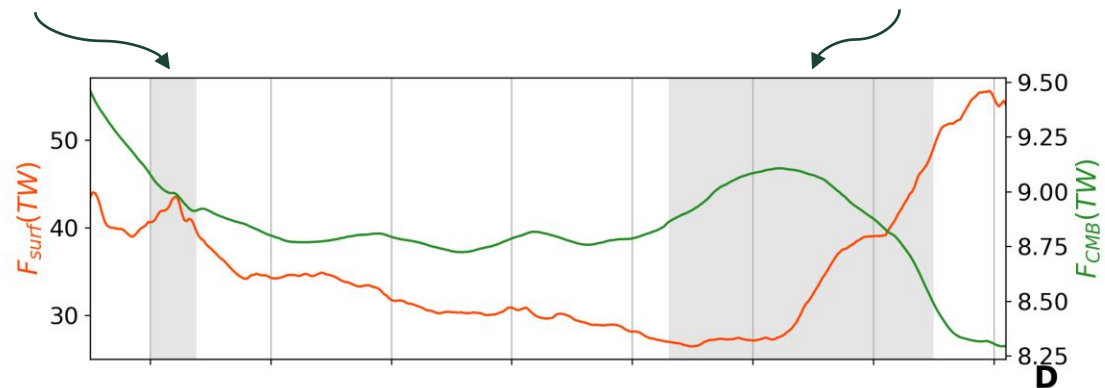
Supercontinent



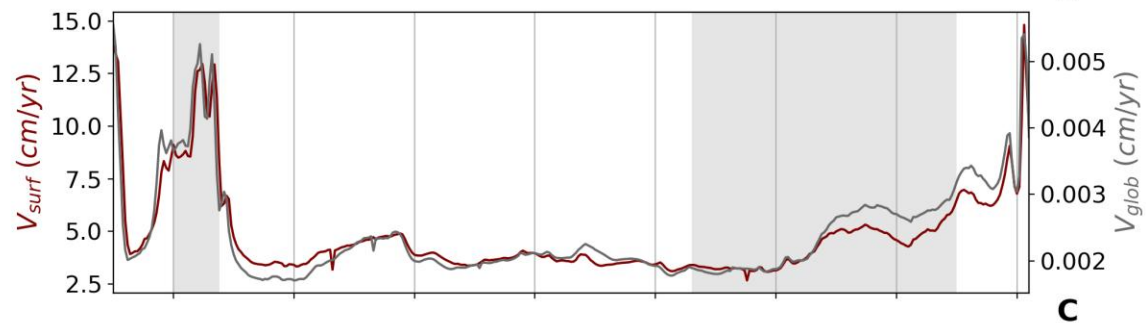
**A**

**B**

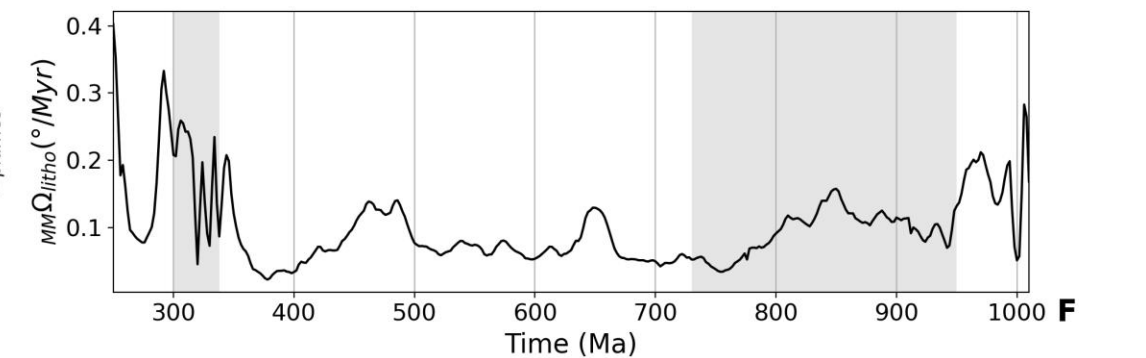
**E**



**D**



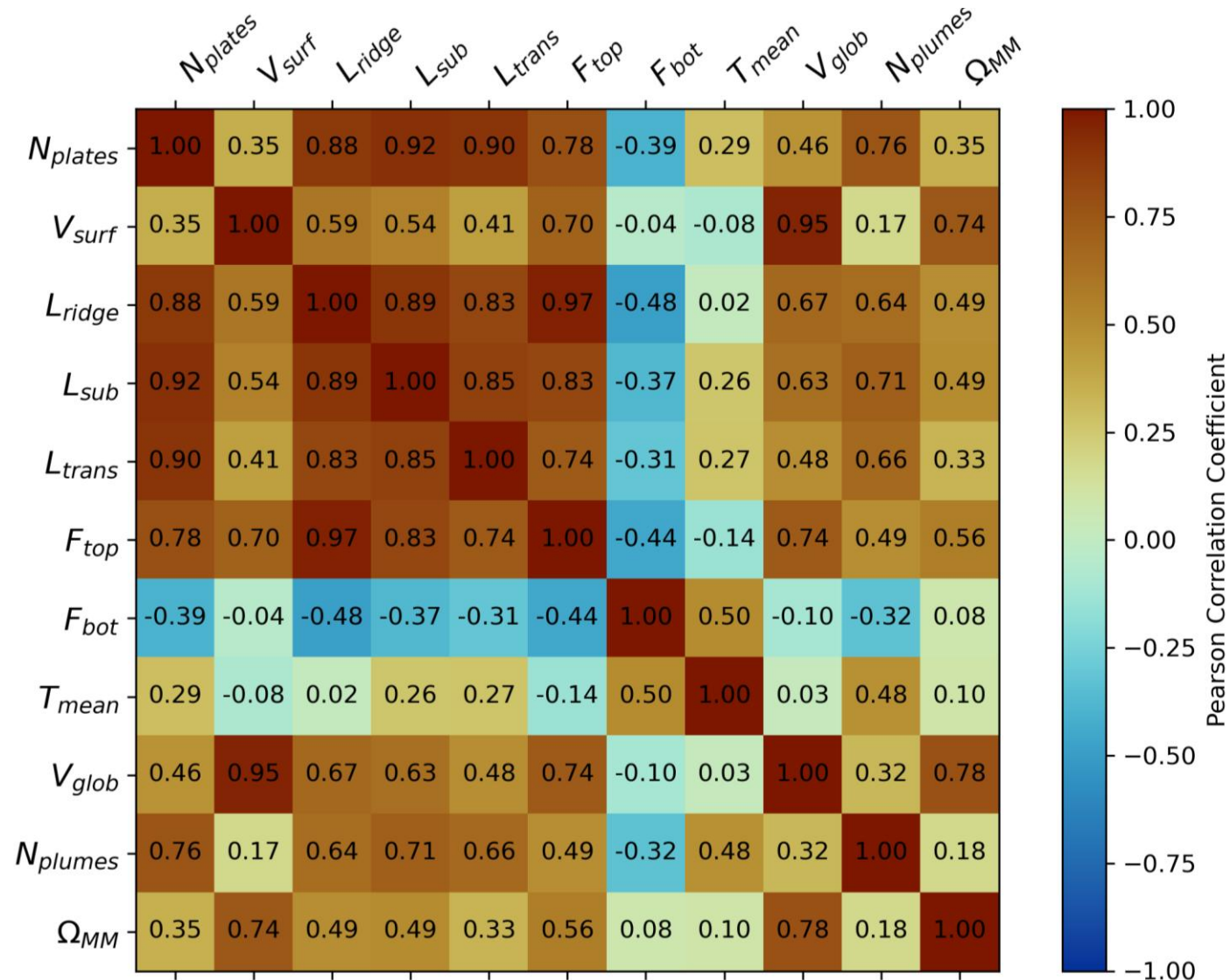
**C**



**F**

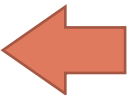


# Correlations



- Surface variables are highly correlated, except for velocity
- LNR correlated mostly correlated with velocity

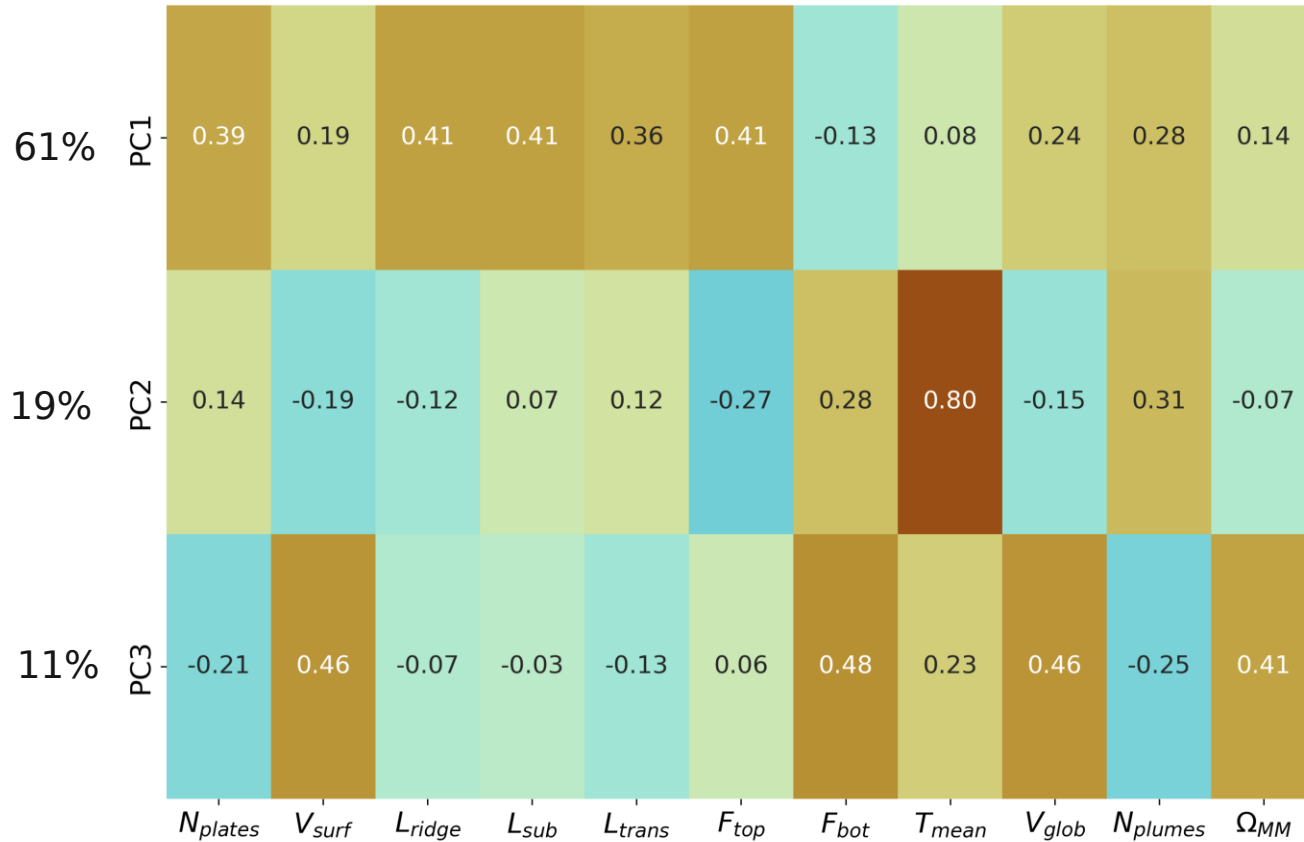
→ Difficult to get information on mantle variables like the temperature of the mantle from surface variables



