

Using principal component analysis in empirical-statistical downscaling to emphasise synoptic scales

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**Meteorologisk
institutt** 150 år

What is PCA?

A way of organising the data according to information contents

Similar to

Eigenvalues

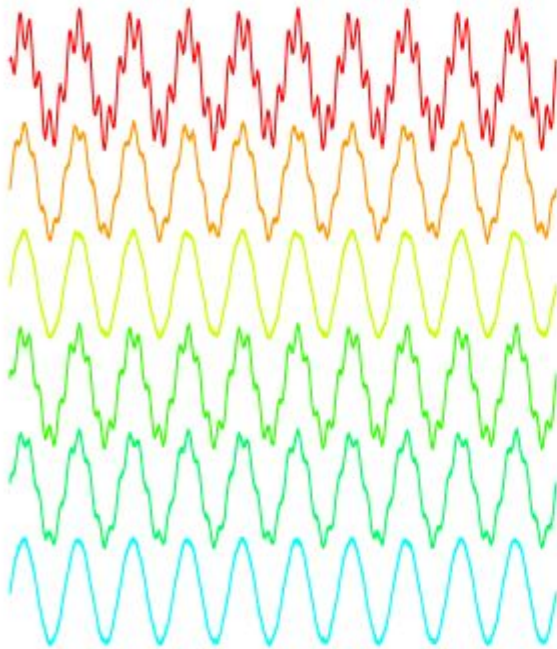
Empirical Orthogonal Functions (EOFs)

Fourier series

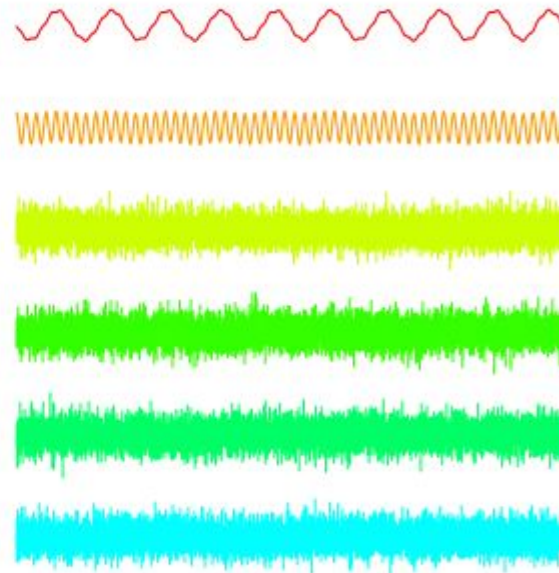
What is PCA?

$$y = \sum_{i=1}^n \beta_i x_i$$

x_i

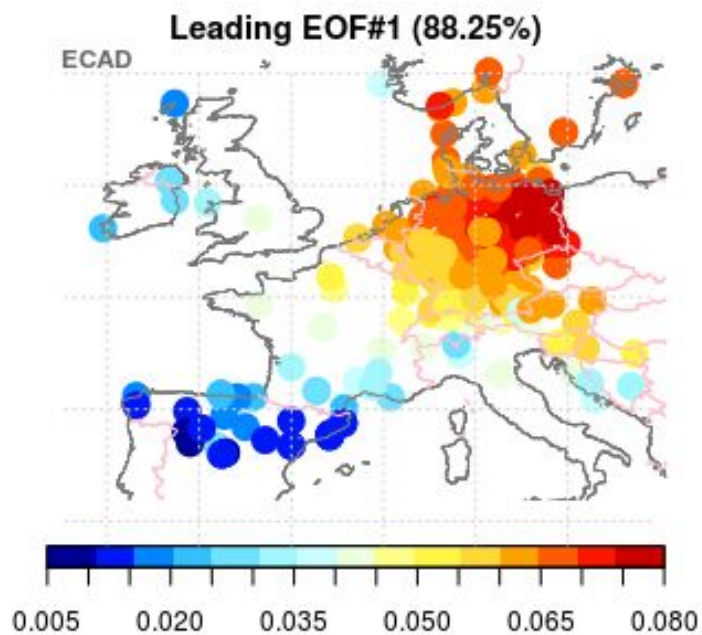


Original data

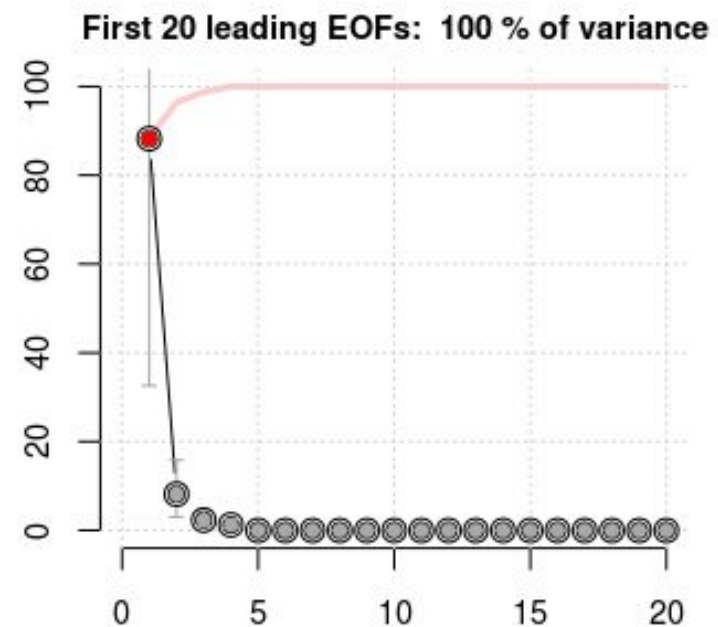


Principal components (PCs)

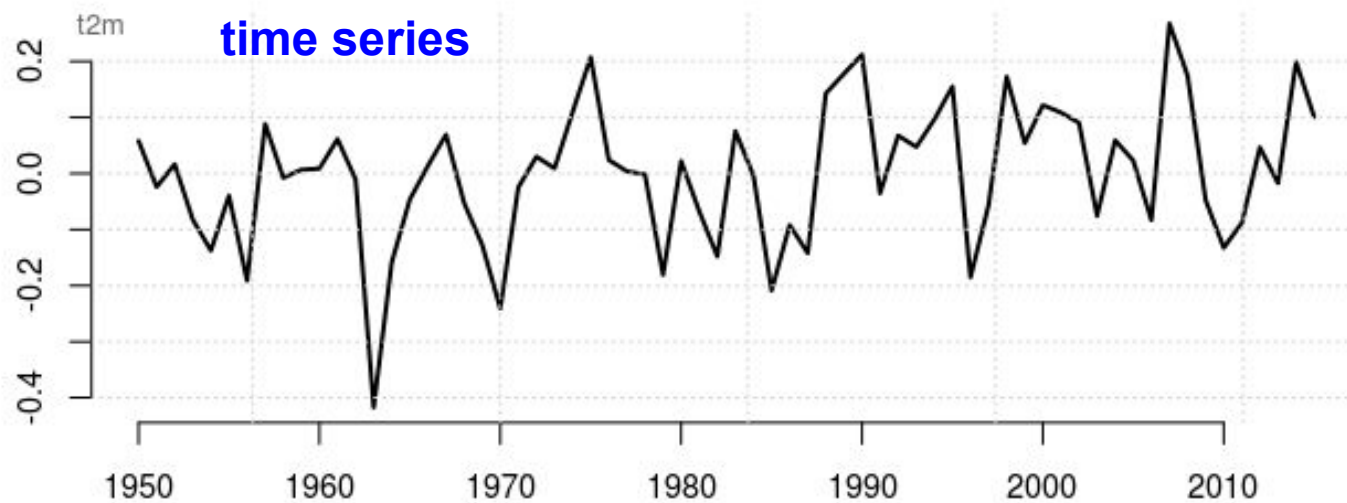
spatial patterns



amplitudes



Leading PC#1 of Mean temperature - Explained variance = 88.25%



Why principal component analysis (PCA)?

