

Extreme Precipitation in the past and future

Non-stationary Large-Scale Statistics of Precipitation
Extremes in Central Europe

Felix S. Fauer
Henning W. Rust

ENVIRONMENT JULY 21, 2023

The Problem With Calling Vermont's Storms a "100-Year-Flood"

Thanks to climate change, these deluges are occurring much more often.

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Tyler Jovic, of Montpelier, carries his neighbor's dog to dry ground on July 11, 2022. Washington Post/Getty

- 100-year-event
- Static Climate?
 - Changing Climate?

For Members

'100 year-event': Denmark braced for extreme torrential rain this weekend

Michael Barrett - michael@thelocal.dk
Published: 12 Jul, 2024 CET. Updated: Fri 12 Jul 2024 11:35 CET

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Rain storm shatters records in N.S., called a "one-in-100 year event"



By Mark Hodgins
Posted Jul 23, 2023 12:32:49 PM. Last Updated Jul 24, 2023 02:16:35 PM.



information. Also, the new model enables insights into the

Motivation

to project small-scale extremes
(extreme precipitation)

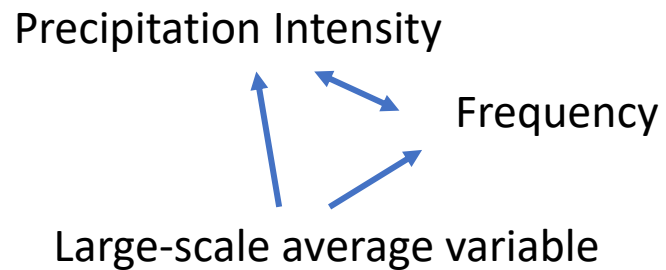
difficult

VS.

to project large-scale average variables
(NAO, temperature, blocking, humidity)

easy

1. Find relation:

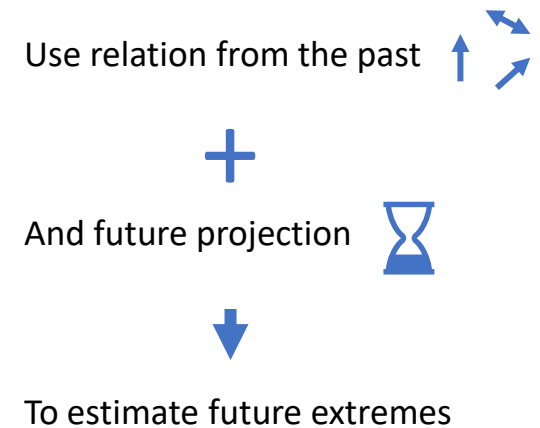


2. Use future projection of large-scale variables (MPI-ESM)



2020 to 2100

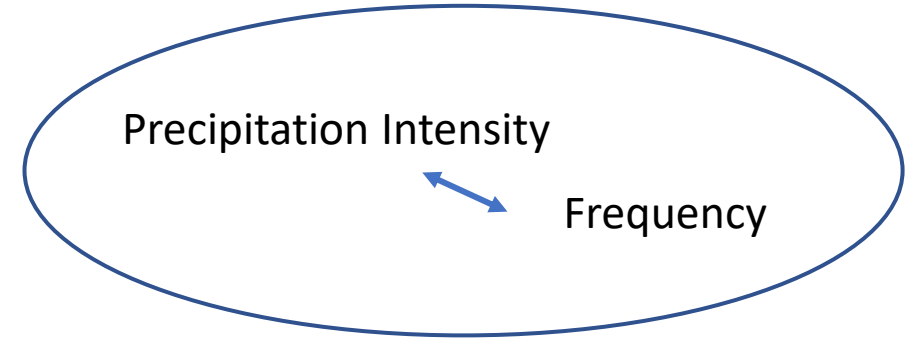
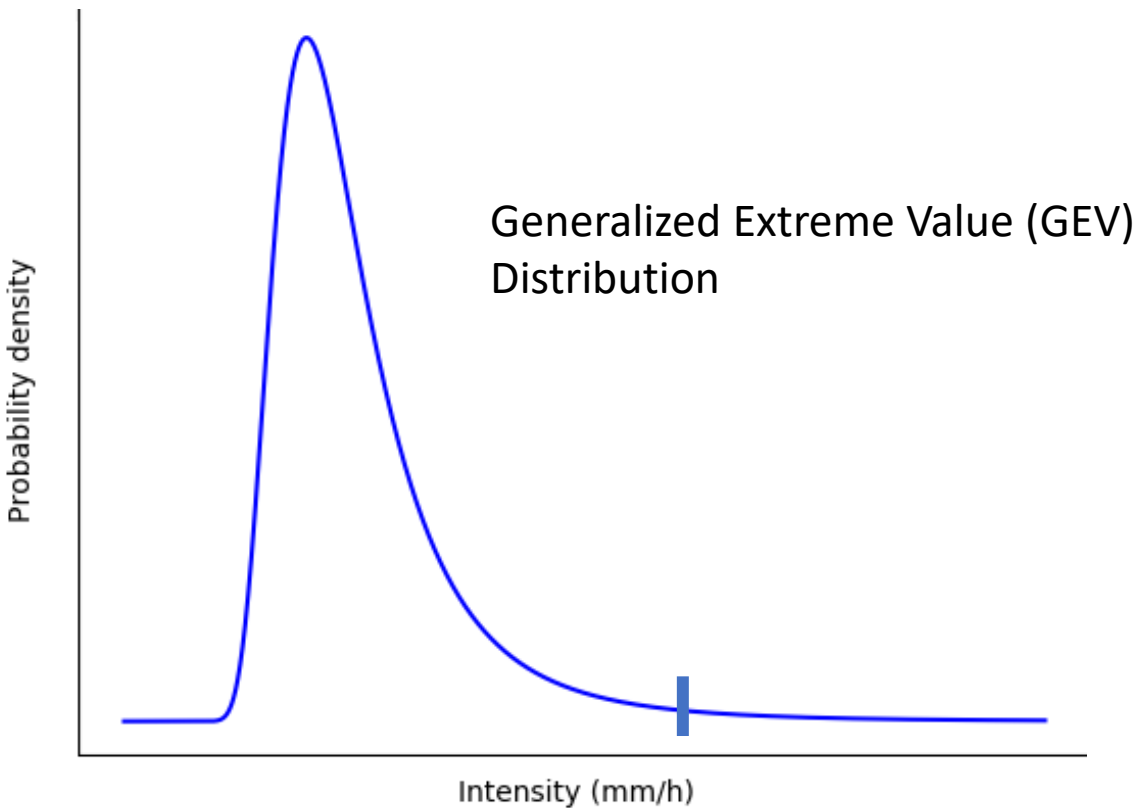
3. Estimate future extremes



Methods



Annual max. intensity: M_{2009} M_{2010} M_{2011} ...

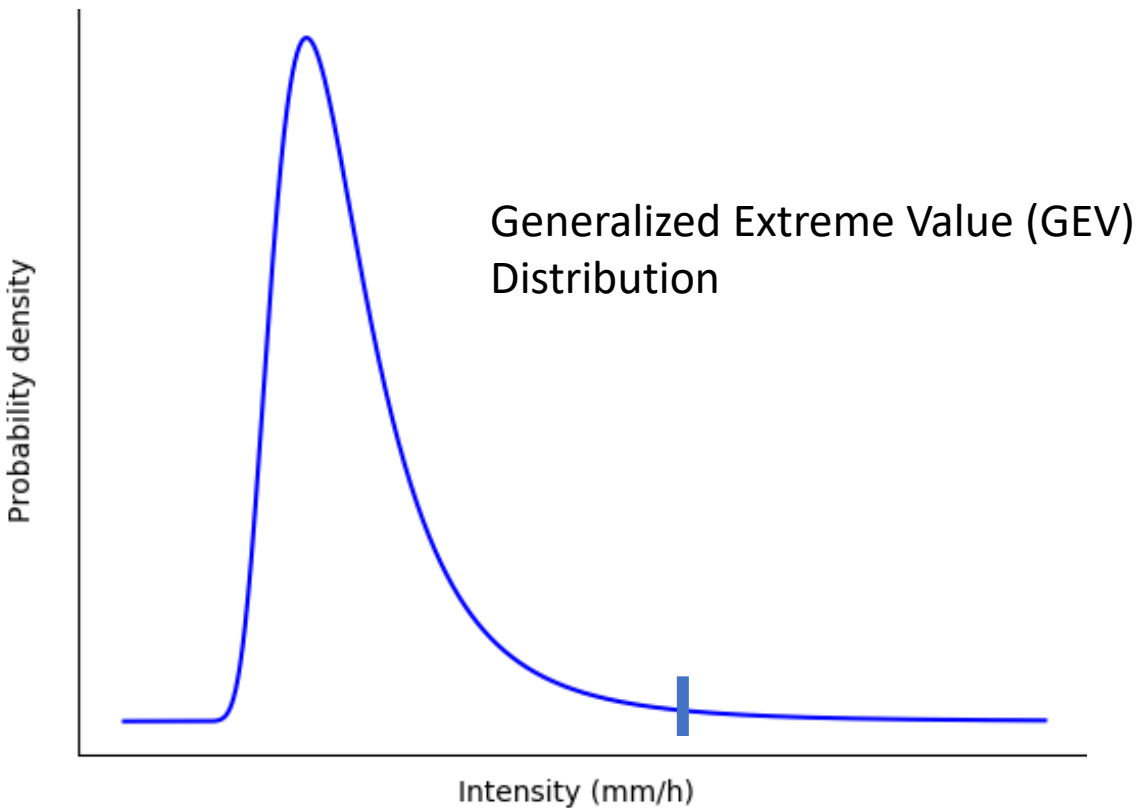


σ (scale)
 μ (location)
 ξ (shape)