# Principal Components



Explained variance



First 3 PC represent ~90% of variance of dataset

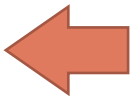


→ Surface/fragmentation

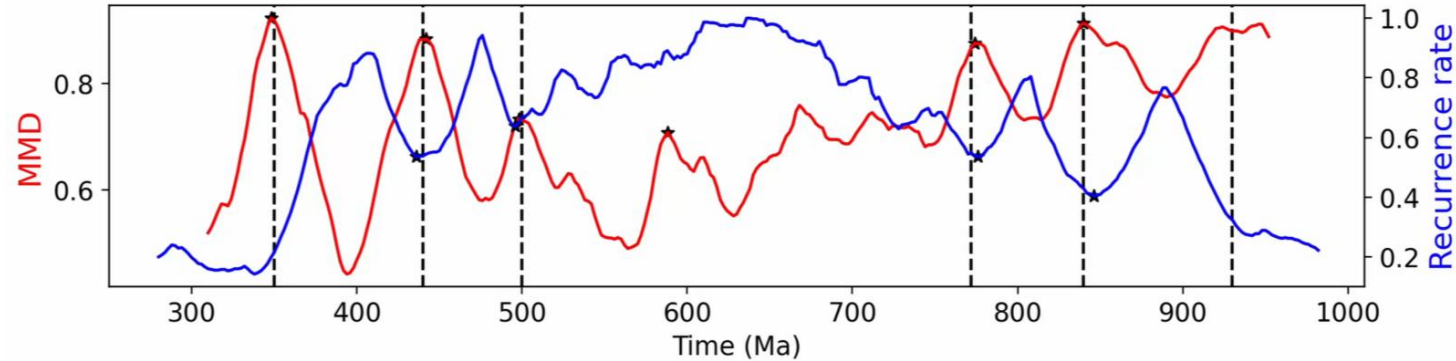
→ Mantle Temperature

→ Kinematics

→ Again, difficult to get information on mantle variables like the temperature of the mantle from surface variables

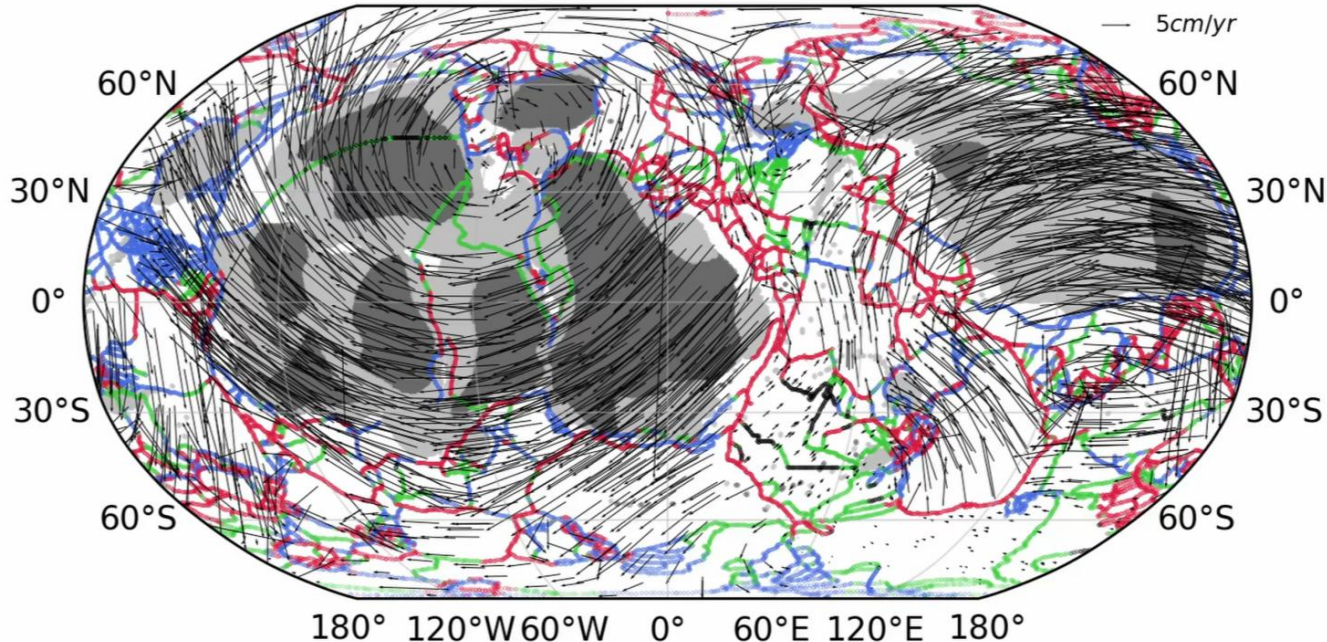


# Identified Transitions

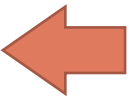


Time: 250 Ma

180° 120°W 60°W 0° 60°E 120°E 180°



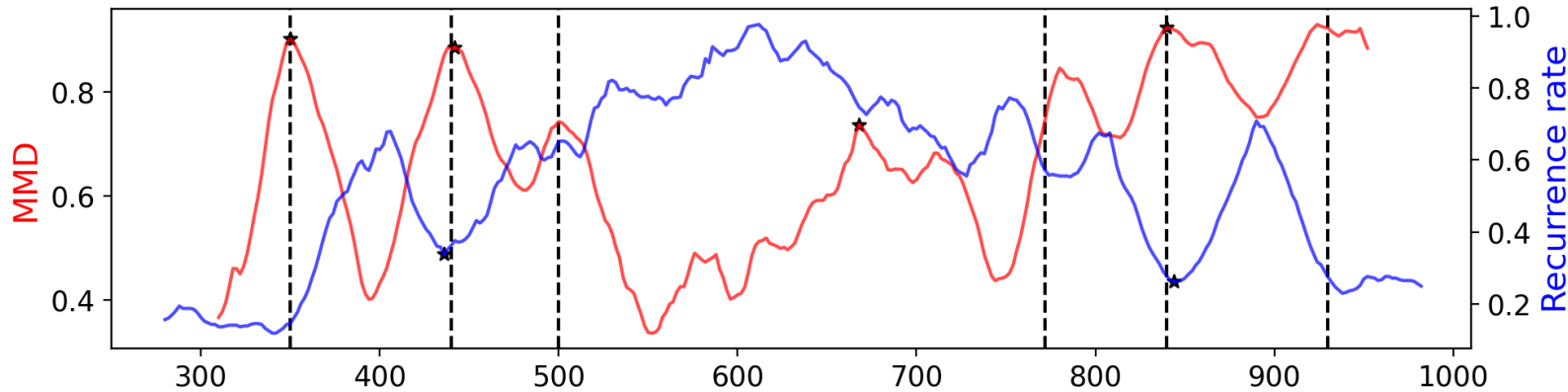
- 6 transitions over 760 Myr
- Transitions are synchronous with major events like tectonic reorganisations or supercontinent breakup
- Continental breakups are associated to abrupt transitions, not continental collisions



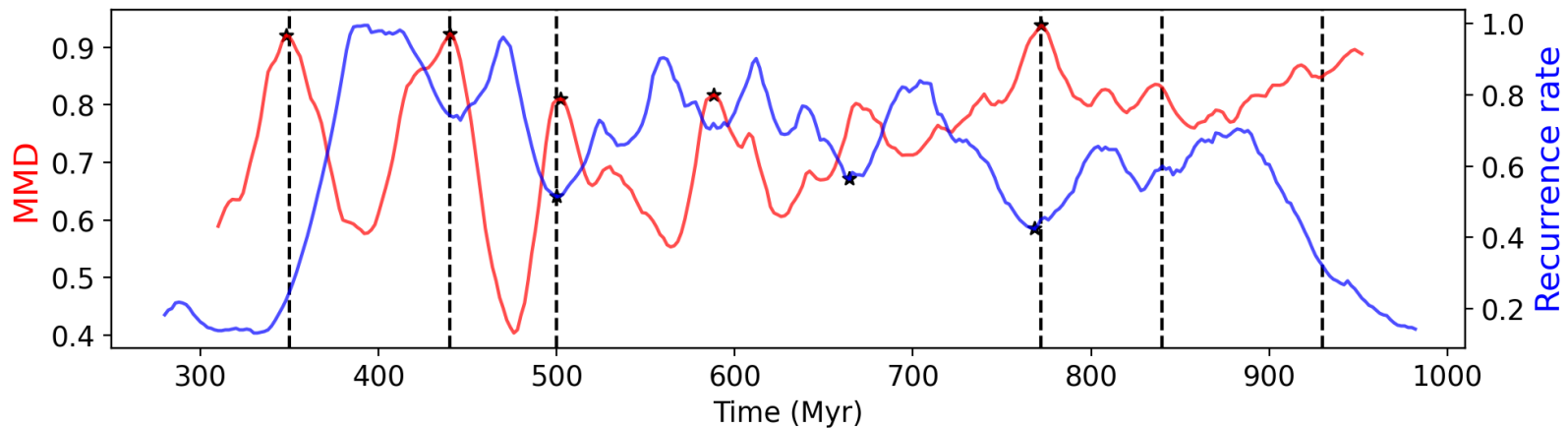
# Some Transitions concern the whole model, some only the surface