Redundant information

Signal enhancement: emphasis large scales

Covariance preservation

Computation time

Orthogonality

How true are these reasons?



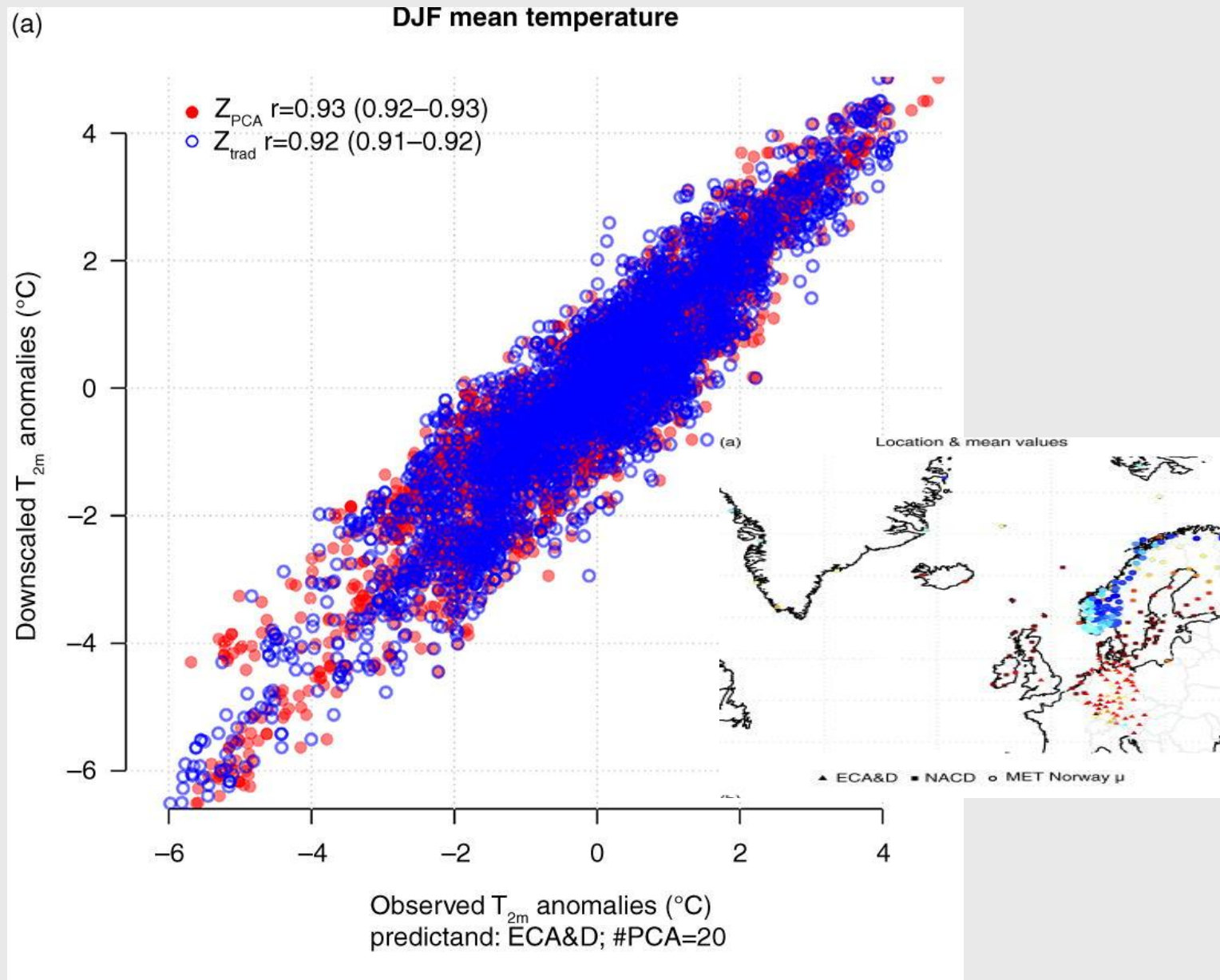
Computation speed

- Apply multiple regression to single principal components.
- Fast: 4 leading modes rather than ~400 stations
 - especially for large ensembles

Computation speed

- Apply multiple regression to single principal components.
- Fast: 4 leading modes rather than ~400 stations
 - especially for large ensembles
- Works for station groups and gridded data