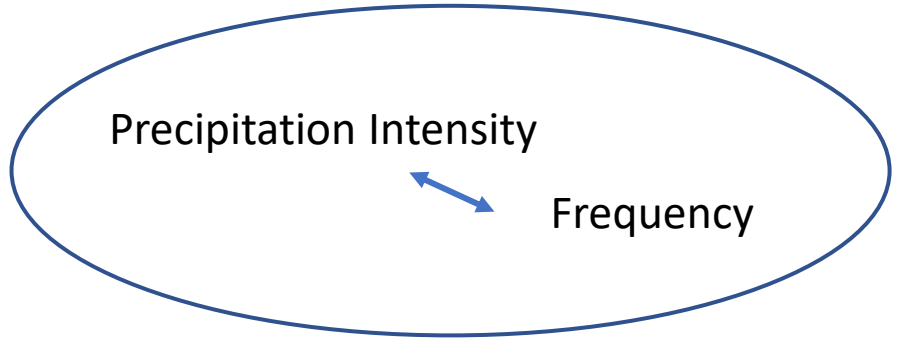
Methods



Annual max. intensity: M_{2009} M_{2010} M_{2011} ...



σ (scale)
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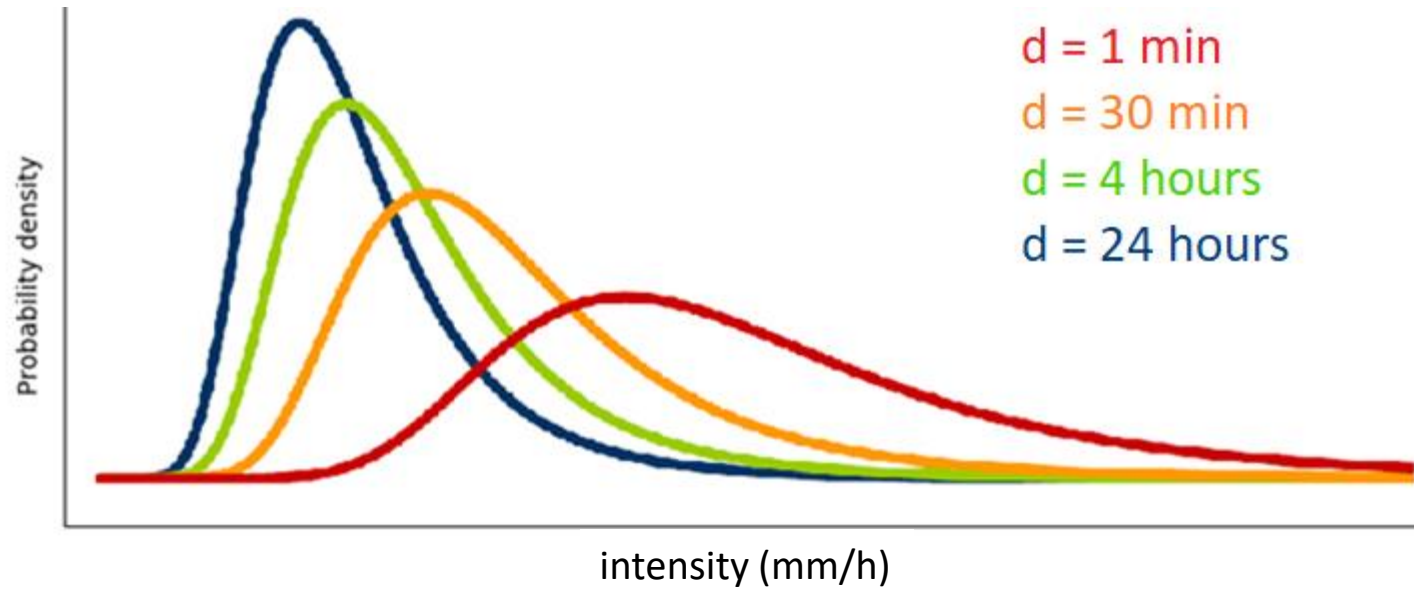