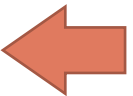
Surface Data



Mantle data



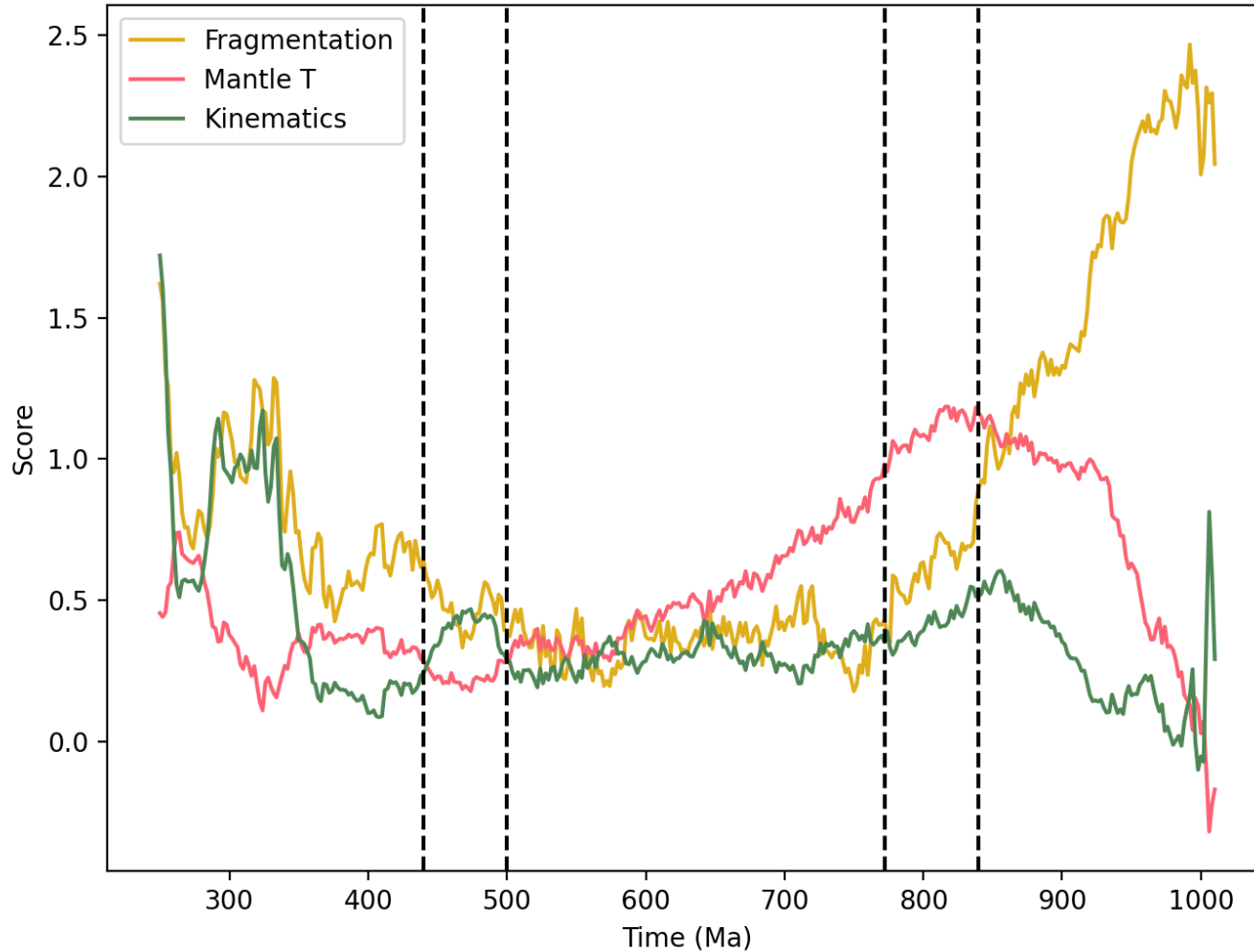
- 1 transition is not identified in the mantle
- Breakups are always identified for both dataset



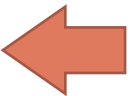
# Principal Components Space



Projection of dataset in space of first 3 principal components



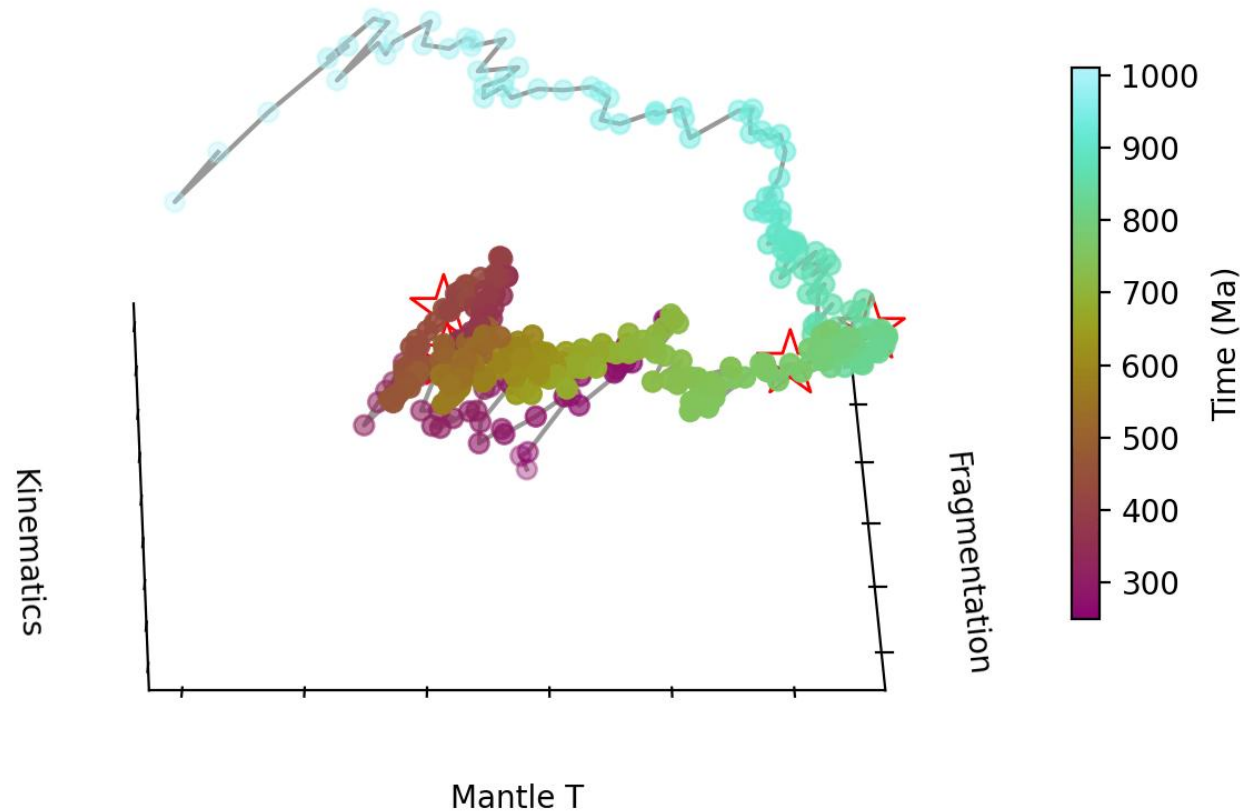
- Transitions are associated with shifts in one or more PC
- Transitions are changes in fragmentation and/or mantle T and/or kinematics of the system



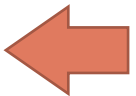
# Principal Components Space



Data in space of 3 first PCs



- Analogous to phase space
- No orbit, one potentially stable region
- Suggests that transitions are not fluctuations but fluctuations on longer timescales could exist
- Most transitions occur outside of 'stable' zone



# Summary

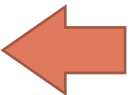


We extracted global geodynamic data from an Earth-like mantle convection model and detected several abrupt transitions for this model

For the Earth :

- Hard to get information from the mantle temperature from kinematics and fragmentation
- Rapid transitions exist, they are characterized by changes in fragmentation and/or mantle T and/or kinematics
- Breakups are associated with abrupt transitions, not collisions
- Those transitions are either shifts from a distinct convective state to another or fluctuations on very long timescales

Any questions ? Contact me : [Ilyas.Jaah@geoazur.unice.fr](mailto:Ilyas.Jaah@geoazur.unice.fr)