Signal: Restructure data with information first

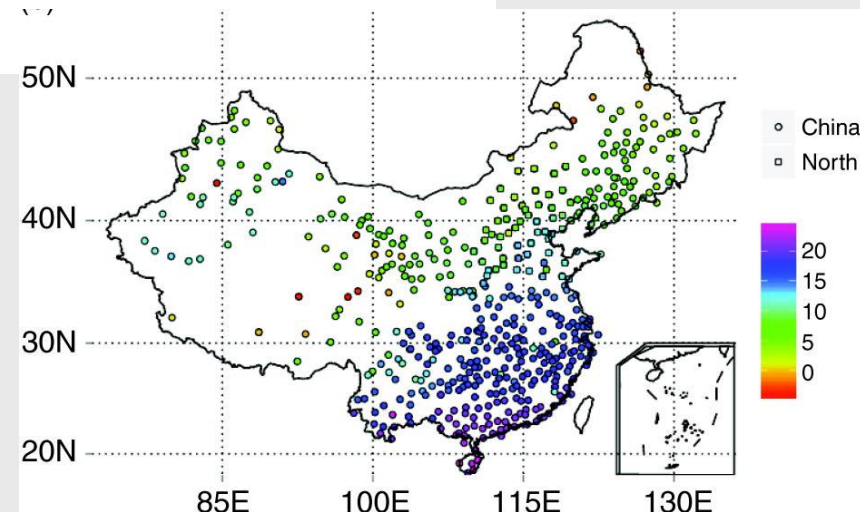


Signal: Sensitivity to the choice of large-scale domain

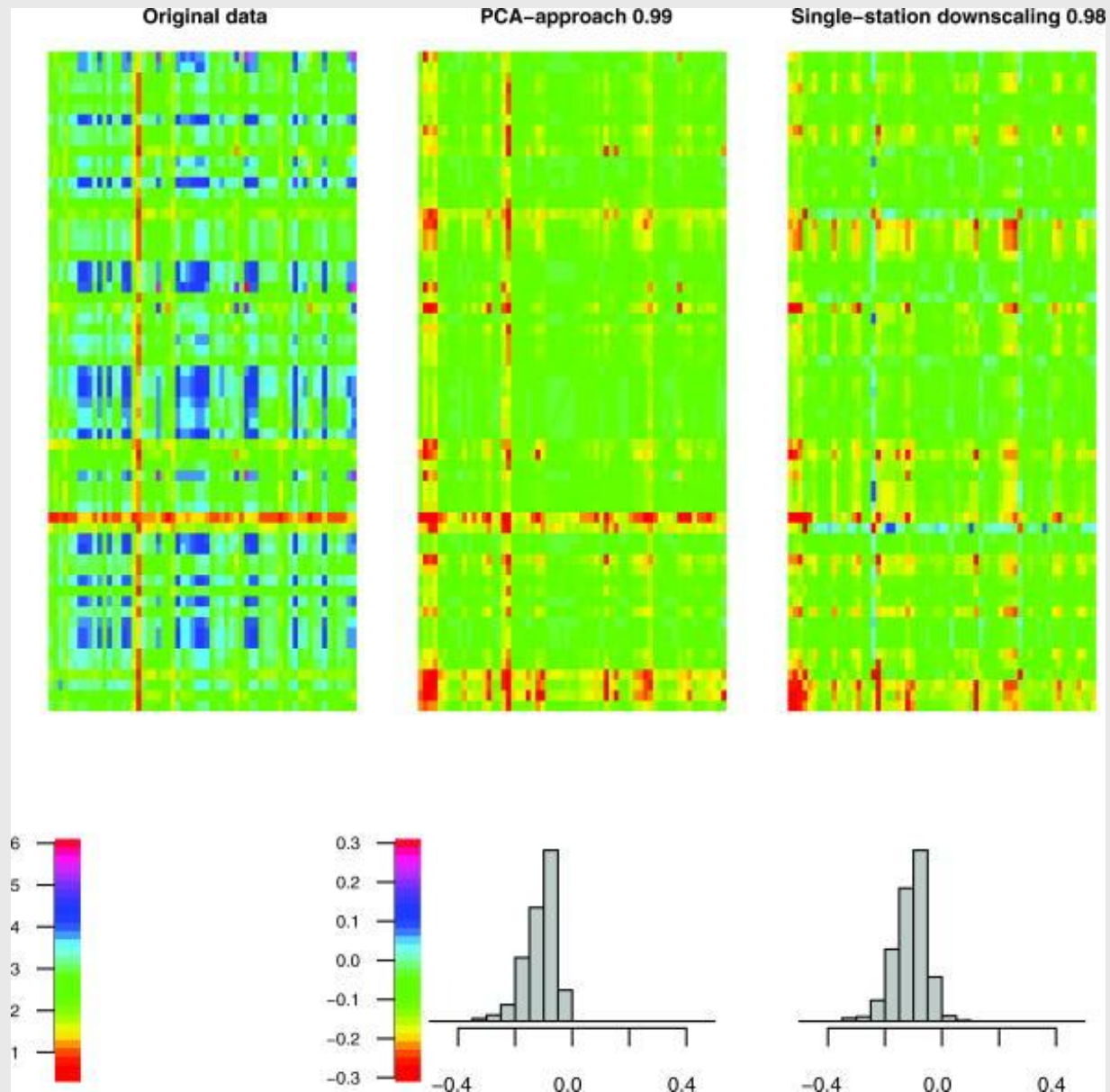
Table 2. Skill scores for the PCA-based and traditional ESD for China

Area (km ²)	27 800 000	31 800 000	35 800 000	34 400 000	39 300 000	44 200 000
DJF						
PCA	0.87	0.86	0.87	0.87	0.86	0.86
trad.	0.83	0.82	0.82	0.84	0.83	0.82
JJA						
PCA	0.71	0.69	0.72	0.73	0.70	0.70
trad.	0.70	0.71	0.70	0.68	0.65	0.64
N_{PCA}	20	20	20	20	20	20
Domain						
W (°E)	70.00	65.00	60.00	70.00	65.00	60.00
E (°E)	140.00	145.00	150.00	140.00	145.00	150.00
S (°N)	15.00	15.00	15.00	10.00	10.00	10.00
N (°N)	55.00	55.00	55.00	60.00	60.00	60.00
N_{PCA}	20	20	20	20	20	20

The entries are correlation scores from the cross-validation. The predictor was the NCEP/NCAR reanalysis and predictands included 499 stations with complete time series over the period 1961–2012. The highest score in each of the comparisons is shown in bold.



Covariance structure

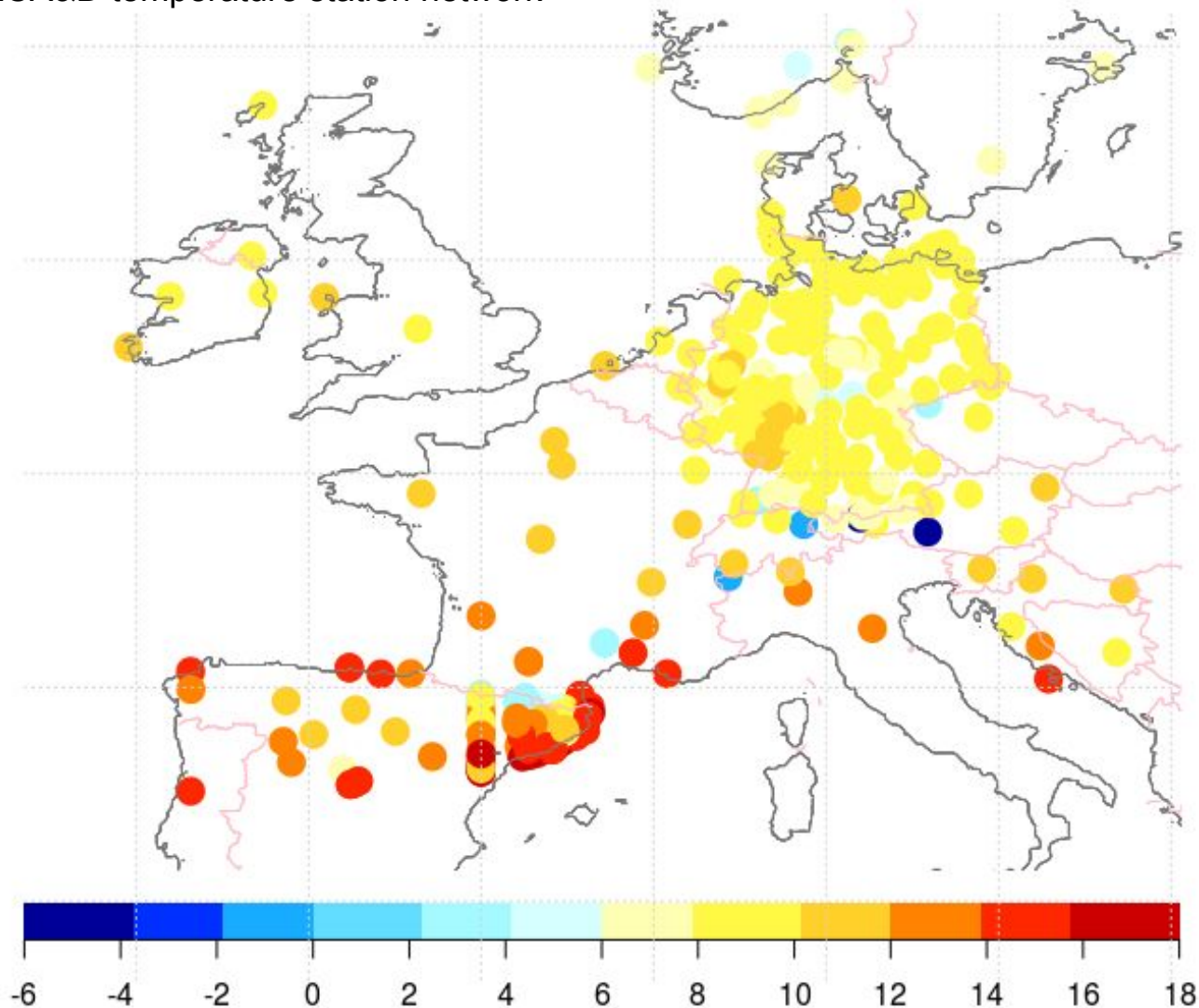


Requirements for PCA-based downscaling

- No missing data
- Suitable distribution
- Not too spatially spread

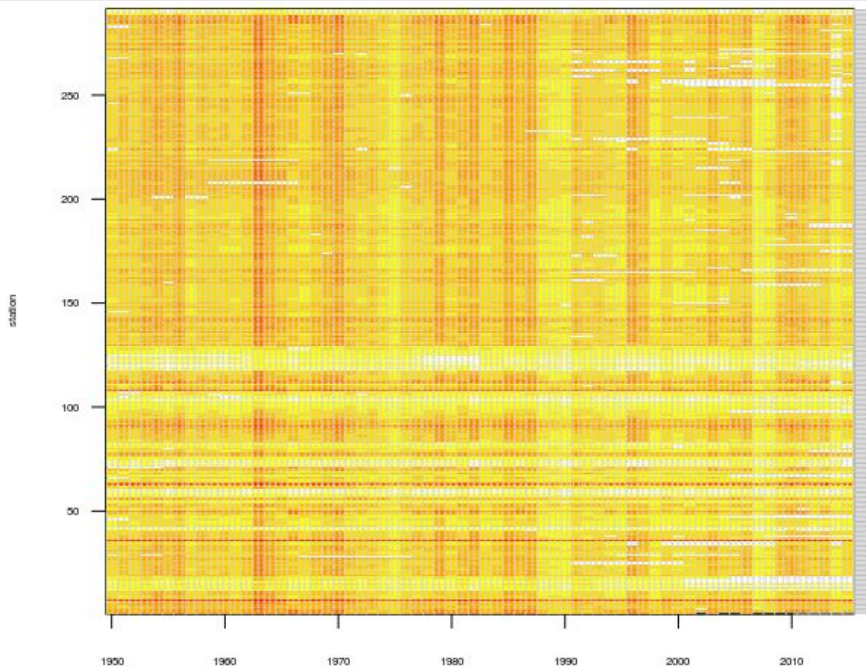
'pcafill' (esd R-package)