Accumulated **daily** precipitation sums

Methods

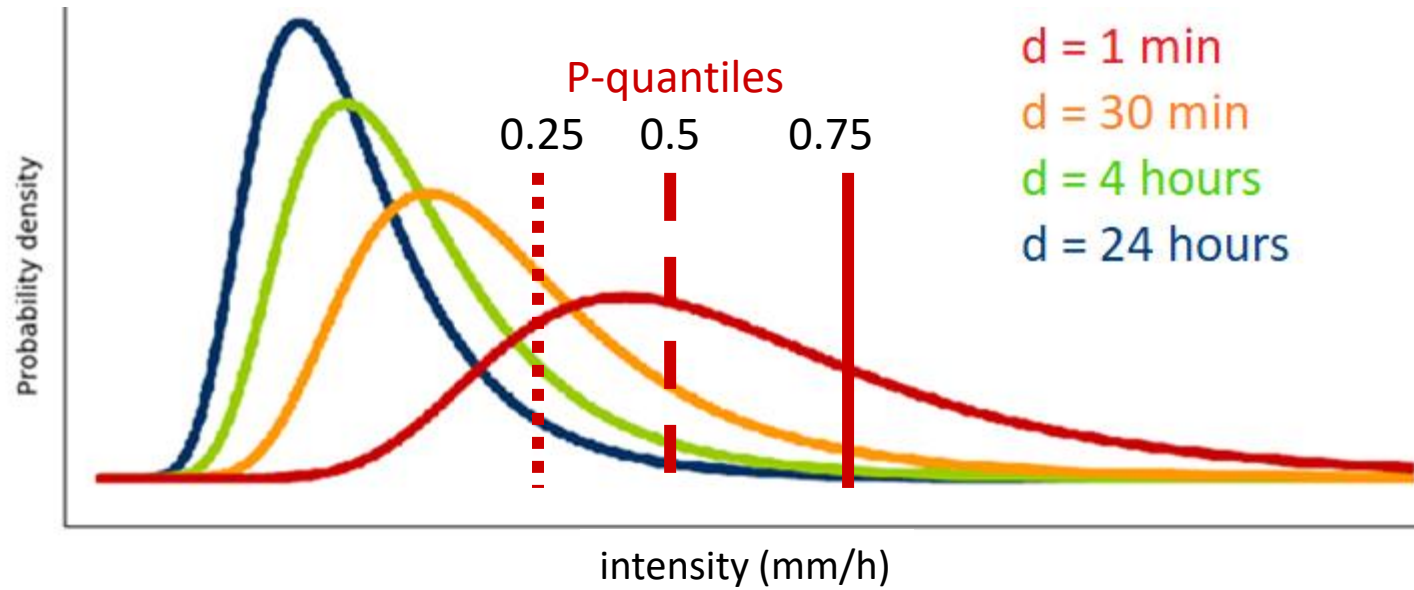
Accumulated precipitation sums d

GEV - curves



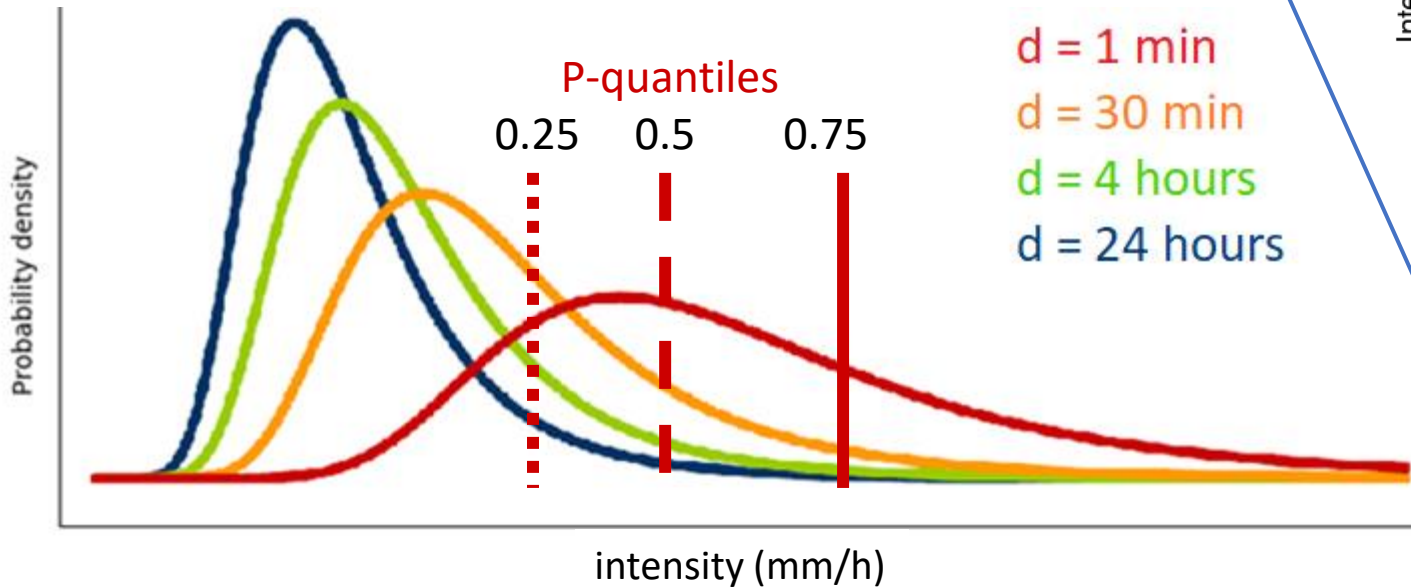
Accumulated precipitation sums d

GEV - curves



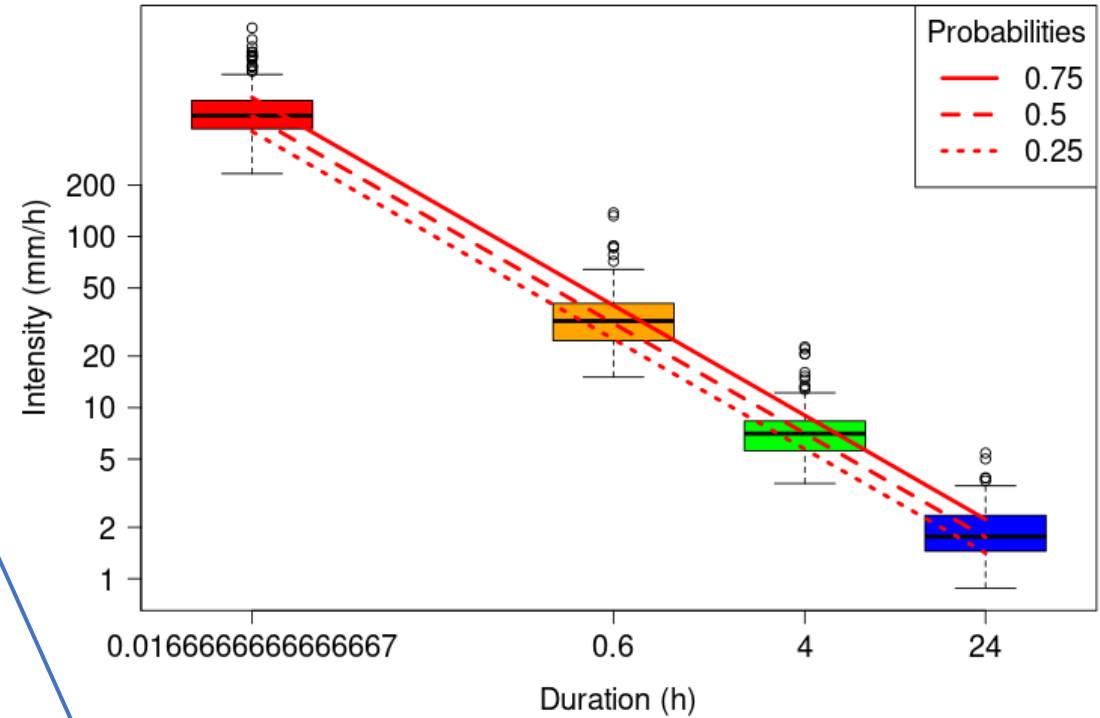
Accumulated precipitation sums d

GEV - curves



IDF curve

Intensity-duration-frequency



Smooth dependency
Duration → intensity

d-GEV

$$G(z; \mu, \sigma, \xi) = \exp \left\{ - \left[1 + \xi \left(\frac{z - \mu(d)}{\sigma(d)} \right) \right]^{-1/\xi} \right\}$$

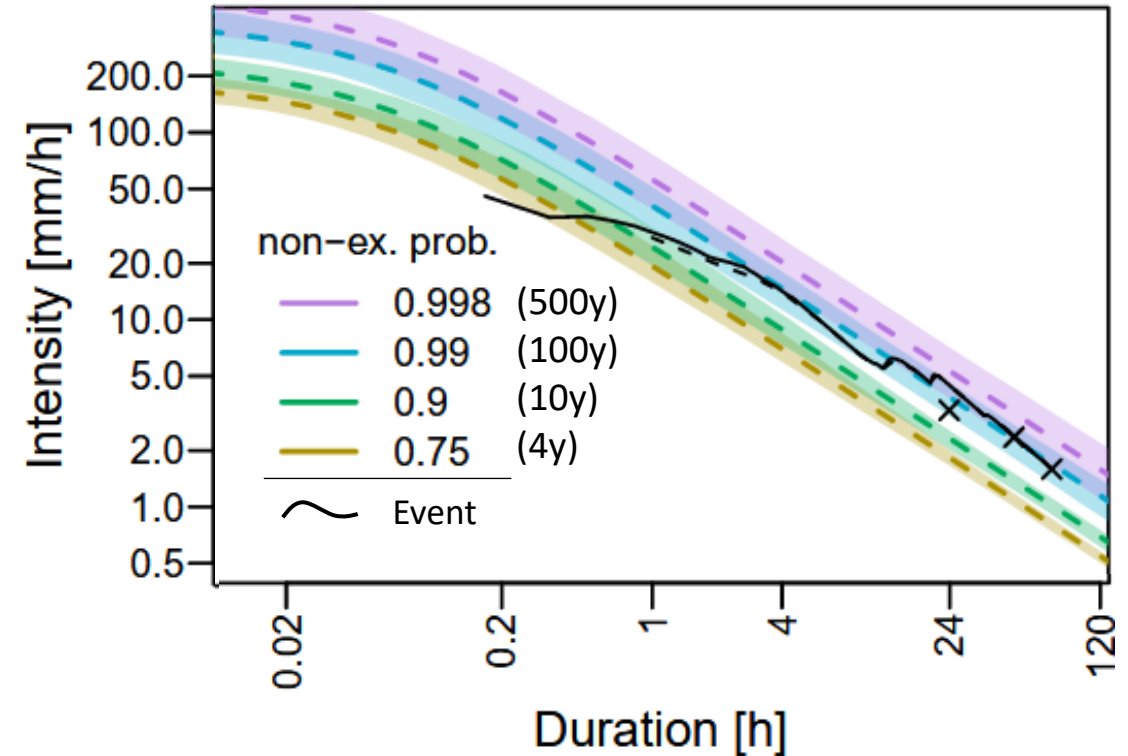
(scale) $\sigma(d)$

(location) $\mu(d)$

(shape) $\xi(d)$

IDF curve

Intensity-duration-frequency



→ Koutsoyiannis et al., 1998
 → Gupta and Waymire, 1990
 → Fauer et al., 2021

d-GEV

$$G(z; \mu, \sigma, \xi) = \exp \left\{ - \left[1 + \xi \left(\frac{z - \mu(d)}{\sigma(d)} \right) \right]^{-1/\xi} \right\}$$

(scale) $\sigma(d) = \sigma_0 (d + \theta)^{-(\eta_1 + \eta_2)} + \tau$

(location) $\mu(d) = \tilde{\mu} (\sigma_0 (d + \theta)^{-\eta_1} + \tau)$

(shape) $\xi(d) = \xi$ [constant]

New d-GEV parameters:

d Duration (accumulation period)

$\tilde{\mu}$ rescaled location

σ_0 normalized scale

θ duration offset (curvature)