# Methods : Model details



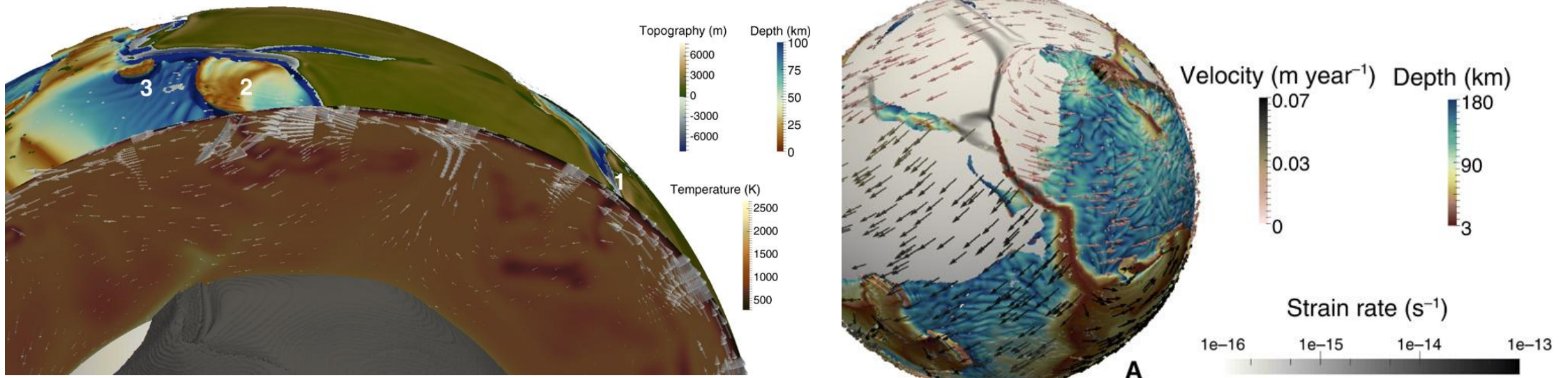
Code StagYY

Free-slip top and bottom boundaries

Lateral viscosity variation

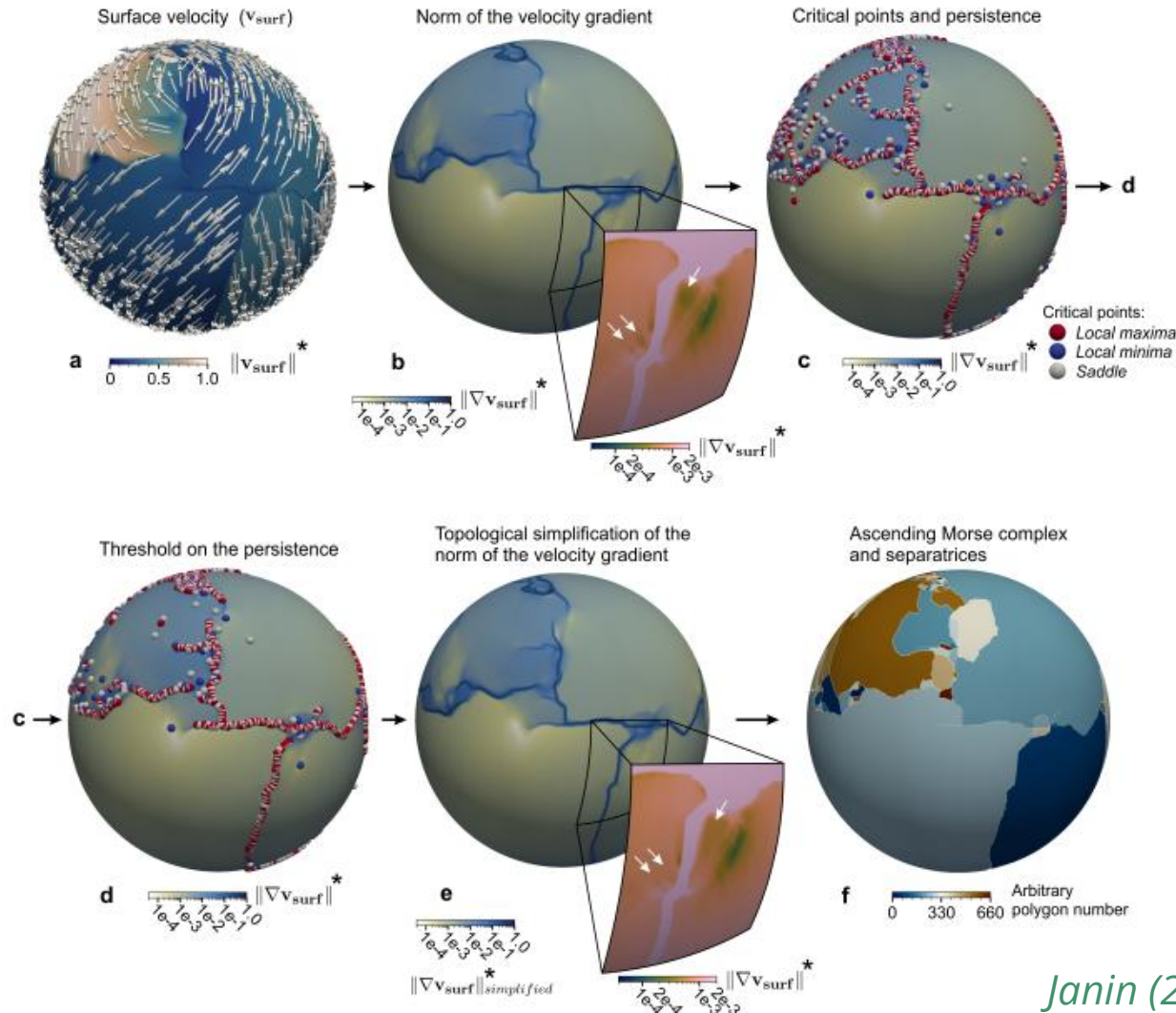
Chemical heterogeneities : Continents (less dense, more viscous) and LLSVP (denser, more viscous)

Initial condition : we fix the continents and solve the flow for the rest of the model until steady-state, then the model starts



*Coltice et al., (2019)*

# Methods : Tessellation

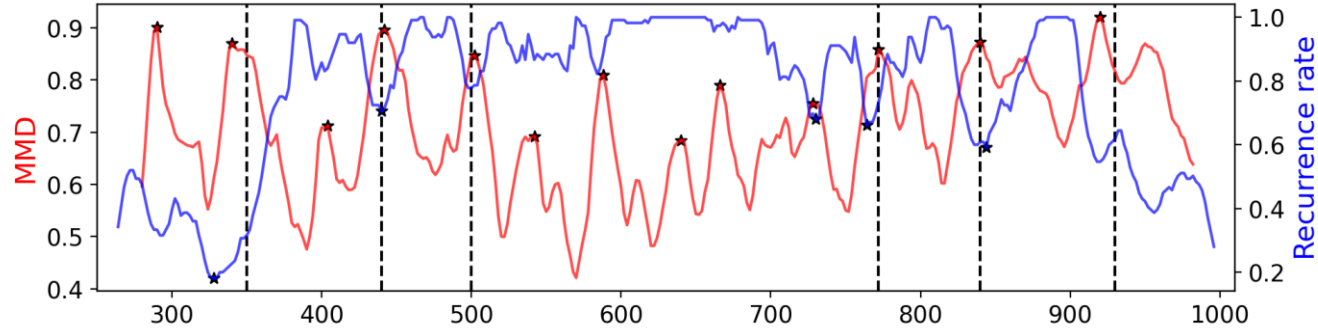


- Developed by Alexandre Janin
- Analysis of norm of velocity gradient
- Computation of critical points and persistence  
~significance of critical points
- Threshold on persistence
- Computation of ascending Morse complex  
~equivalent to watershed decomposition

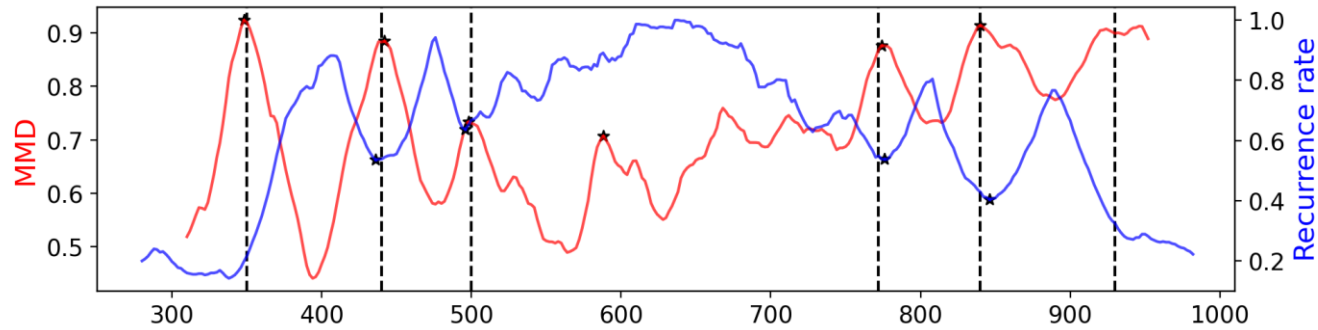
Janin (2022)