ECA&D temperature station network

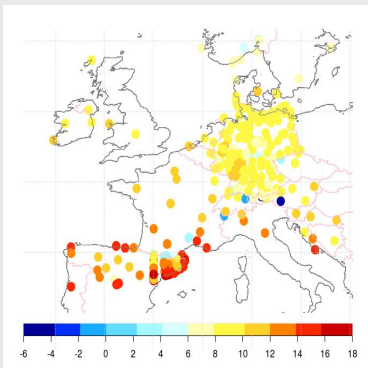
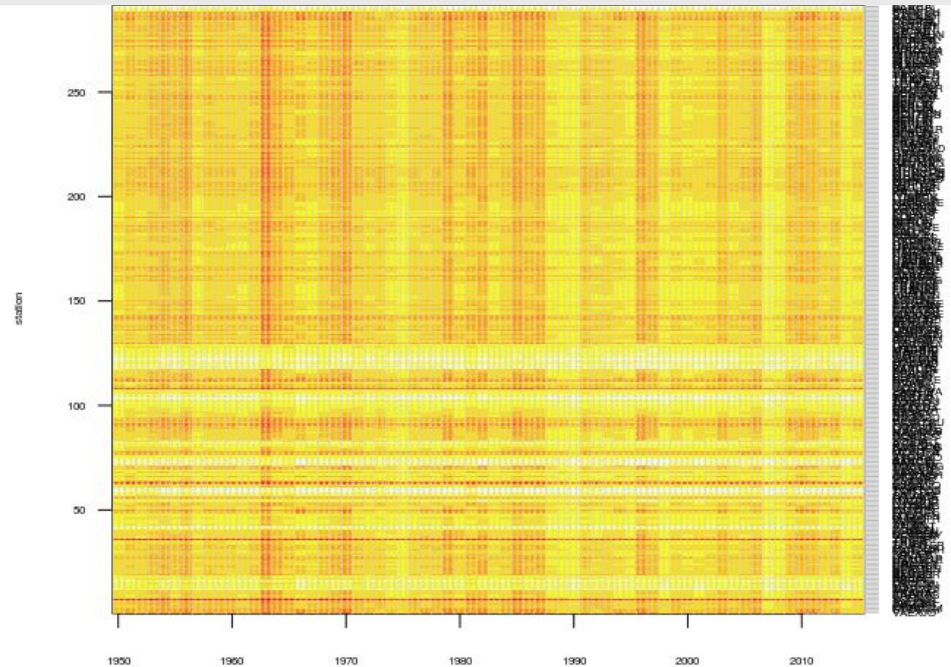


'pcafill' (esd R-package)

Data matrix with missing data
(white spaces)