ξ shape

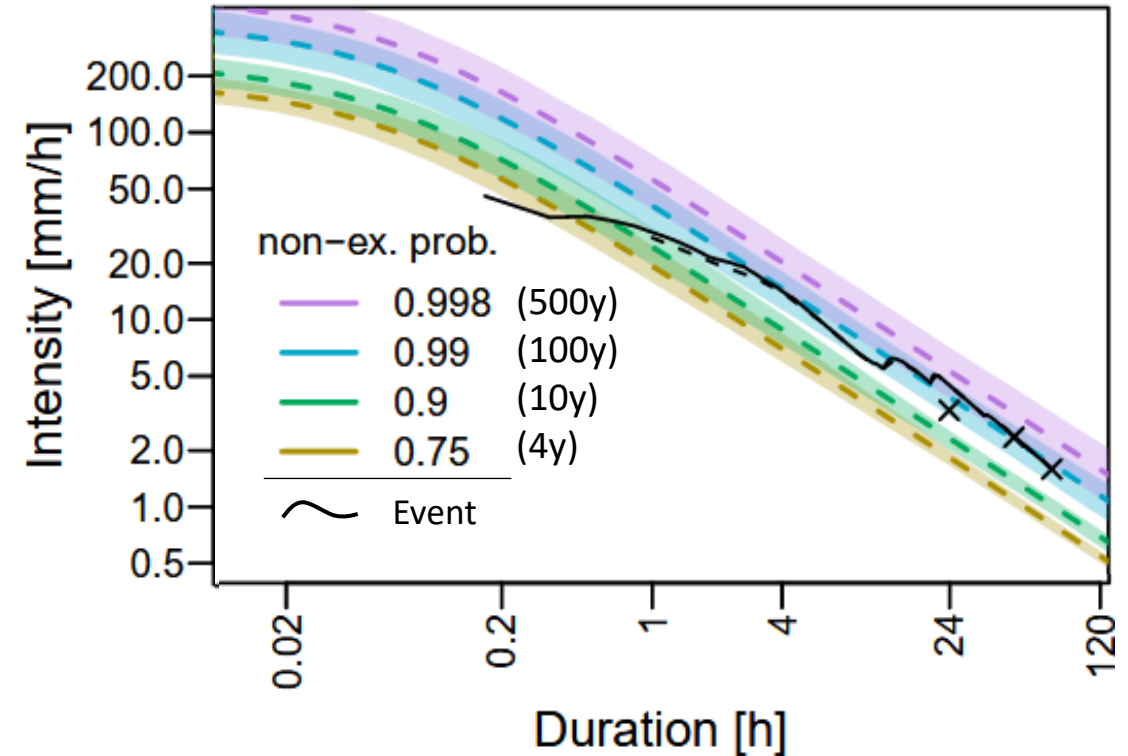
η_1 duration exponent (slope)

η_2 2nd duration exponent (multiscaling)

τ intensity offset (flattening)

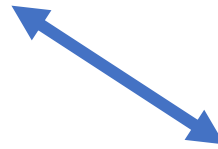
IDF curve

Intensity-duration-frequency



→ Koutsoyiannis et al., 1998
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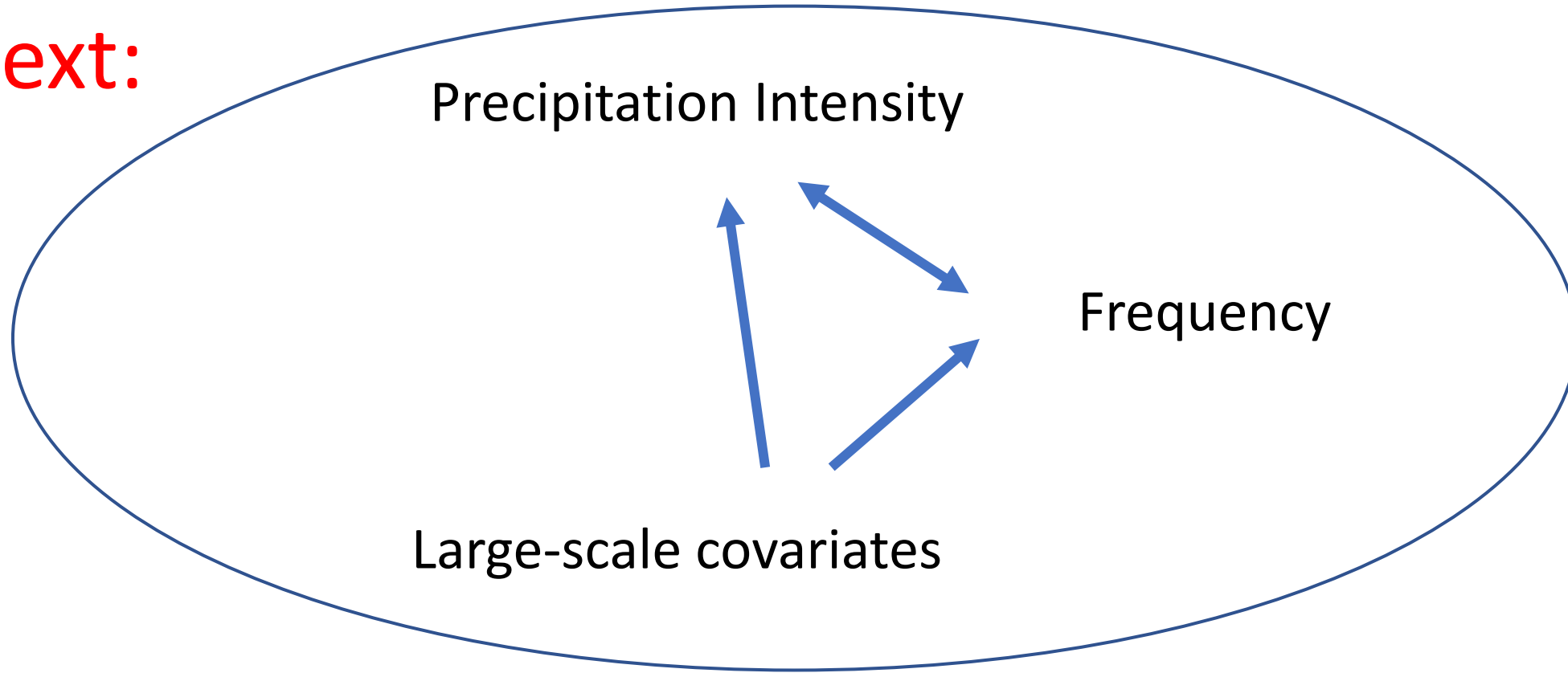
Precipitation Intensity



Frequency

→ Distribution parameters: function of large-scale variable

Next:



Distribution parameters: function of large-scale variable

All d-GEV parameters are linear models,
depending on large-scale covariates,
4th order

Example for dependencies of location:

$$\tilde{\mu} = \beta_0 + \beta_1 \text{NAO} + \beta_2 \text{temperature}^2$$

Distribution parameters: function of large-scale variable

All d-GEV parameters are linear models,
depending on large-scale covariates,
4th order

Example for dependencies of location:

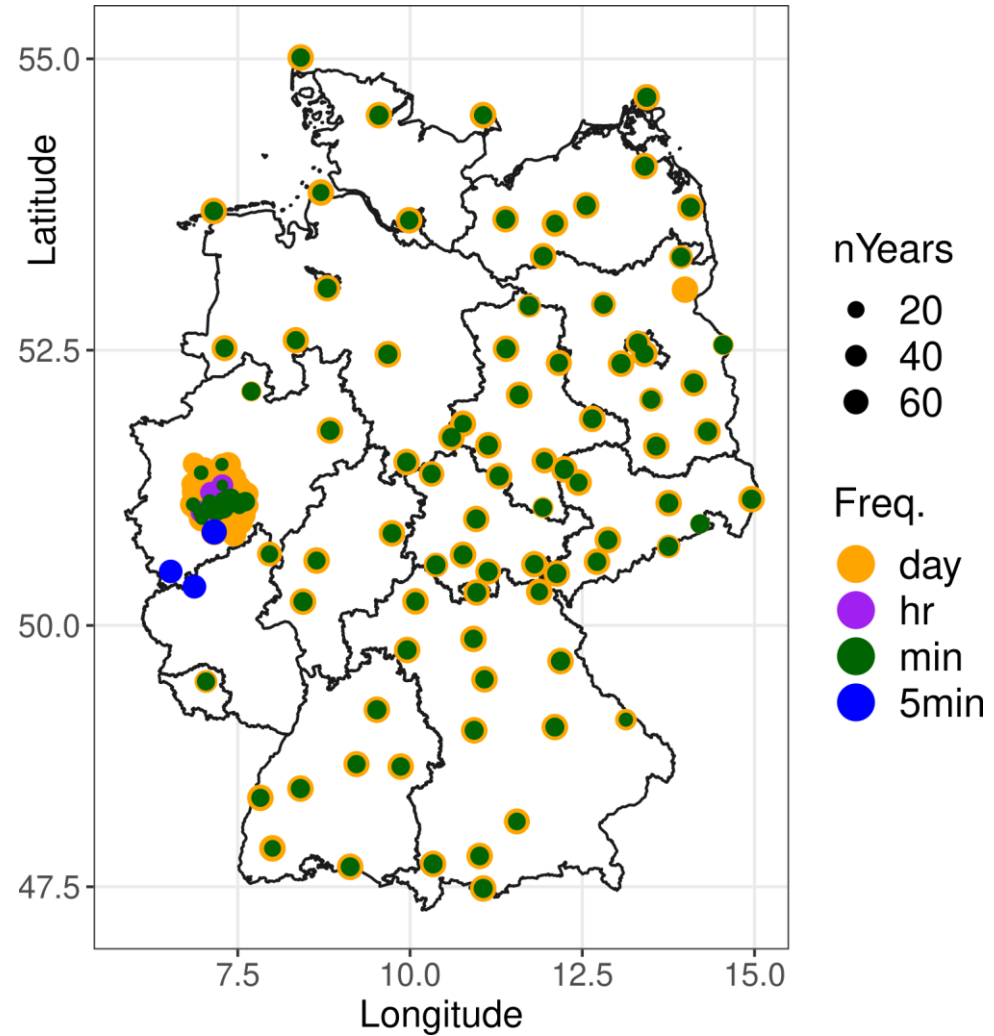
$$\tilde{\mu} = \beta_0 + \beta_1 \text{NAO} + \beta_2 \text{temperature}^2$$