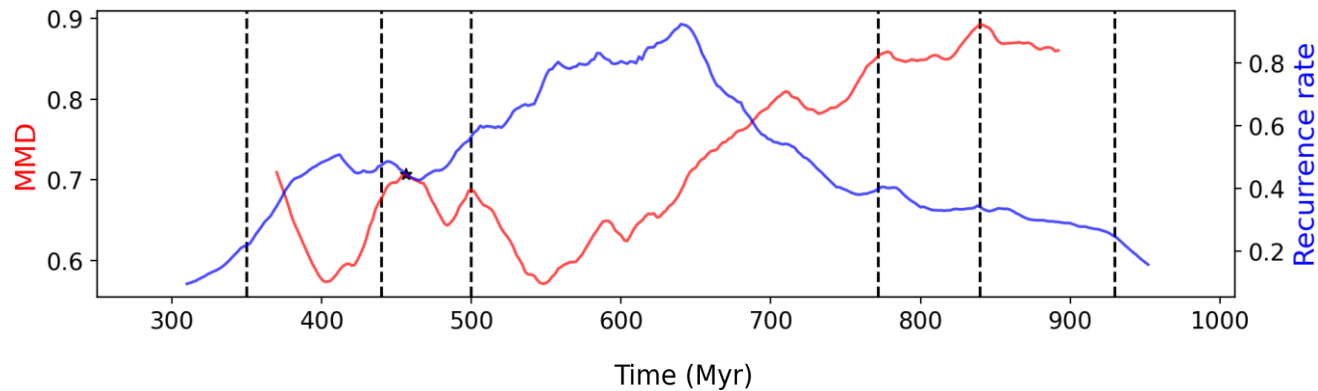
# Impact of window size on MMD and RR



W = 30Myr, 15 points



W = 60Myr, 30 points



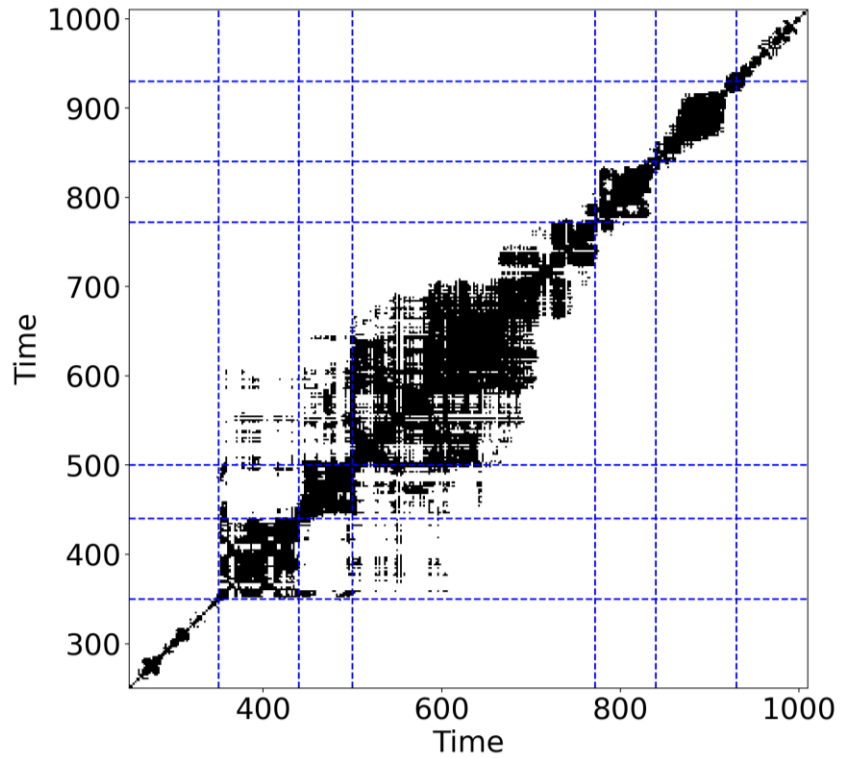
W = 120Myr, 60 points



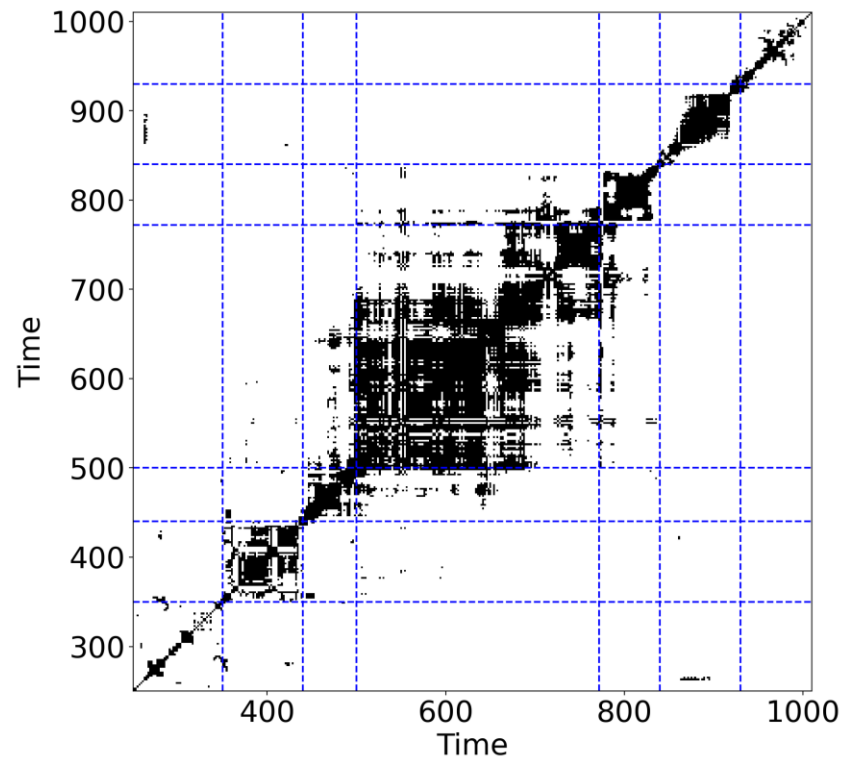
# Recurrence Plots of the Dataset



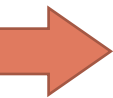
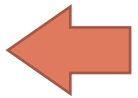
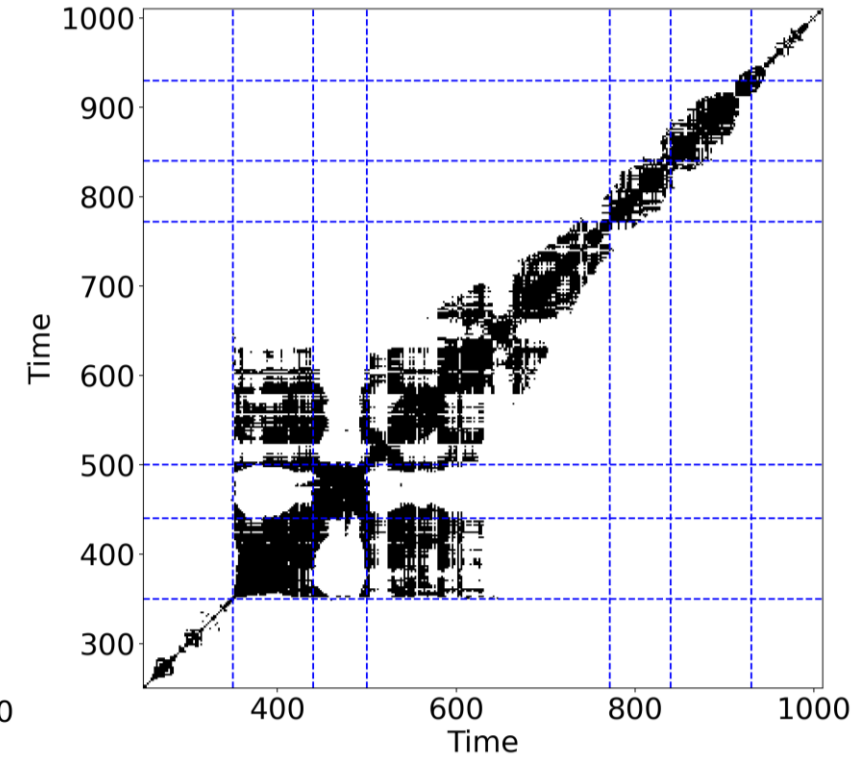
Recurrence plot for all the data



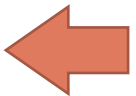
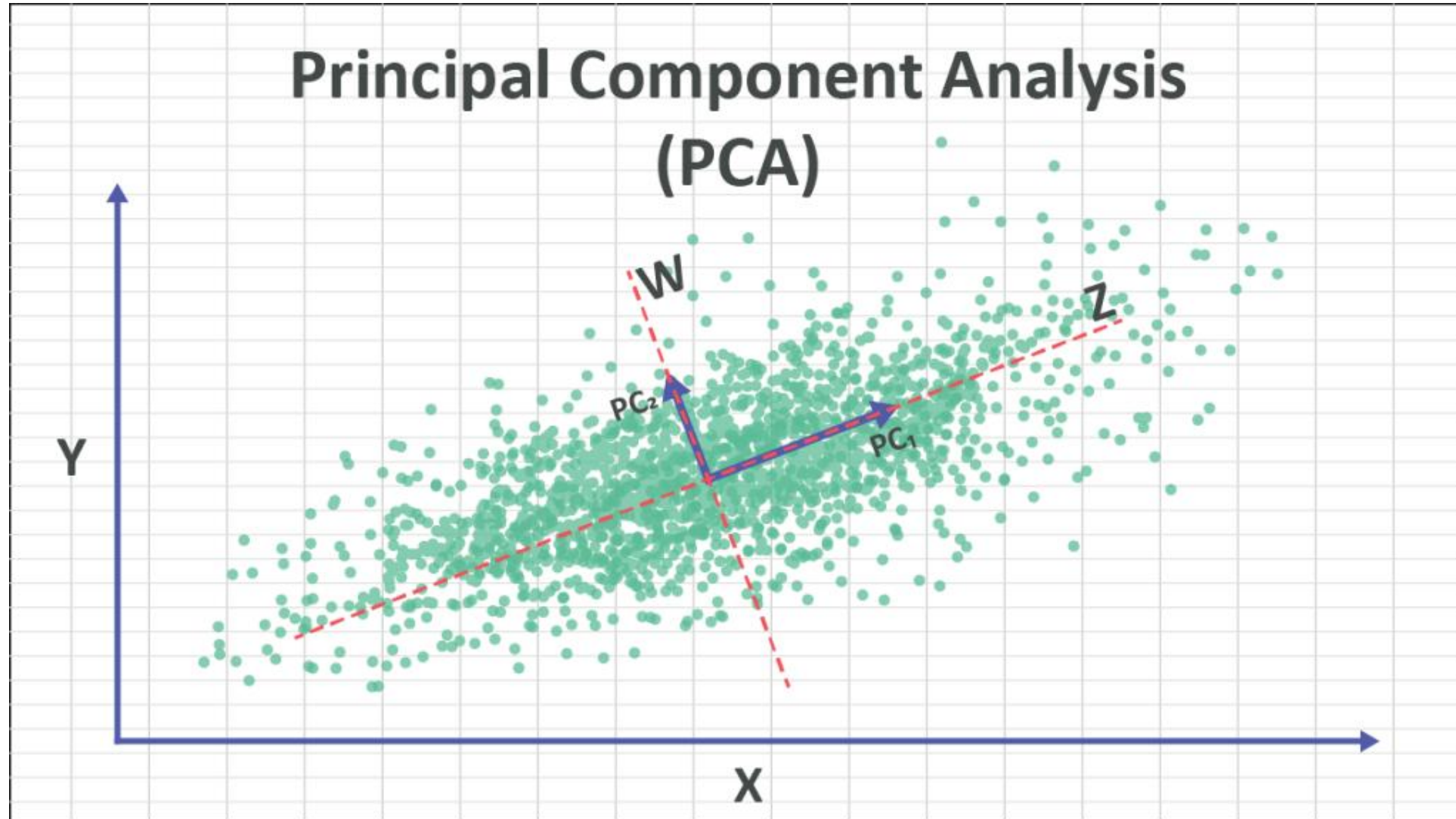
Recurrence plot for the surface