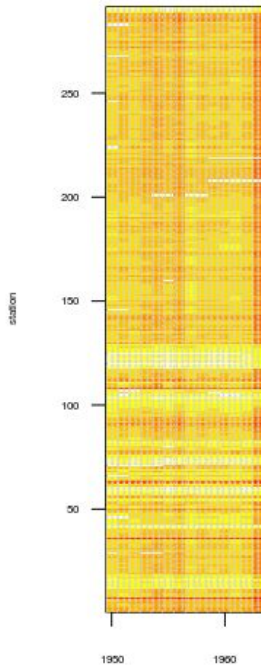


Complete data matrix

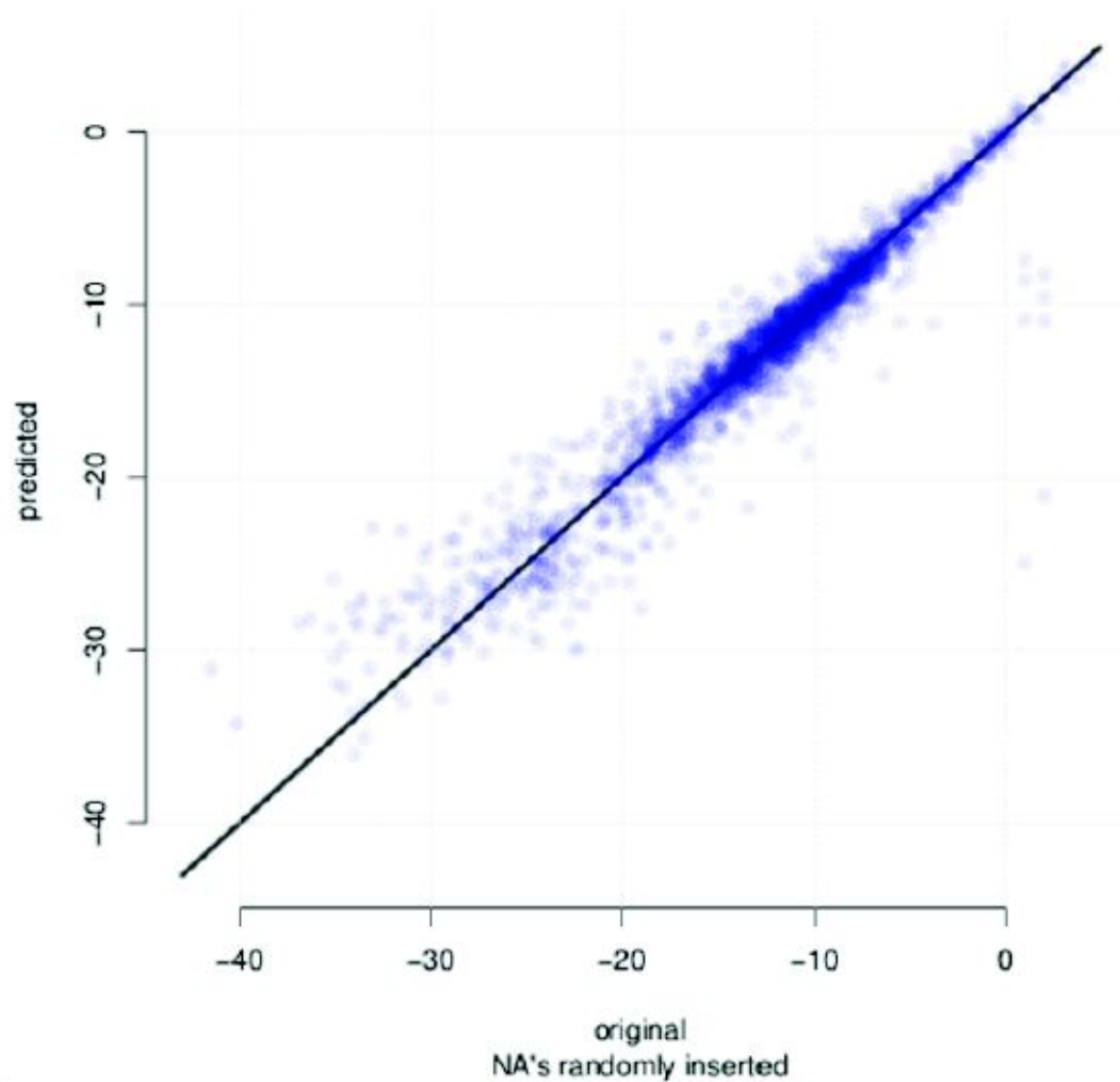


'pcafill' (

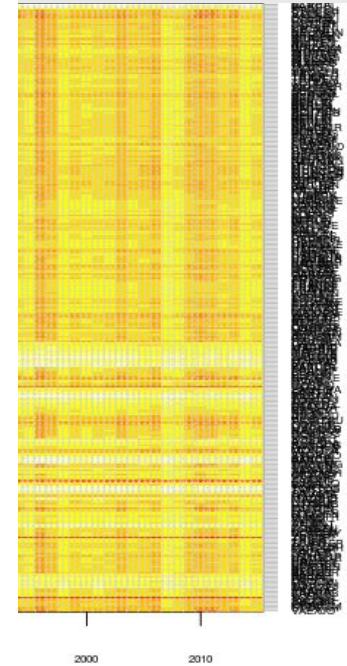
Data



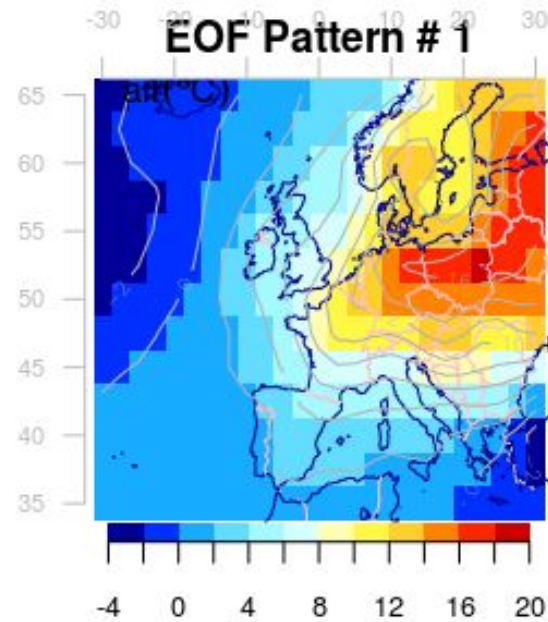
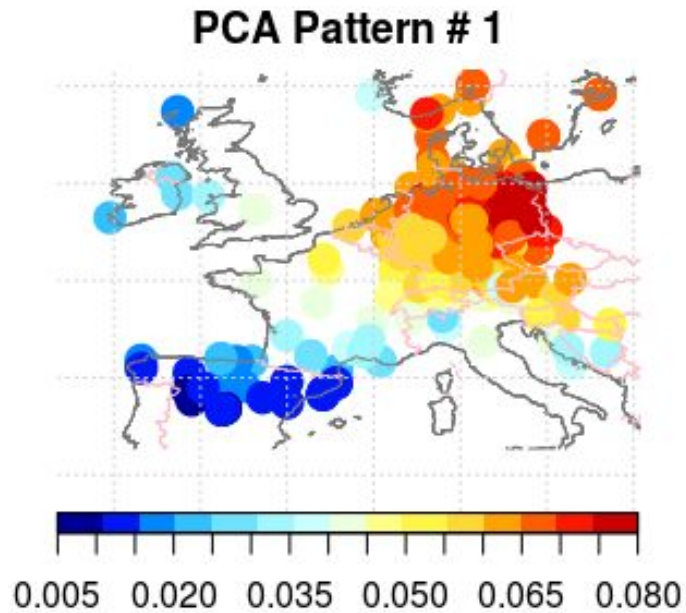
Test of prediction of missing values



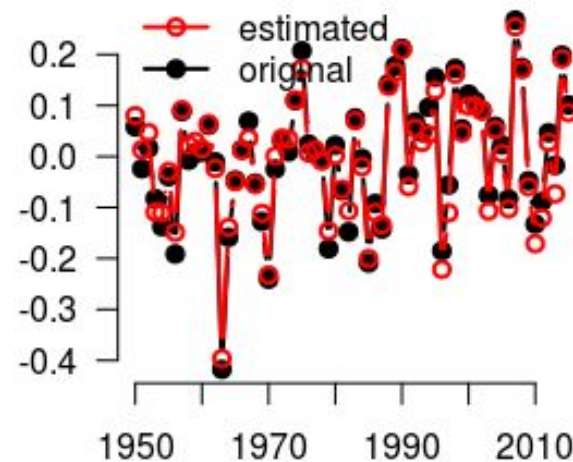
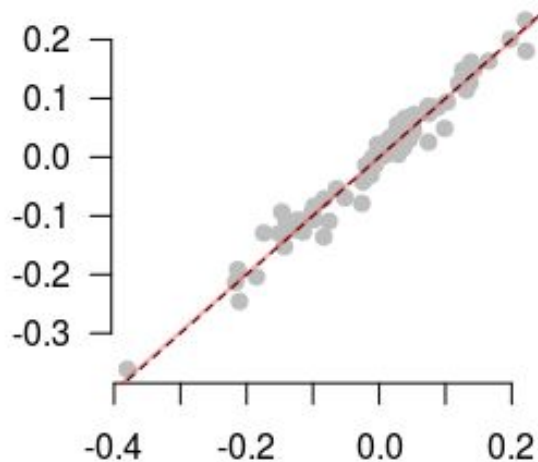
matrix