- Same for all d-GEV parameters
- Stepwise BIC model selection
- Cross-validated (2-fold)

Data

Precipitation

- station-based data



(Fauer, Rust, 2023)

Data

Precipitation

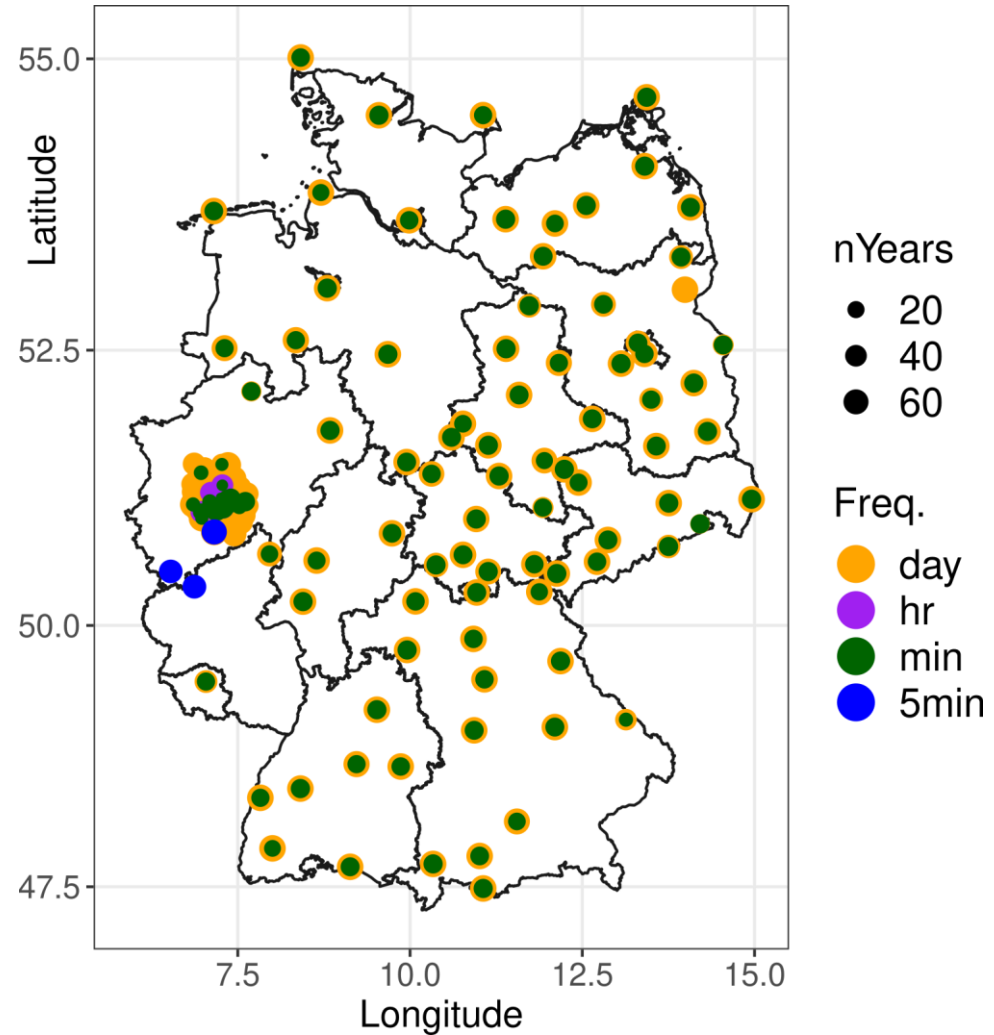
- station-based data

Large-Scale variables

- North Atlantic Oscillation (NOAA)
- Temperature and humidity (ERA5)
- Binary Blocking-Index (BBI) (ERA5)

→ all 1950-2015

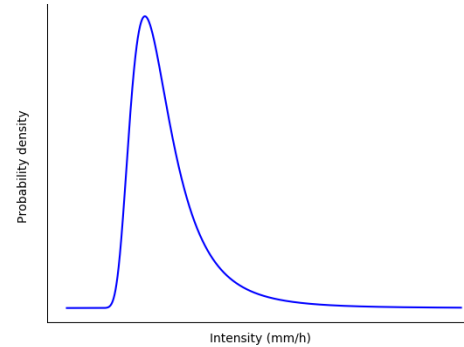
→ all averaged over month/year



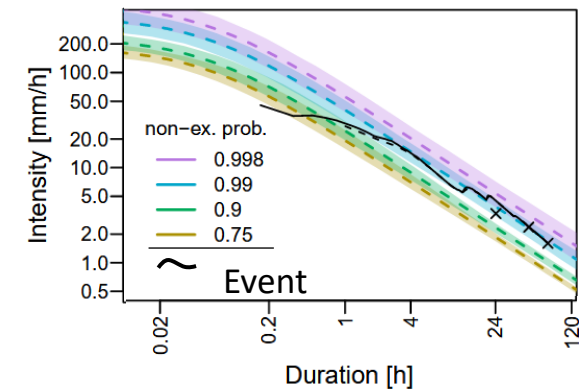
(Fauer, Rust, 2023)