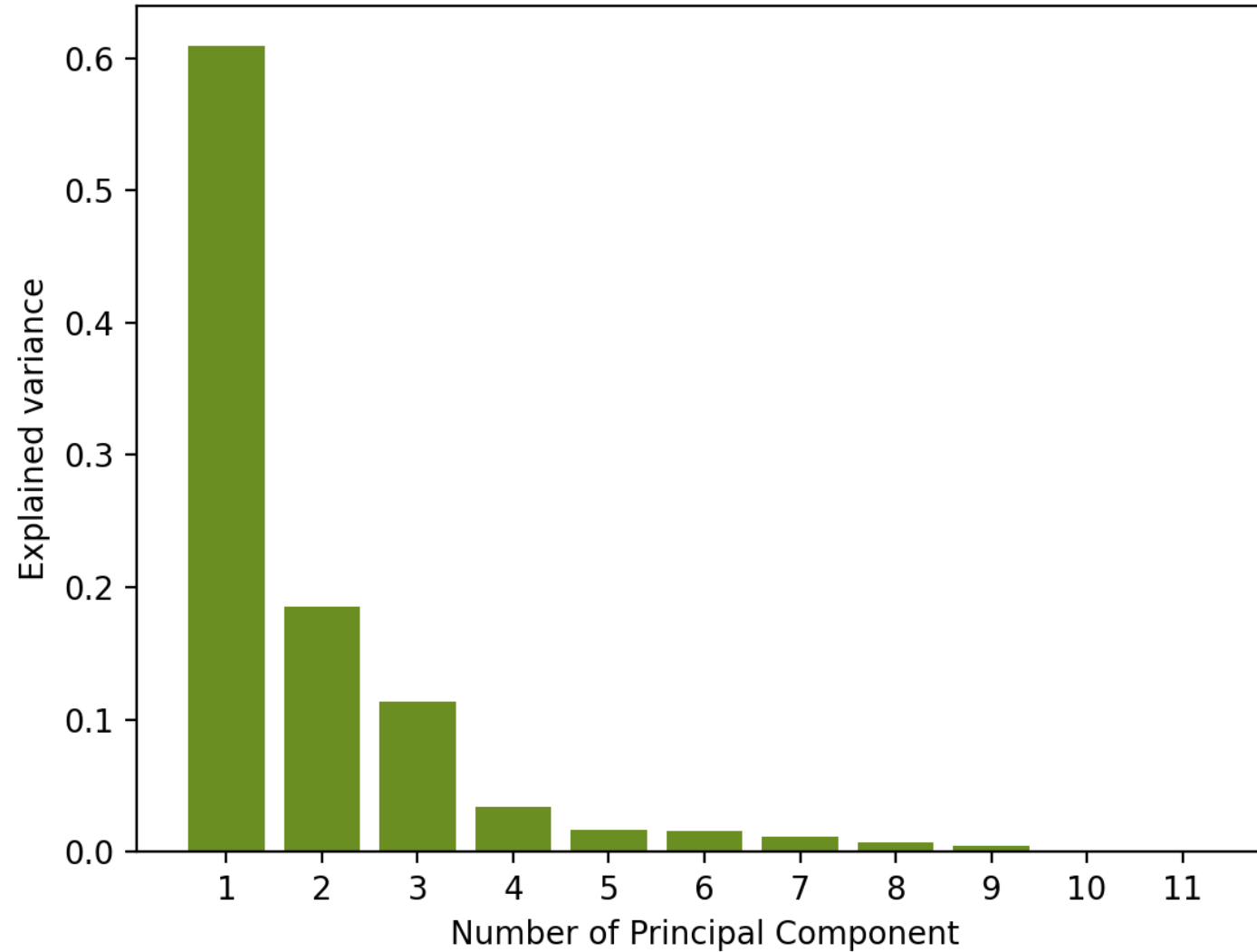
Recurrence plot for the mantle



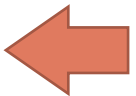
# Methods : PCA, how it works



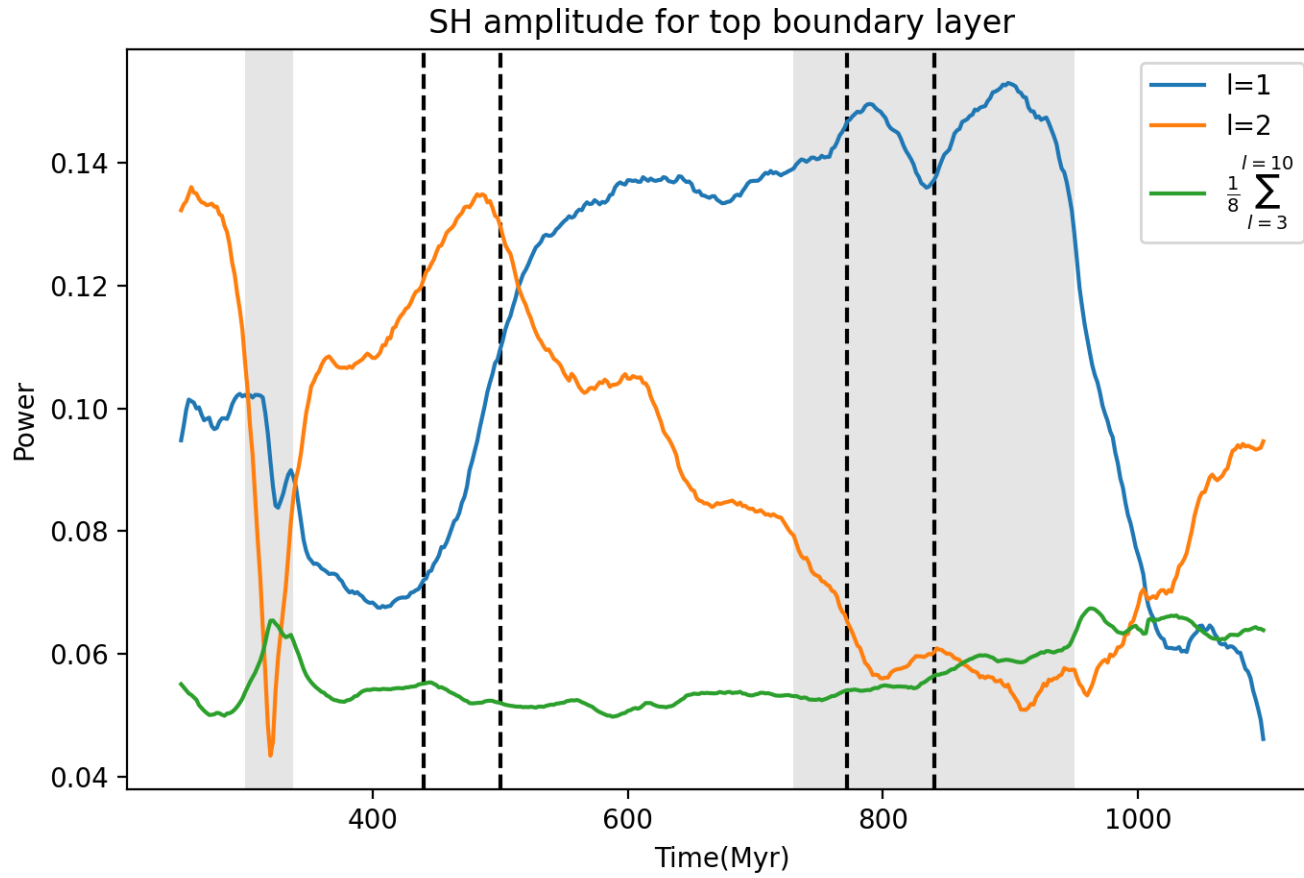
# Variance of Principal Components



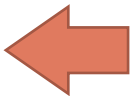
First PC : 61%  
Second PC : 19%  
Third PC : 11%