Downscaling: diagnostics for leading PCA

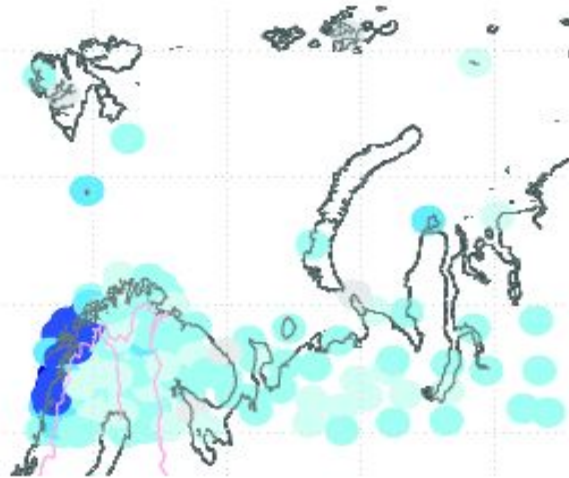


Cross-validation: $r = 0.98$

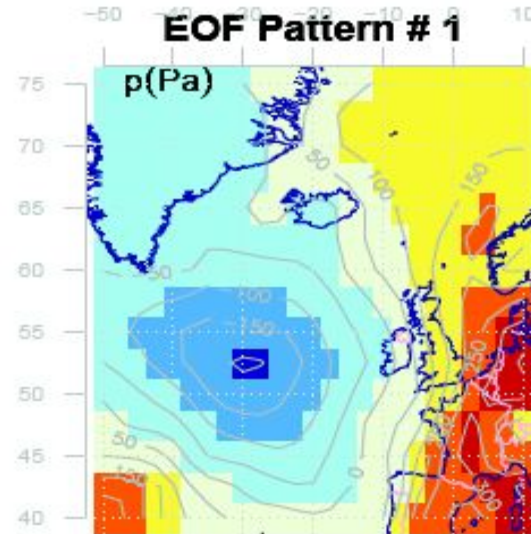


“Warm season” wet-day mean precip μ

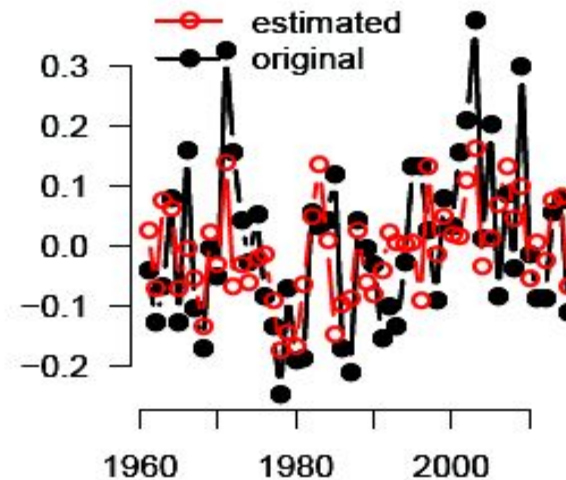
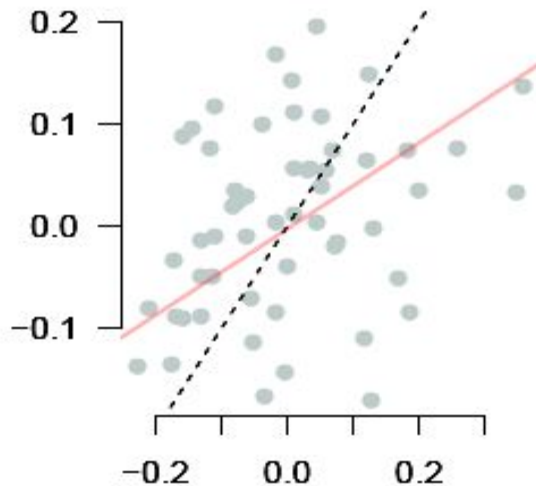
PCA Pattern # 1



EOF Pattern # 1

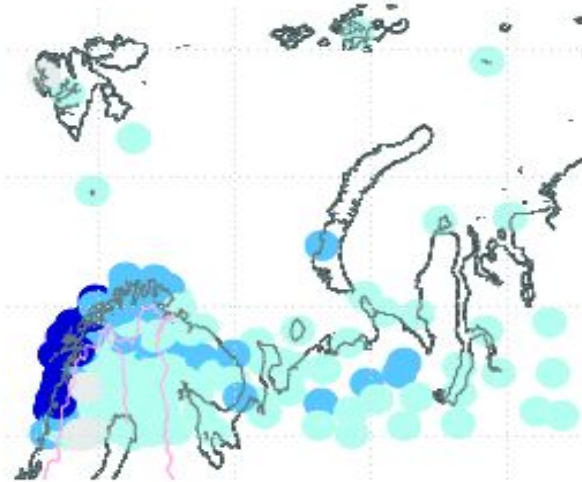


Cross-validation

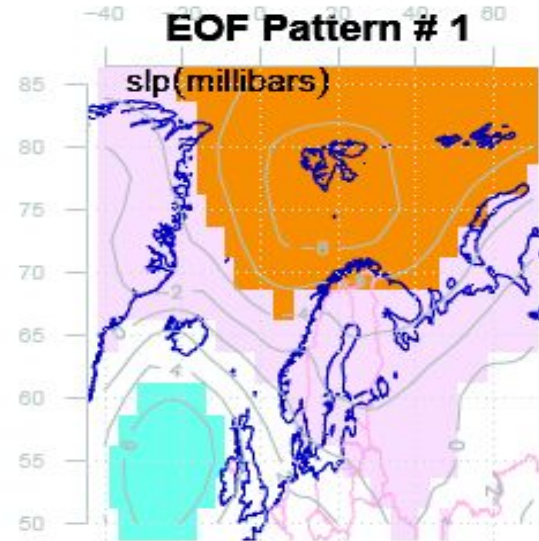


“Warm season” wet-day frequency f_w

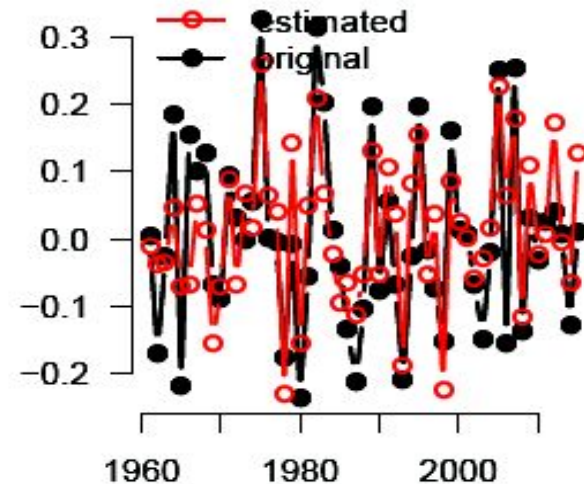
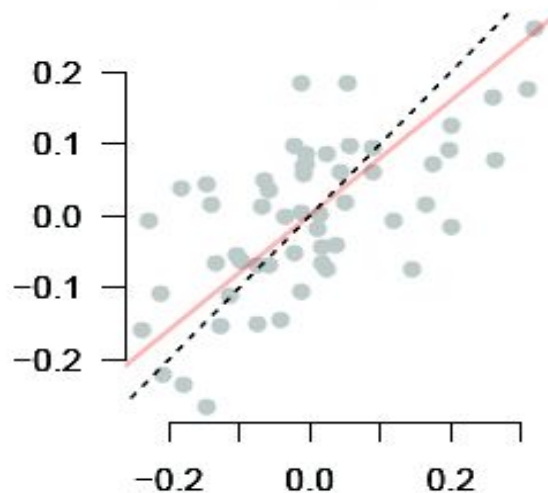
PCA Pattern # 1