Summary of methods

1. Model distribution of extremes (GEV)



2. Include duration dependence of GEV – parameters (\rightarrow d-GEV)




3. Include large-scale dependence of d-GEV parameters

$$\tilde{\mu} = f(\text{NAO}, \dots)$$

$$\sigma_0 = f(\text{time}, \dots)$$

Results

Large-scale dependencies in the **past**

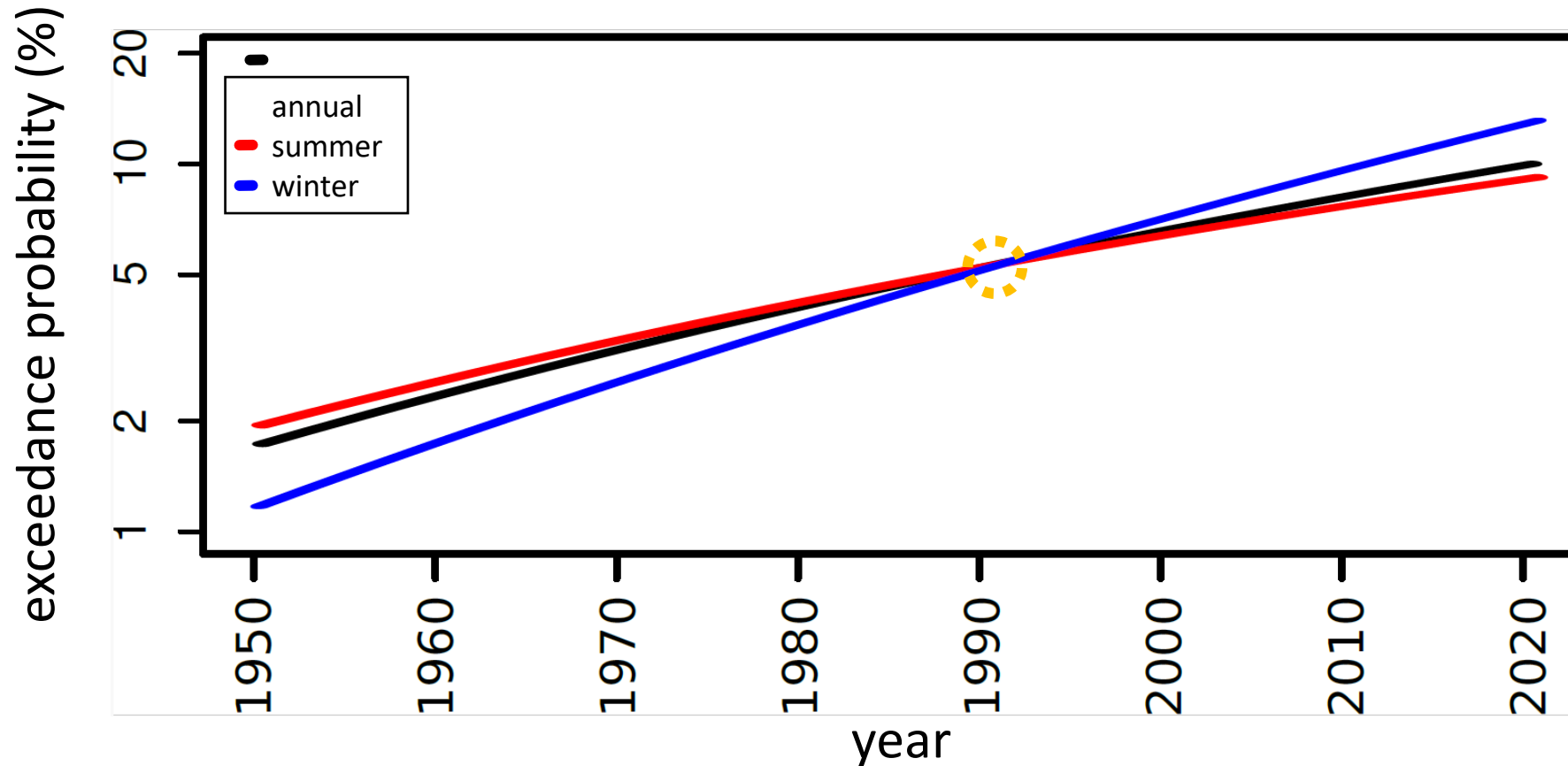
- define a reference event 
- simulate changes of probability \updownarrow in changing large scale conditions \leftrightarrow
- other parameters are fixed



Reference event at

- Probability $p = 5\%$
- Year $y = 1990$
- NAO $n = 0$
- Temperature $T = 10^\circ\text{C}$
- Blocking $b = 0$
- Humidity $h = 75\%$


One station
Bever-Talsperre



(Fauer, Rust, 2023)

Results

Large-scale dependencies in the **past**

- define a reference event 
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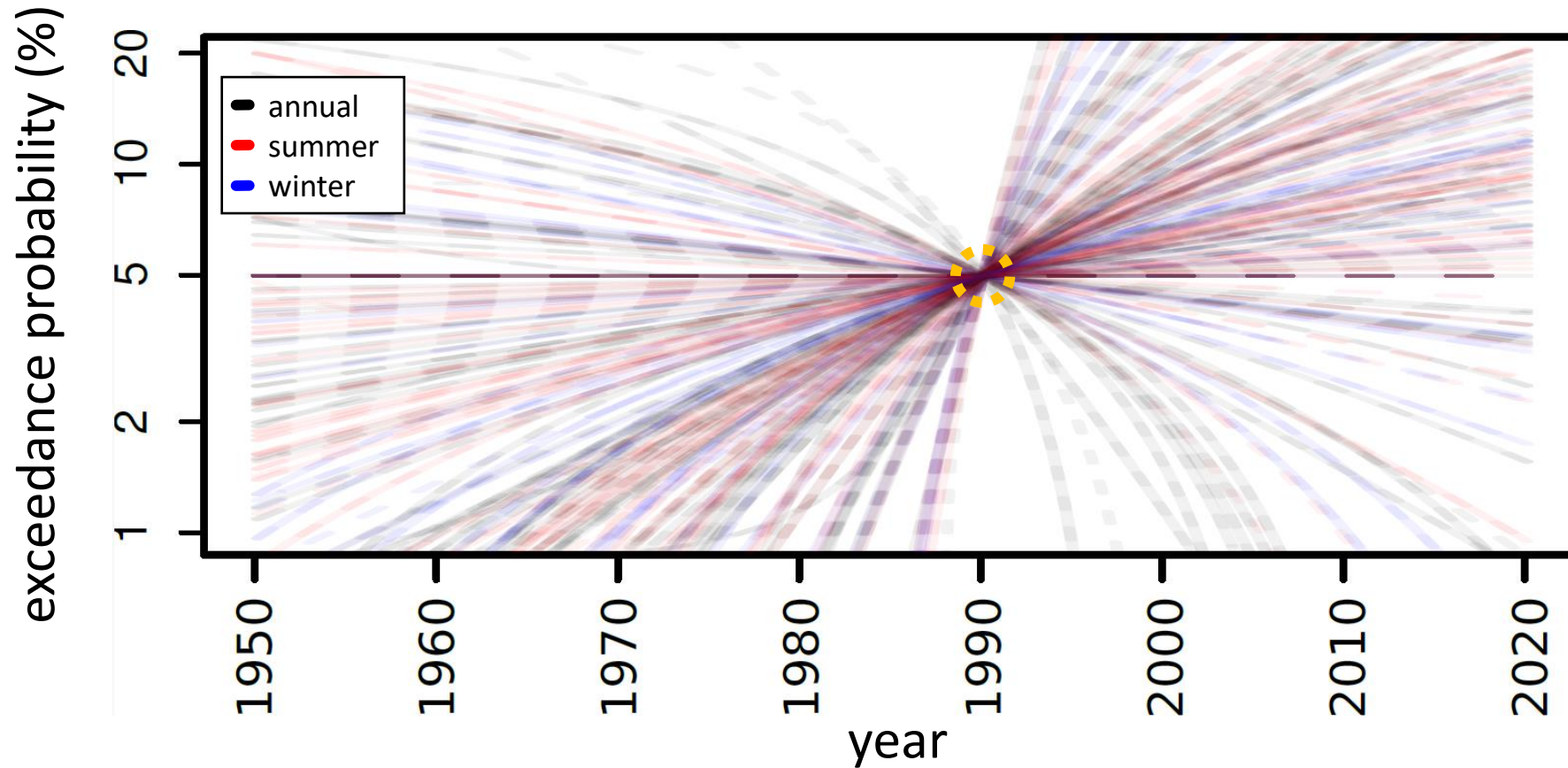


Reference event at

- Probability $p = 5\%$
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- Temperature $T = 10^\circ\text{C}$
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All Stations

(Fauer, Rust, 2023)



Results

Large-scale dependencies in the **past**

- define a reference event 
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- other parameters are fixed