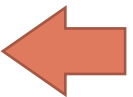
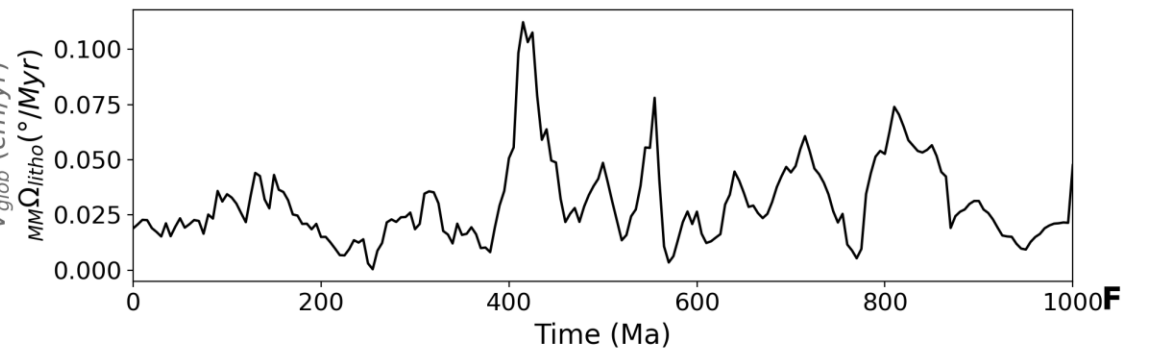
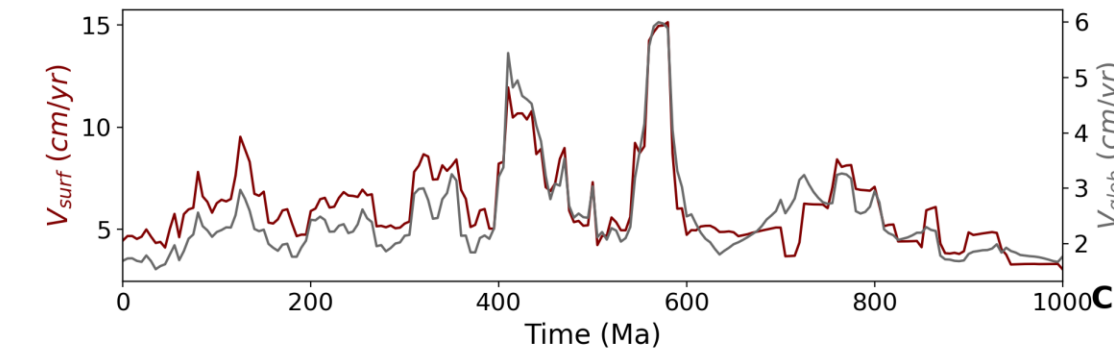
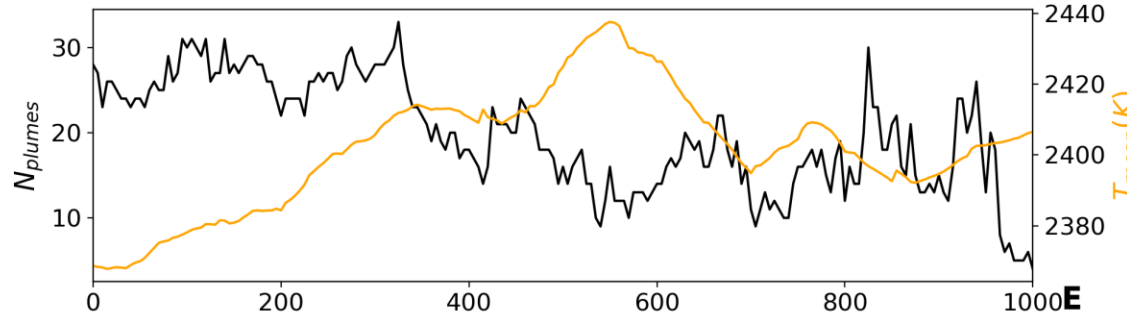
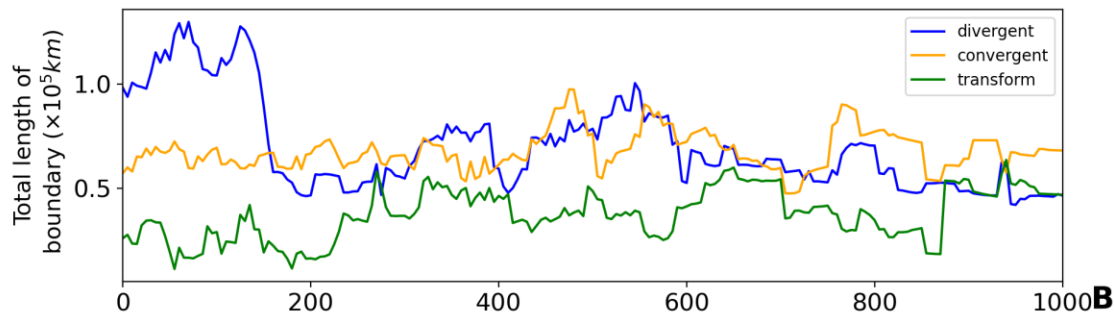
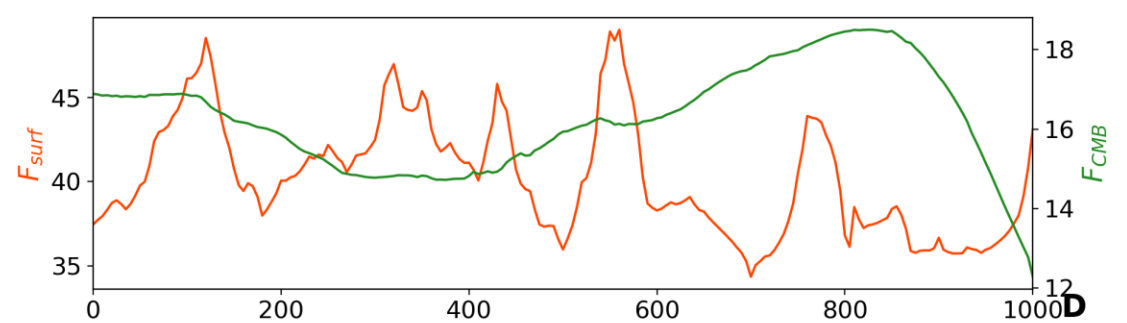
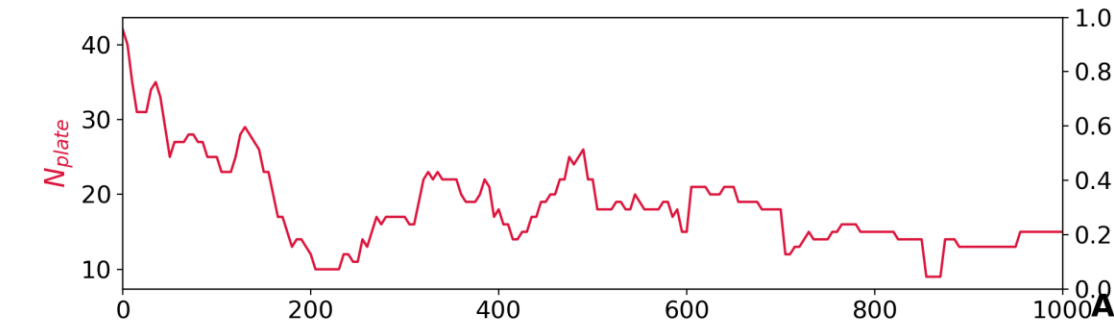
# Results : Thermal heterogeneity spectrum



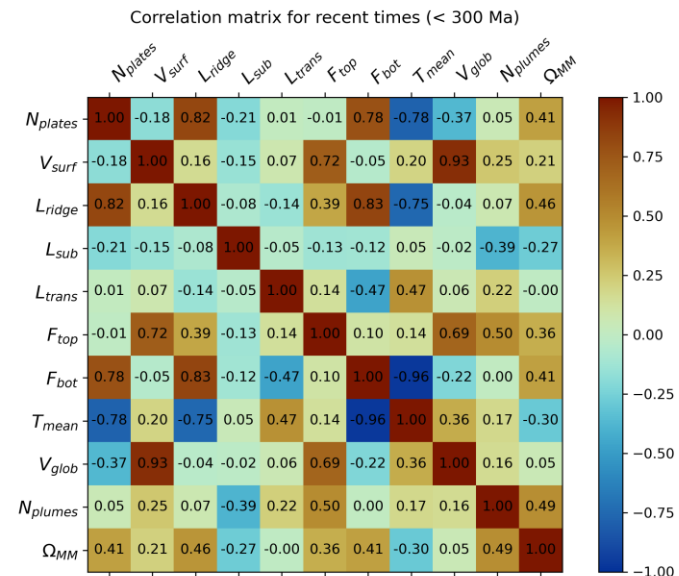
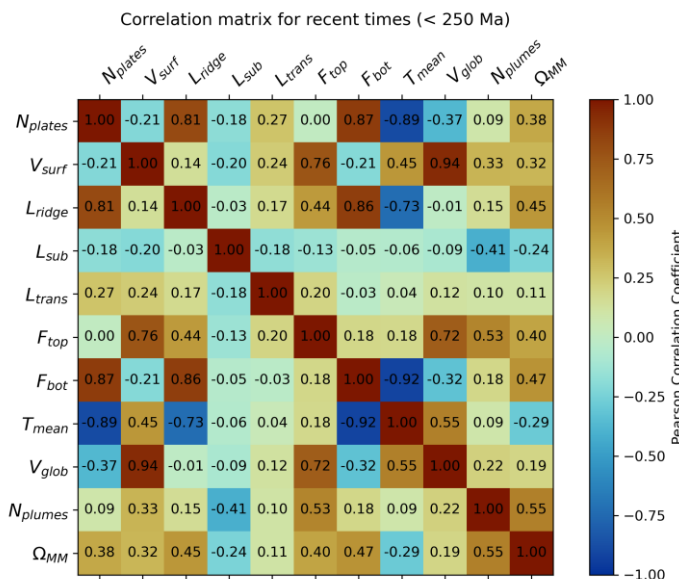
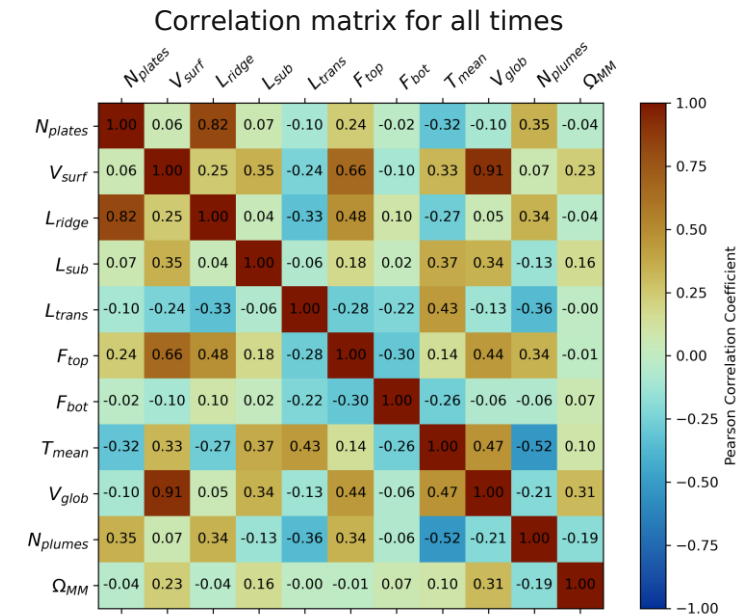
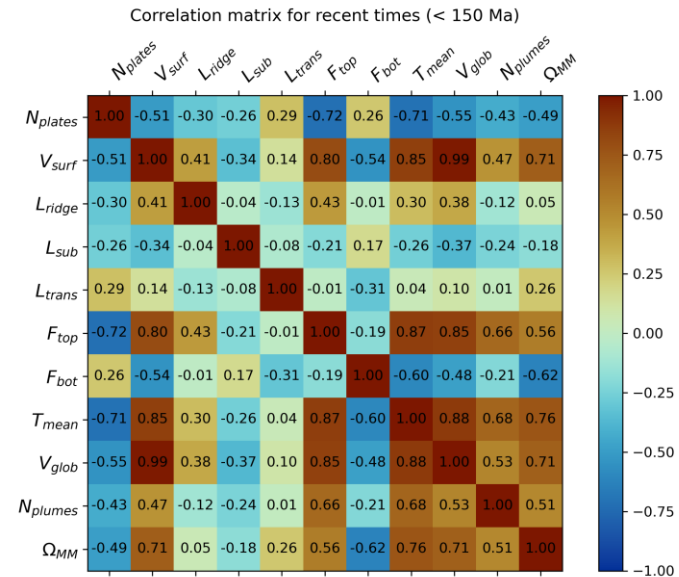
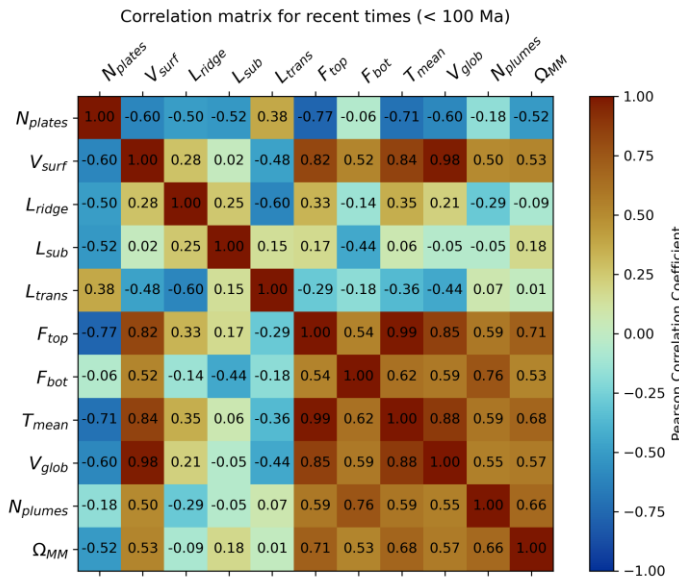
- Supercontinent cycle : degree 1 to form supercontinent, degree 2 to disperse
- Some transitions are synchronous with changes in long wavelength of convection