EOF Pattern # 1

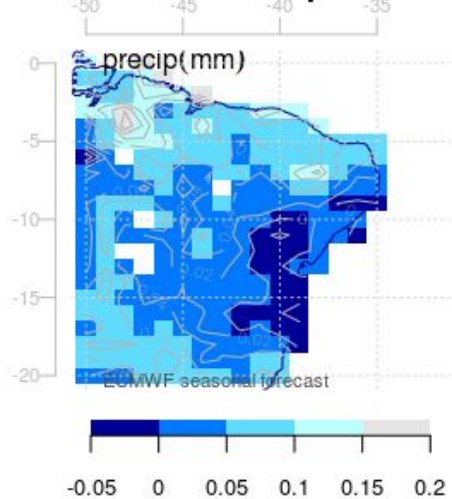


Cross-validation

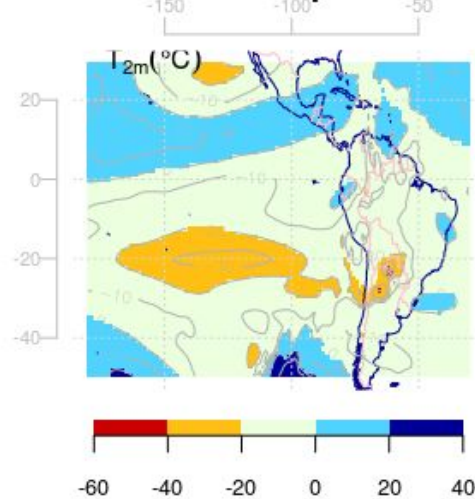


Model output statistics (MOS) in seasonal prediction ensemble

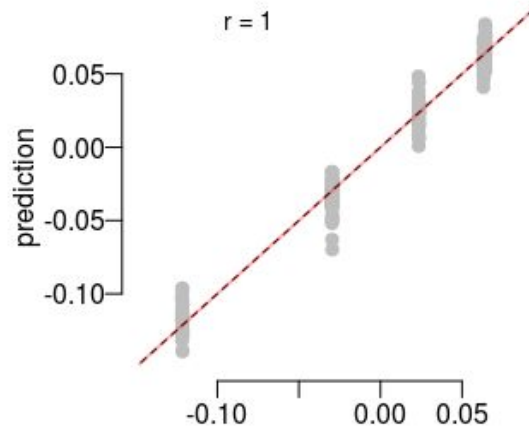
Predictand EOF pattern # 1



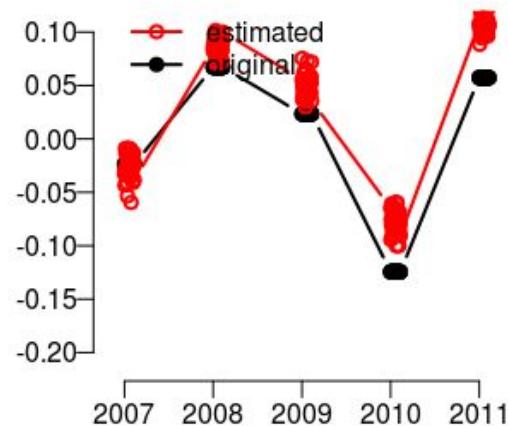
Predictor EOF pattern # 1



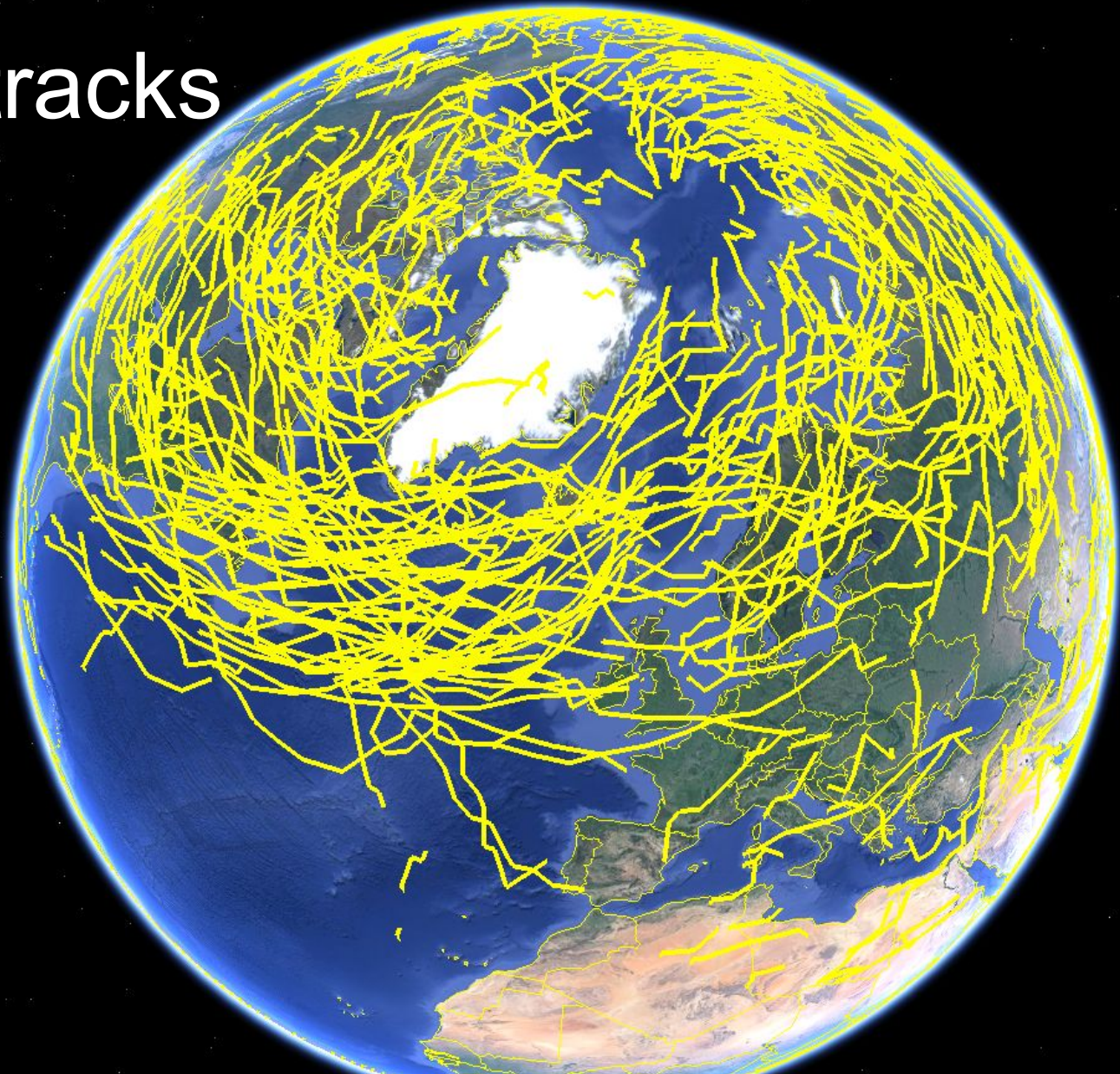
Cross-validation



PC 1



Storm tracks



Data SIO, NOAA, U.S. Navy, NGA, GEBCO
US Dept of State Geographer
© 2013 Google
Image Landsat

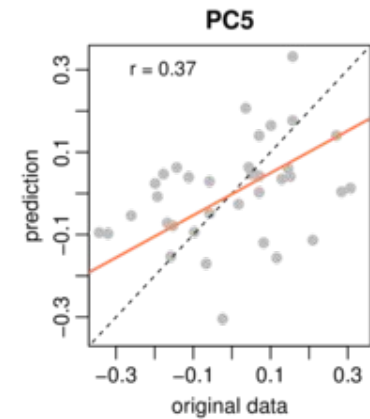
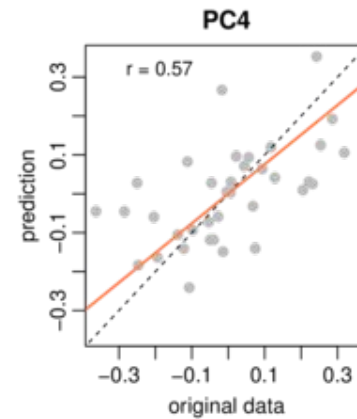
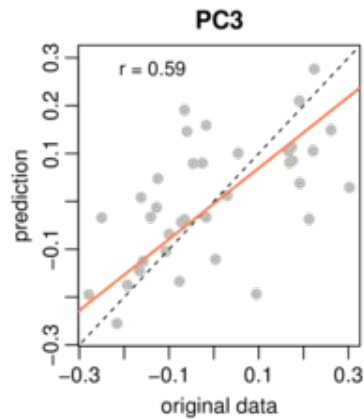
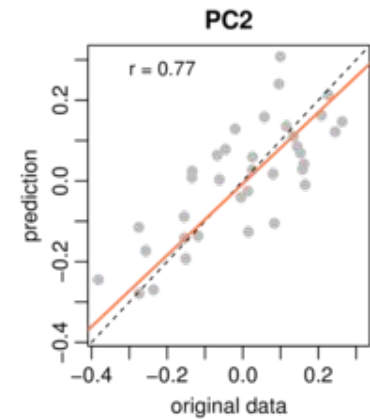
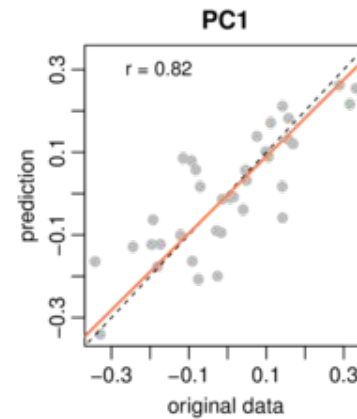
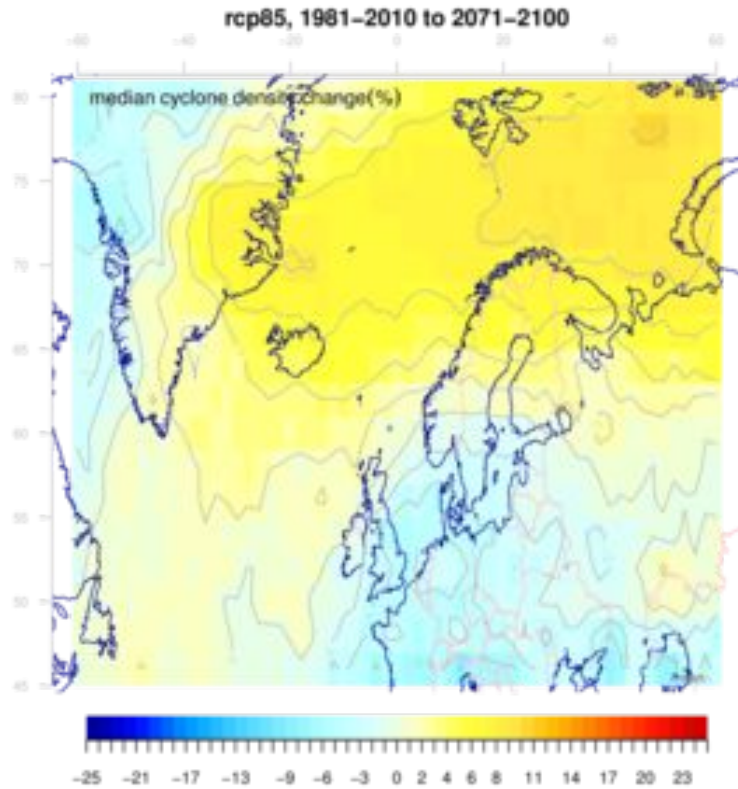
©2010 Google