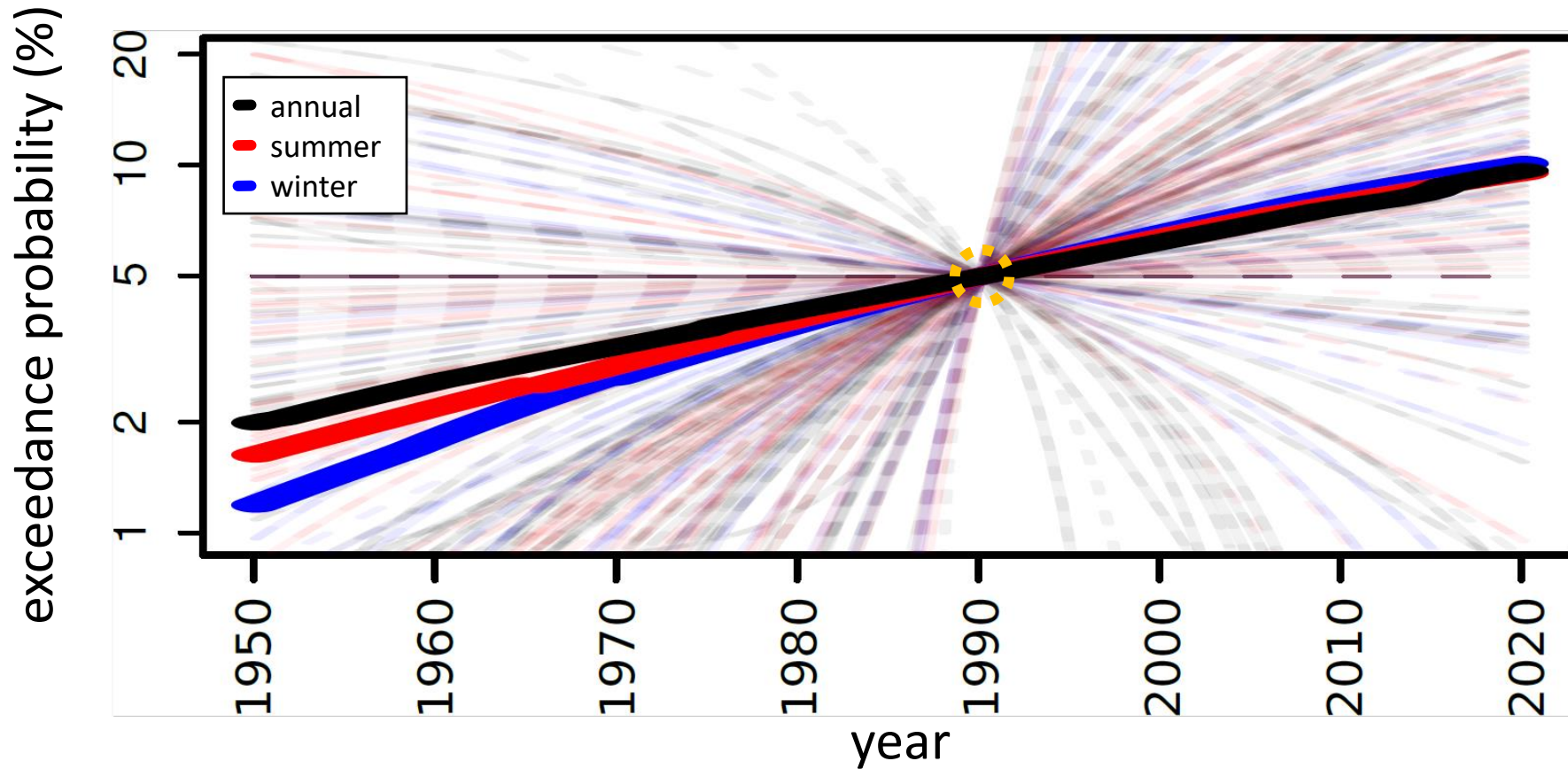


Reference event at

- Probability $p = 5\%$
- Year $y = 1990$
- NAO $n = 0$
- Temperature $T = 10^\circ\text{C}$
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- Humidity $h = 75\%$




Median over all stations




(Fauer, Rust, 2023)

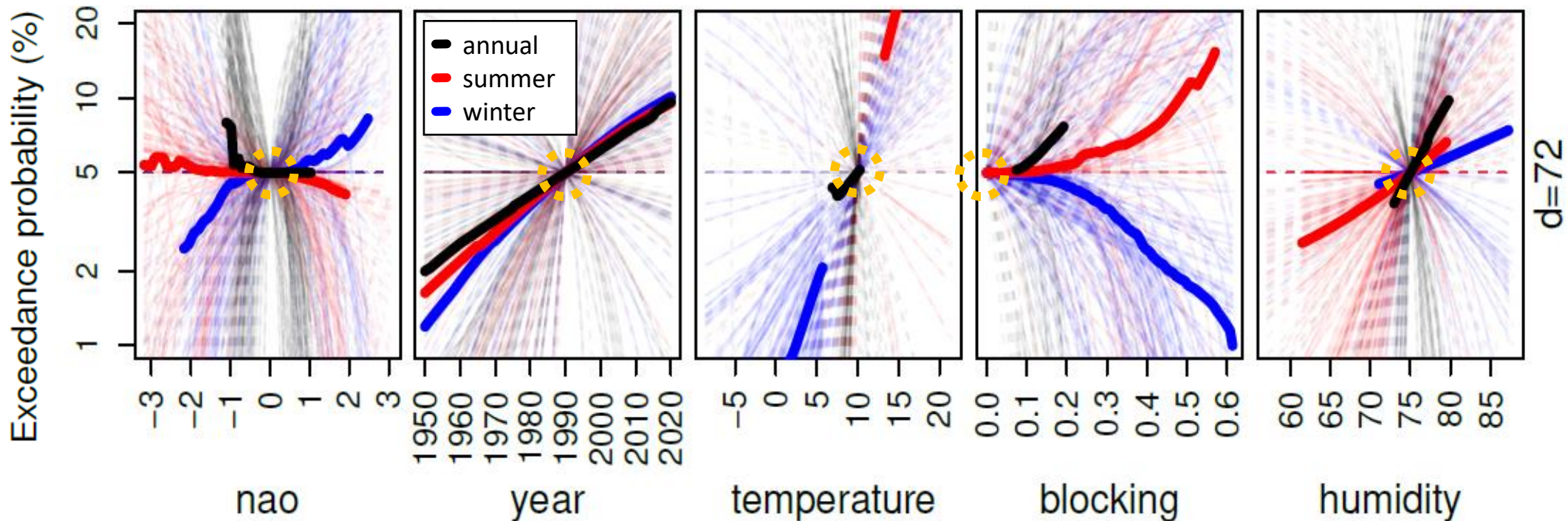
Results

Large-scale dependencies in the **past**

- define a reference event 
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 Median over all stations

-  Reference event at
- Probability $p = 5\%$
 - Year $y = 1990$
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 - Blocking $b = 0$
 - Humidity $h = 75\%$

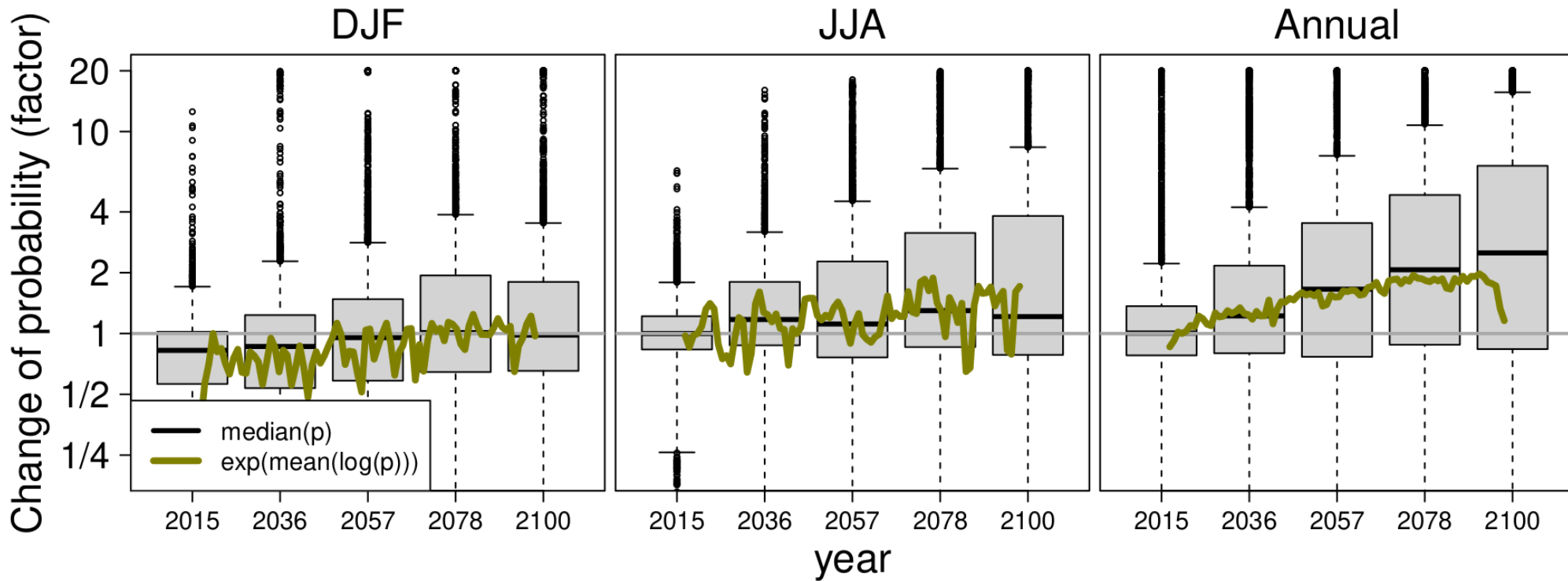
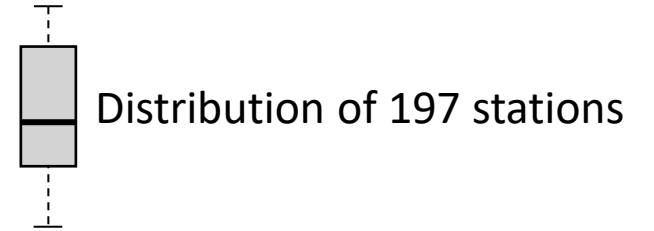


(Fauer, Rust, 2023)

Results

Large-scale dependencies – Future Projections

- Simulate changes of probability \updownarrow in changing large-scale conditions \leftrightarrow
- Use projections from MPI-ESM for temperature, humidity, blocking, year (5y running mean)