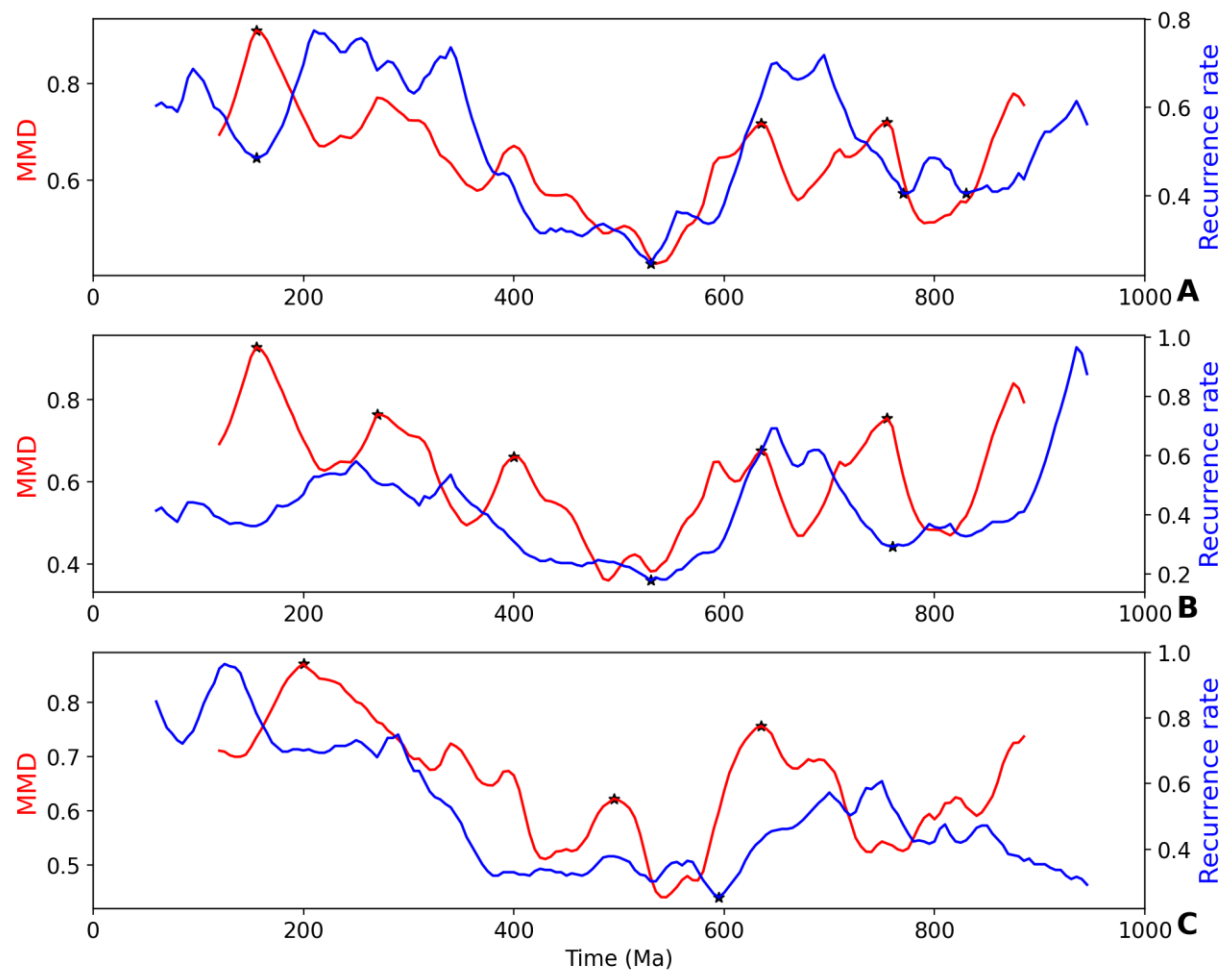
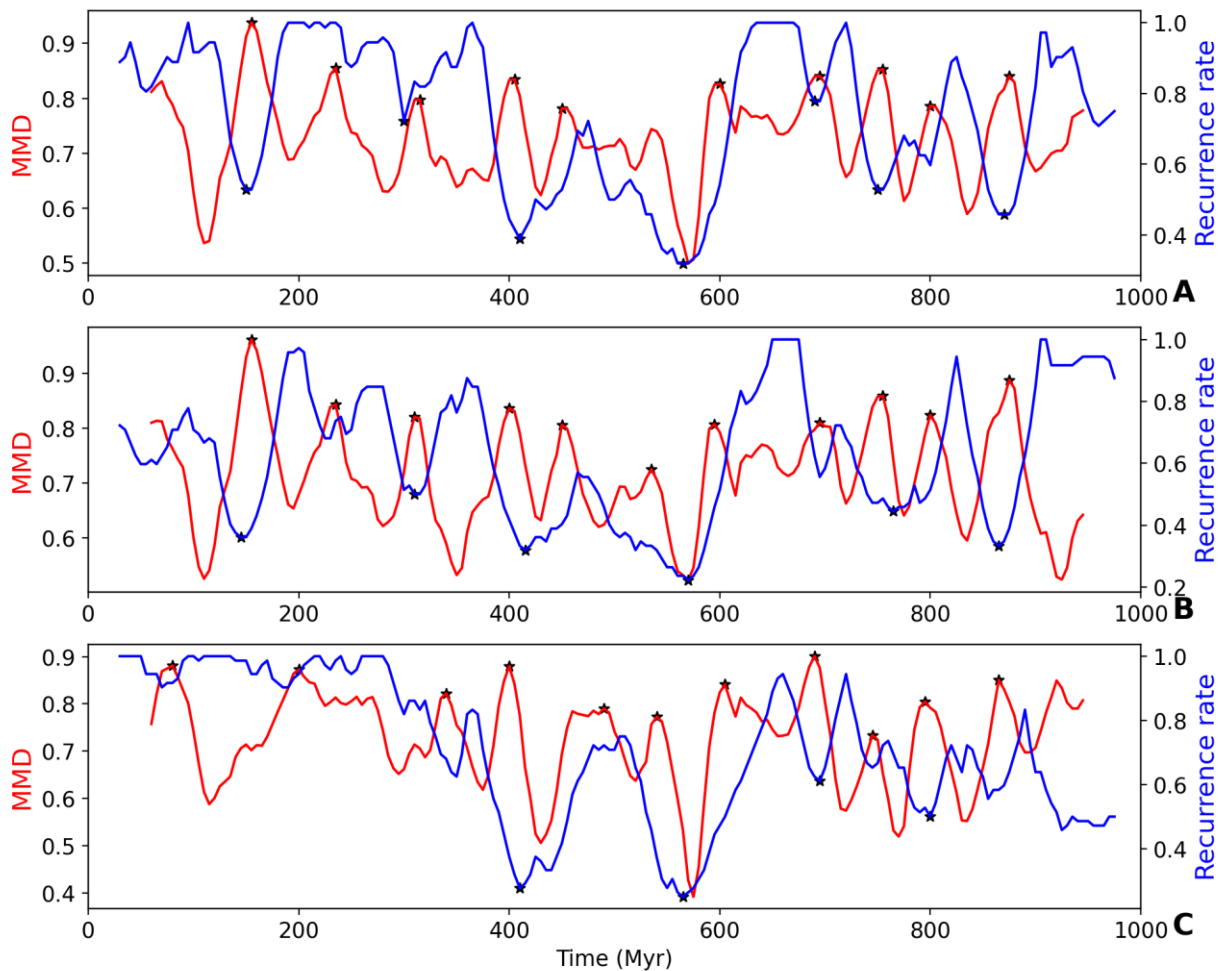
# Test on Kinematically Constrained Flow Model



# Test on Kinematically Constrained Flow Model



# Test on Kinematically Constrained Flow Model



←  $W = 60\text{Myr}, 12\text{ points}$

$W = 120\text{Myr}, 24\text{ points}$  →