49°07'59.04" N, 0°46'06.54" W, elev: 0000 M

Elev: 5000.70 mi



“Warm season” wet-day mean precip μ



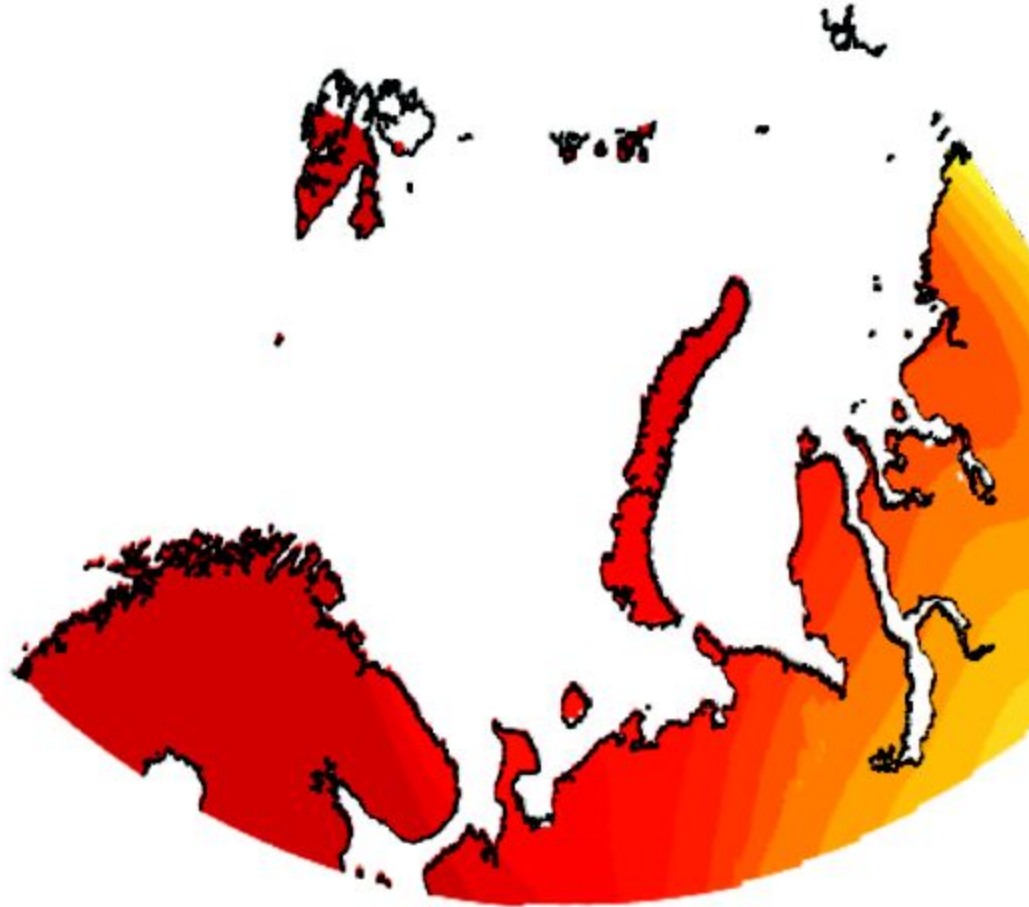
Easier post-processing



PCA quick to grid: only a few patterns

95 percentile diff (2099 – 2010)

RCP8.5 (DJF)



$T_{2m} (^{\circ}\text{C})$

2099 -4 -2 0 1 2 3 4 5 6 7 8 9 10 12 14 16 18

LatticeKrig
Covariate: z

Thank you for your attention!

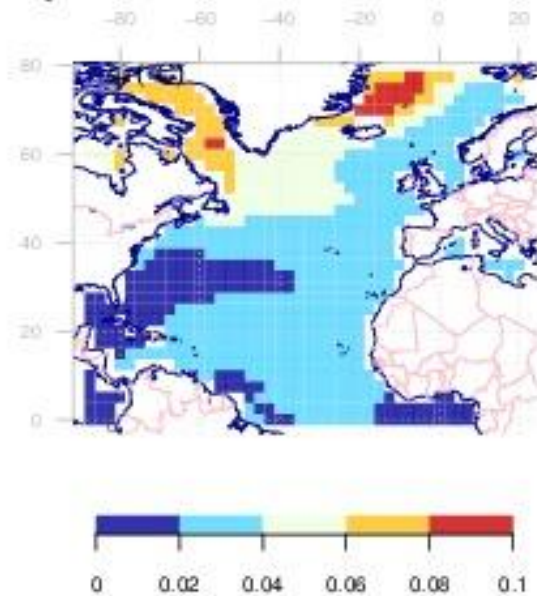
Tellus A 2015, 67, 28326, <http://dx.doi.org/10.3402/tellusa.v67.28326>

Benestad, Rasmus; Parding, Kajsa; Isaksen, Ketil, Mezghani, Abdelkader
“Climate change and projections for the Barents region: what is expected to
change and what will stay the same?”, ERL-102170.R2 (accepted)

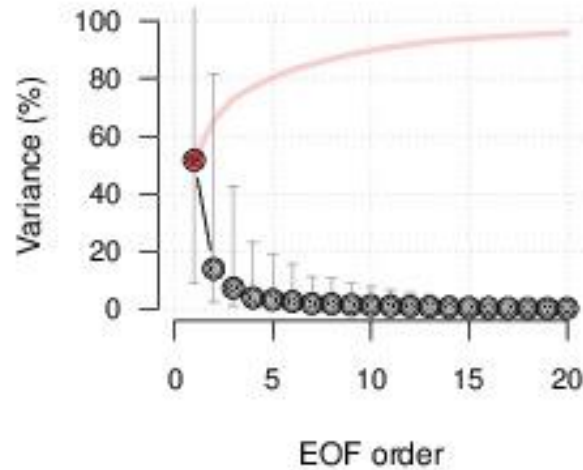
https://github.com/metno/esd_Rmarkdown/tree/master/CORDEX

MOS in decadal prediction ensemble

1 years



First 20 leading EOFs: 95.8 % of variance



Leading PC#1 of Monthly Mean Air Temperature at sigma level 0.995 – Explained variance = 51.71%