Use our R library *IDF* 😊

available on CRAN

```
library(IDF)
```

```
# aggregate precip sums
```

```
block_maxima = IDF.agg(data, ds)
```

```
# estimate d-GEV parameters
```

```
fit = gev.d.fit(block_maxima$xdat, block_maxima$ds)
```

```
# plot IDF-curves
```

```
IDF.plot(ds, gev.d.parameters(fit), lwd=3)
```

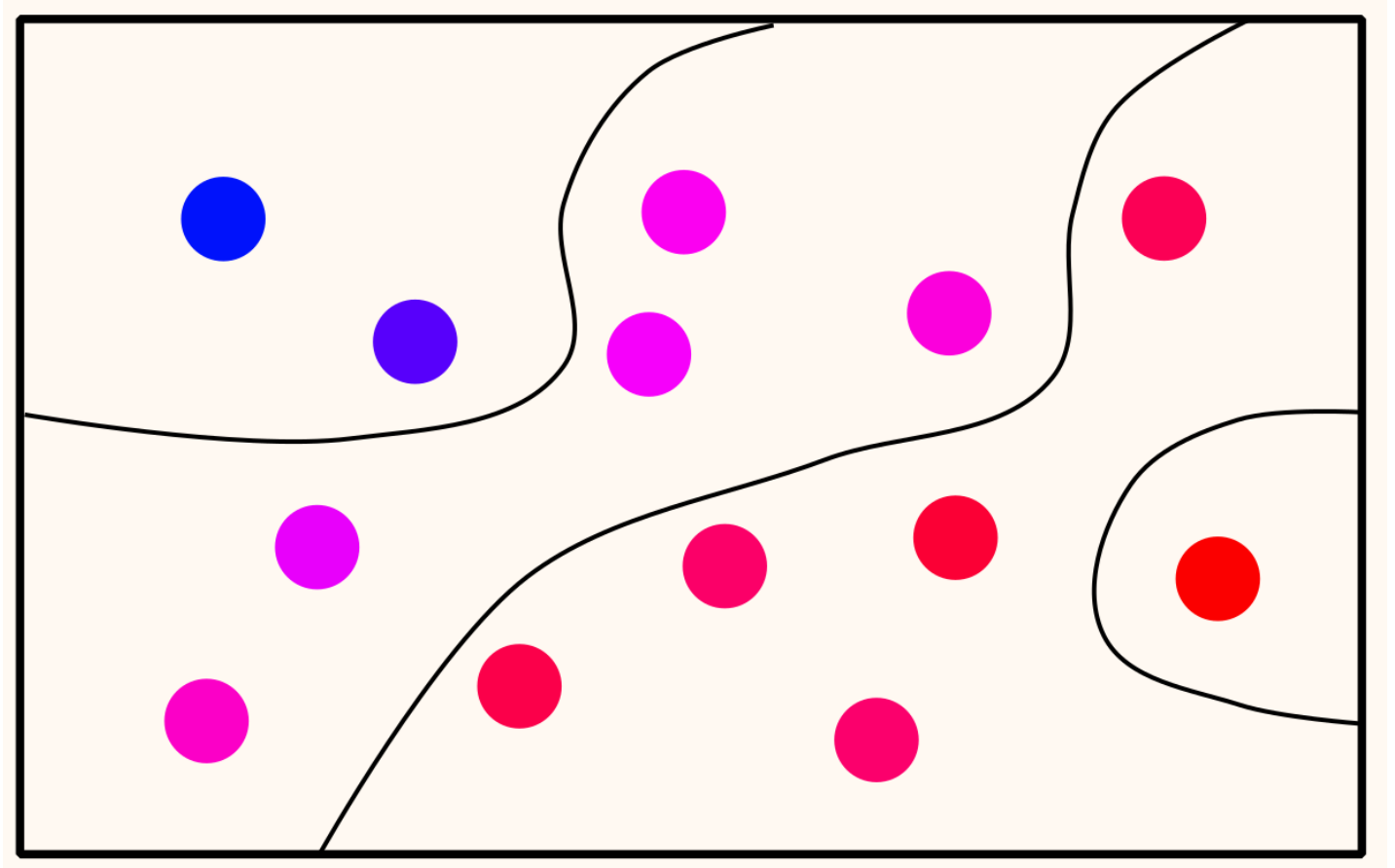
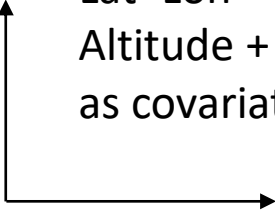
- convenient aggregation
- Parallelize processes
- Easy inclusion of covariates
- Extract parameters
- Plot IDF curves
- Customize your plots

Find more information about d-GEV parameters:
Fauer et al, 2021

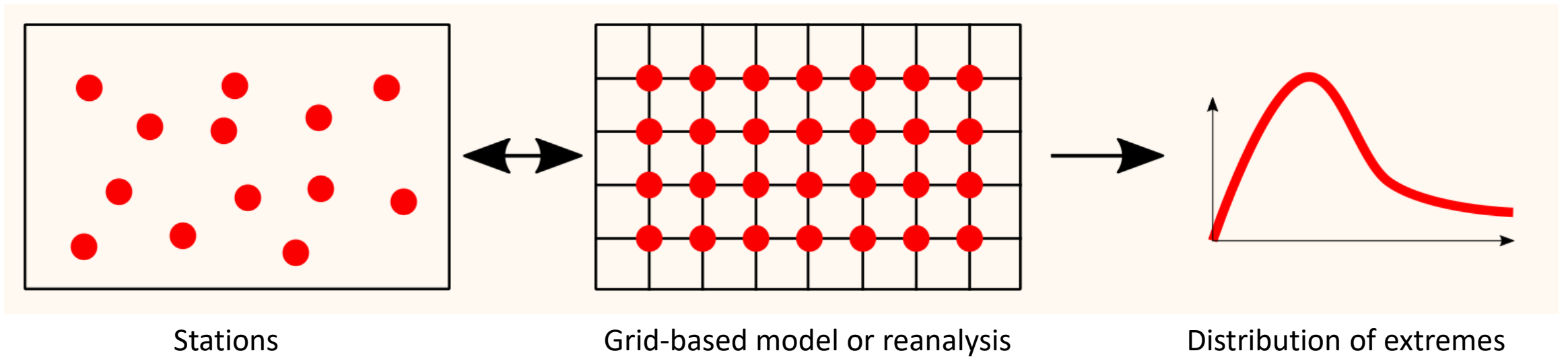
Future Plans - Outlook

- Exploit smoothness in space for the flexible IDF model based on location covariates

Lat+Lon +
Altitude + slope
as covariates



- Develop approaches to combine gridded data sets (high spatial resolution) and station-based data (long time records)



- Identify further meaningful covariates
- Focus on methods to prevent overfitting

Topography

Land cover

Altitude

Slope



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Non-stationary large-scale statistics of precipitation extremes in central Europe

Original Paper | Open access | Published: 23 July 2023

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Abstract

Extreme precipitation shows non-stationarity, meaning that its distribution can change with time or other large-scale variables. For a classical frequency-intensity analysis this effect is often neglected. Here, we propose a model including the influence of North Atlantic Oscillation, time, surface temperature and a blocking index. The model features flexibility to use annual maxima as well as seasonal maxima to be fitted in a generalized extreme value setting. To further increase the efficiency of data usage, maxima from different accumulation durations are aggregated so that information for extremes on different time scales can be provided. Our model is trained to individual station data with temporal resolutions ranging from one minute to one day across Germany. Models are chosen with a stepwise BIC model selection and verified with a cross-validated quantile skill index. The verification shows that the new model performs better than a reference model without large-scale information. Also, the new model enables insights into the

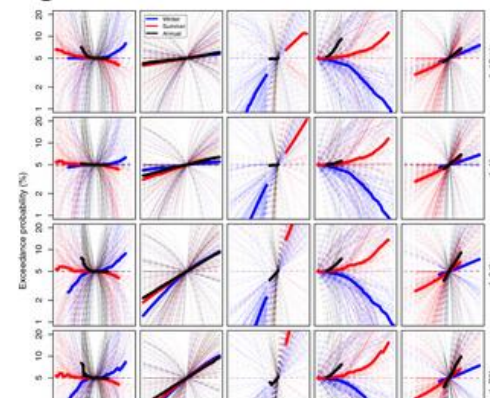
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Sections Figures References

Fig. 6



Thank you for Listening



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[https://doi.org/10.1016/S0022-1694\(98\)00097-3](https://doi.org/10.1016/S0022-1694(98)00097-3)
- **Fauer, FS, Rust, HW** (2023) Non-stationary large-scale statistics of precipitation extremes in central Europe. Stoch Environ Res Risk Assess 37, 4417–4429.
<https://doi.org/10.1007/s00477-023-02515-z>